

The $(g-2)_\mu$ in Lepton-specific 2HDM

Eung Jin Chun

In collaboration with A. Broggio, M. Passera, K.M. Patel, S.K. Vempati, arXiv:1409.3199;
Z. Kang, M. Takeuchi, Y.L.S. Tsai, work in progress.

Introduction

- "Can the muon $g-2$ be accounted for in 2HDMs?"

$$\Delta a_\mu \equiv a_\mu^{\text{EXP}} - a_\mu^{\text{SM}} = +262(85) \times 10^{-11}$$

a lot of studies in SUSY, much less in 2HDMs...

0102145, 146, 147, ... vs. Dedes, Haber, 0102297

Cheung, Chou, Kong, 0103183

- Constraints from the 126 GeV Higgs data at LHC.
- Extra Higgs spectrum constrained by EWPD, vacuum stability & perturbativity, and also by $B_q \rightarrow X_s \gamma, \mu^+ \mu^-, \text{etc.}$
- The unique choice: Type X with Barr-Zee two loop in the ranges of $20 < m_A(\text{GeV}) < 120$, $t_\beta > 50$, & $200 < m_H \sim m_{H^\pm}(\text{GeV}) < 600$.

2HDMs

- Two Higgs Doublets:

$$\Phi_{1,2} = (\phi_{1,2}^+, \frac{1}{\sqrt{2}} [v_{1,2} + \rho_{1,2} + i \eta_{1,2}]) \rightarrow h, H, A, H^\pm; \quad t_\beta = \frac{v_1}{v_2}$$

$$G^0 = \eta_1 c_\beta + \eta_2 s_\beta \quad h = \rho_1 c_\alpha - \rho_2 s_\alpha$$

$$A = \eta_1 s_\beta - \eta_2 c_\beta \quad H = \rho_1 s_\alpha + \rho_2 c_\alpha$$

- Gauge coupling: $\mathcal{L}_g = g_V m_V (s_{\beta-\alpha} h + c_{\beta-\alpha} H) VV + \dots$
- FCNC: Mass diagonalization \neq Yukawa diagonalization

$$\mathcal{L}_{Yuk} = y_{ij}^{u2} \Phi_2 q_i u_j^c + y_{ij}^{dp} \Phi_p q_i d_j^c + y_{ij}^{eq} \Phi_q l_i e_j^c + h.c.$$

$$M_{ij}^f = y_{ij}^{f1} \frac{v_1}{\sqrt{2}} + y_{ij}^{f2} \frac{v_2}{\sqrt{2}} \rightarrow y_{ij}^d h d_i d_j^c + \dots$$

4 types of 2HDMs

Natural flavor conservation imposed by Z_2 :
only one Higgs to each Yukawa type (d, e)

Nb) Type III : aligned Yukawa
 $y_{ij}^1 \sim y_{ij}^2$

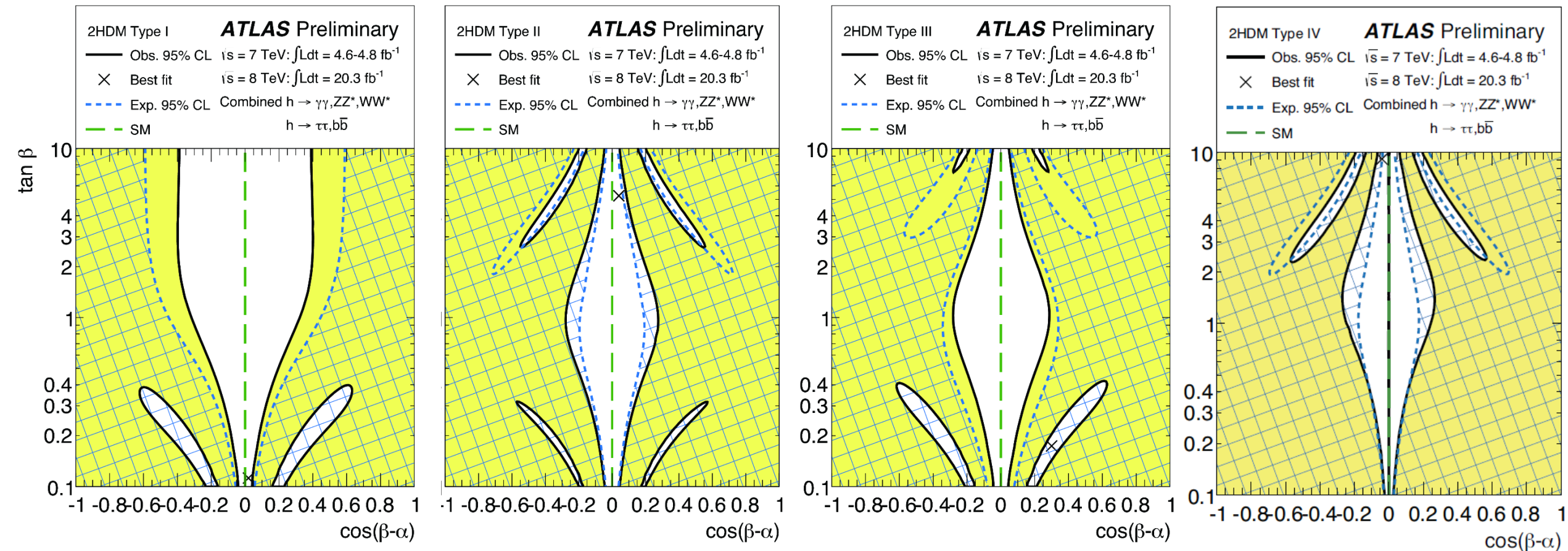
$\Phi_2(+), \Phi_1(-); t_R(+), d_R(\pm), e_R(\pm)$

Model	u_R^i	d_R^i	e_R^i		y_u^A	y_d^A	y_l^A	y_u^H	y_d^H	y_l^H	y_u^h	y_d^h	y_l^h
Type I	Φ_2	Φ_2	Φ_2	Type I	$\cot \beta$	$-\cot \beta$	$-\cot \beta$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$
Type II	Φ_2	Φ_1	Φ_1	Type II	$\cot \beta$	$\tan \beta$	$\tan \beta$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$-\frac{\sin \alpha}{\cos \beta}$	$-\frac{\sin \alpha}{\cos \beta}$
Lepton-specific	Φ_2	Φ_2	Φ_1	Type X	$\cot \beta$	$-\cot \beta$	$\tan \beta$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$-\frac{\sin \alpha}{\cos \beta}$
Flipped	Φ_2	Φ_1	Φ_2	Type Y	$\cot \beta$	$\tan \beta$	$-\cot \beta$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$-\frac{\sin \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\sin \beta}$

$$\begin{aligned}
 \mathcal{L}_{\text{Yukawa}}^{\text{2HDM}} = & - \sum_{f=u,d,\ell} \frac{m_f}{v} \left(\xi_h^f \bar{f} f h + \xi_H^f \bar{f} f H - i \xi_A^f \bar{f} \gamma_5 f A \right) \\
 & \quad \quad \quad 126 \text{ GeV} \\
 & - \left\{ \frac{\sqrt{2} V_{ud}}{v} \bar{u} (m_u \xi_A^u P_L + m_d \xi_A^d P_R) d H^+ + \frac{\sqrt{2} m_\ell \xi_A^\ell}{v} \bar{\nu}_L \ell_R H^+ + \text{H.c.} \right\}
 \end{aligned}$$

126 GeV SM Higgs: $g_{hVV} = \sin(\beta - \alpha) \approx 1$

ATLAS-CONF-2014-010



Aligned/decoupled 2HDMs

$$\begin{aligned}
 V_H = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - \left(m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{H.c.} \right) \\
 & + \frac{1}{2} \lambda_1 \left(\Phi_1^\dagger \Phi_1 \right)^2 + \frac{1}{2} \lambda_2 \left(\Phi_2^\dagger \Phi_2 \right)^2 + \lambda_3 \left(\Phi_1^\dagger \Phi_1 \right) \left(\Phi_2^\dagger \Phi_2 \right) + \lambda_4 \left(\Phi_1^\dagger \Phi_2 \right) \left(\Phi_2^\dagger \Phi_1 \right) \\
 & + \left[\frac{1}{2} \lambda_5 \left(\Phi_1^\dagger \Phi_2 \right)^2 + \cancel{\lambda_6 \left(\Phi_1^\dagger \Phi_1 \right) \left(\Phi_1^\dagger \Phi_2 \right)} + \cancel{\lambda_7 \left(\Phi_2^\dagger \Phi_2 \right) \left(\Phi_1^\dagger \Phi_2 \right)} + \text{H.c.} \right],
 \end{aligned}$$

Model	u_R^i	d_R^i	e_R^i		y_u^A	y_d^A	y_l^A	y_u^H	y_d^H	y_l^H	y_u^h	y_d^h	y_l^h
Type I	Φ_2	Φ_2	Φ_2	Type I	$\cot \beta$	$-\cot \beta$	$-\cot \beta$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$
Type II	Φ_2	Φ_1	Φ_1	Type II	$\cot \beta$	$\tan \beta$	$\tan \beta$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$-\frac{\sin \alpha}{\cos \beta}$	$-\frac{\sin \alpha}{\cos \beta}$
Lepton-specific	Φ_2	Φ_2	Φ_1	Type X	$\cot \beta$	$-\cot \beta$	$\tan \beta$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$-\frac{\sin \alpha}{\cos \beta}$
Flipped	Φ_2	Φ_1	Φ_2	Type Y	$\cot \beta$	$\tan \beta$	$-\cot \beta$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$-\frac{\sin \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\sin \beta}$

$$\begin{aligned}
 \mathcal{L}_{\text{Yukawa}}^{\text{2HDM}} = & - \sum_{f=u,d,\ell} \frac{m_f}{v} \left(\xi_h^f \bar{f} f h + \xi_H^f \bar{f} f H - i \xi_A^f \bar{f} \gamma_5 f A \right) \\
 & - \left\{ \frac{\sqrt{2} V_{ud}}{v} \bar{u} (m_u \xi_A^u P_L + m_d \xi_A^d P_R) d H^+ + \frac{\sqrt{2} m_\ell \xi_A^\ell}{v} \bar{\nu}_L \ell_R H^+ + \text{H.c.} \right\}
 \end{aligned}$$

126 GeV

1

LHC Higgs data
 $\cos(\beta - \alpha) \approx 0$

Muon $g-2$

● One-loop contribution:

$$\delta a_{\mu}^{2\text{HDM}}(1\text{loop}) = \frac{G_F m_{\mu}^2}{4\pi^2 \sqrt{2}} \sum_{j=h,H,A,H^{\pm}} (y_{\mu}^j)^2 r_{\mu}^j f_j(r_{\mu}^j)$$

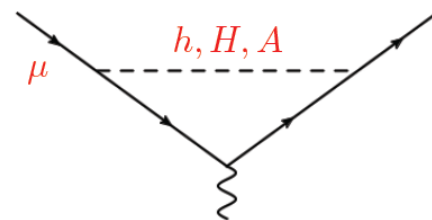
For $r_{\mu}^j = m_{\mu}^2/M_j^2 \ll 1$:

$$f_{h,H}(r) \sim -\ln r - 7/6 + O(r) > 0$$

$$f_A(r) \sim +\ln r + 11/6 + O(r) < 0$$

$$f_{H^{\pm}}(r) \sim -1/6 + O(r) < 0$$

roughly scales with m_{μ}^4 !



● Two-loop Barr-Zee type diagrams:

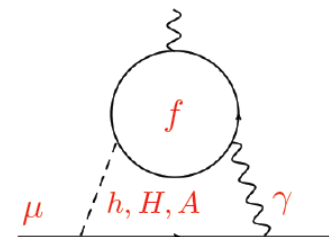
$$\delta a_{\mu}^{2\text{HDM}}(2\text{loop} - \text{BZ}) = \frac{G_F m_{\mu}^2}{4\pi^2 \sqrt{2}} \frac{\alpha_{\text{em}}}{\pi} \sum_{f; i=h,H,A} N_f^c Q_f^2 y_{\mu}^i y_f^i r_f^i g_i(r_f^i)$$

m_f^2/m_{μ}^2 w.r.t. 1 loop

$$g_{h,H}(r) < 0$$

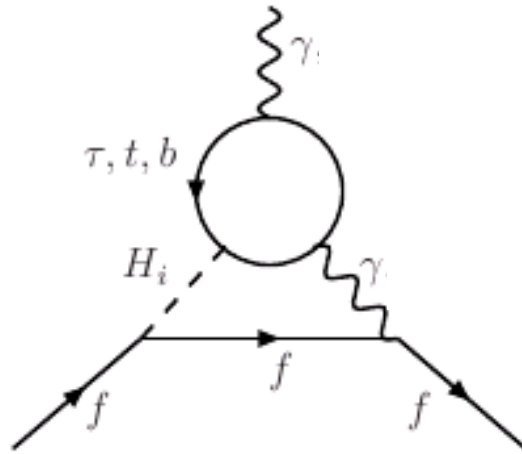
$$g_A(r) > 0$$

**Type II, $M_A \gtrsim 3\text{GeV}$ & $\tan\beta \gtrsim 5$:
(2loop)_A > (1loop)_A. Similar for X.**



Muon $g-2$ vs. $b \rightarrow s \gamma$

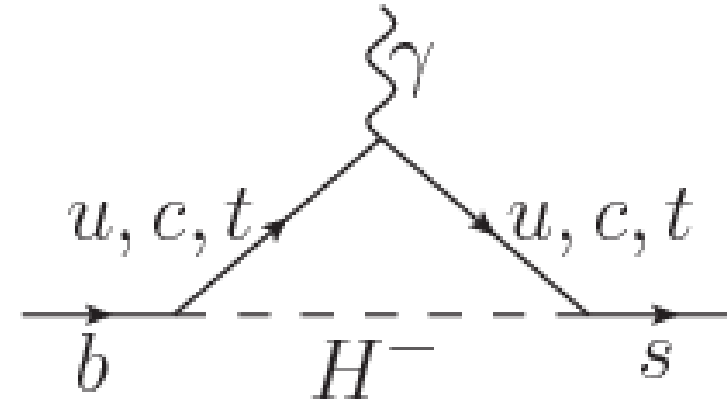
Cheung, Chou, Kong, 0103183
Cao, et.al, 0909.5148



$$\delta a_{\mu}^{2\text{loop}}(\gamma\text{BZ}) = \frac{G_F m_{\mu}^2}{4\pi^2 \sqrt{2}} \frac{\alpha_{\text{em}}}{\pi} \sum_{i,f} N_f^c Q_f^2 y_{\mu}^i y_f^i r_f^i g_i(r_f^i)$$

	τ	t	b
I	$1/t_{\beta}^2$	$-1/t_{\beta}^2$	$1/t_{\beta}^2$
II	t_{β}^2	1	t_{β}^2
X	t_{β}^2	1	-1
Y	$1/t_{\beta}^2$	$-1/t_{\beta}^2$	-1

H : negative
A : positive



$$\frac{m_t}{t_{\beta}} P_L - \frac{m_b}{t_{\beta}} P_R \quad (I, X) \quad \text{NA} \quad \text{for } t_{\beta} > 2$$

$$\frac{m_t}{t_{\beta}} P_L + m_b t_{\beta} P_R \quad (II, Y) \quad m_{H^{\pm}} > 380 \text{ GeV}$$

EWPD

$$M_W^2 = \frac{M_Z^2}{2} \left[1 + \sqrt{1 - \frac{4\pi\alpha}{\sqrt{2}G_F M_Z^2} \frac{1}{1 - \Delta r}} \right]$$

$$\sin^2 \theta_{\text{eff}}^{\text{lept}} = k_l (M_Z^2) \sin^2 \theta_W$$

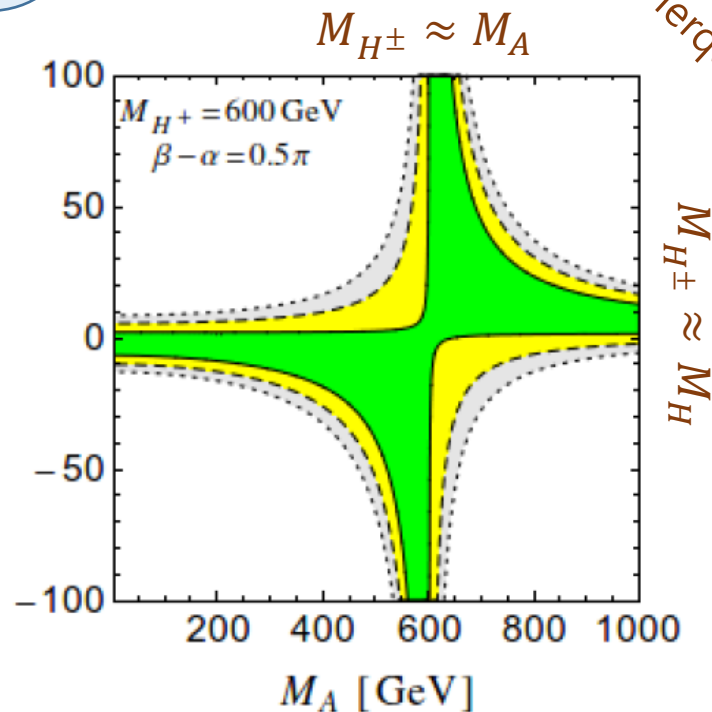
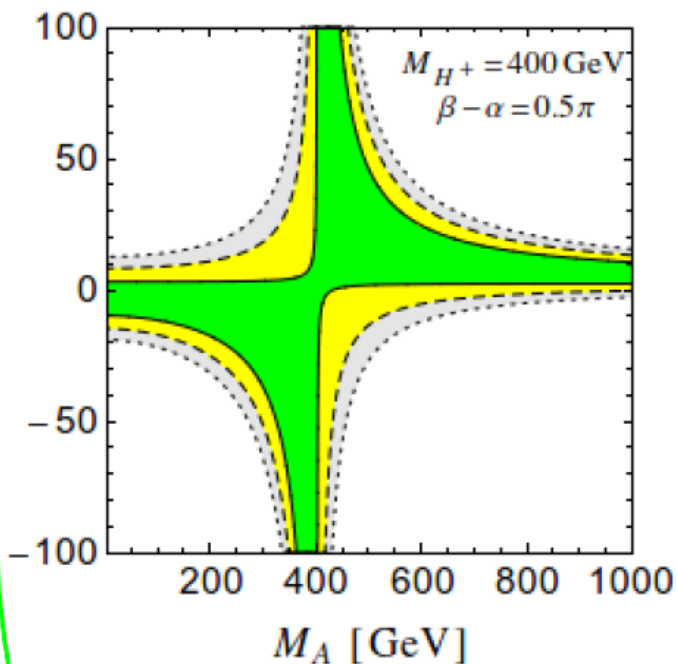
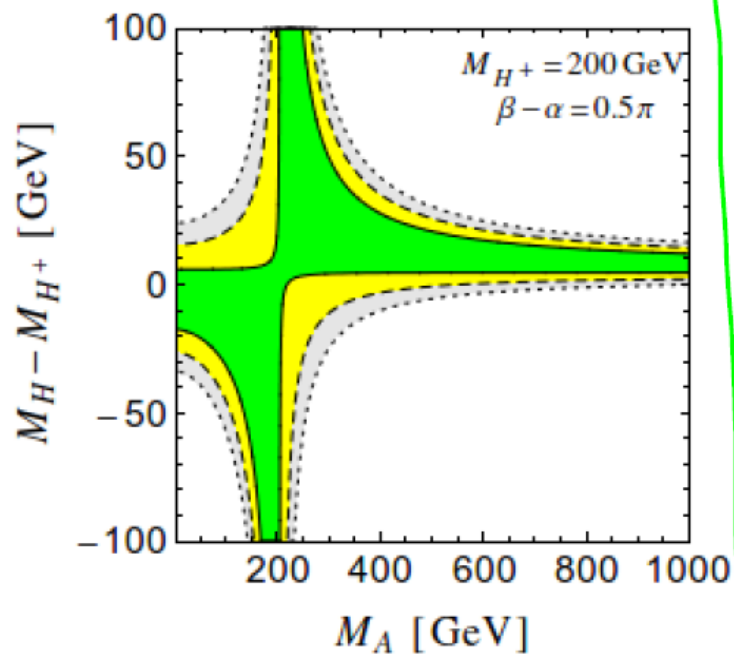
$$M_W^{\text{exp}} = 80.385 \pm 0.015 \text{ GeV},$$

$$\sin^2 \theta_{\text{eff}}^{\text{lept, exp}} = 0.23153 \pm 0.00016.$$

$$\Delta r^{2\text{HDM}} = \Delta \alpha^{2\text{HDM}} - \frac{\cos^2 \theta_W}{\sin^2 \theta_W} \Delta \rho^{2\text{HDM}} + \dots,$$

$$\Delta k_l^{2\text{HDM}} = + \frac{\cos^2 \theta_W}{\sin^2 \theta_W} \Delta \rho^{2\text{HDM}} + \dots,$$

Twisted custodial symmetry:
Gerard-Herquet, 0703051



Vacuum stability & perturbativity

$$\lambda_{1,2} > 0, \quad \lambda_3 > -\sqrt{\lambda_1 \lambda_2}, \quad |\lambda_5| < \lambda_3 + \lambda_4 + \sqrt{\lambda_1 \lambda_2}$$

$$m_{12}^2(m_{11}^2 - m_{22}^2 \sqrt{\lambda_1/\lambda_2})(\tan \beta - (\lambda_1/\lambda_2)^{1/4}) > 0$$

$$M_A^2 = \frac{m_{12}^2}{\sin \beta \cos \beta} - \lambda_5 v^2,$$

$$M_{H^\pm}^2 = M_A^2 + \frac{1}{2} v^2 (\lambda_5 - \lambda_4).$$

For $\tan \beta \gg 1$ in the SM limit: $\sin(\beta - \alpha) = 1$,

$$\lambda_2 v^2 \simeq M_h^2 + \lambda_1 v^2 / \tan^4 \beta,$$

$$\lambda_3 v^2 \simeq 2M_{H^\pm}^2 - 2M_H^2 + M_h^2 + \lambda_1 v^2 / \tan^2 \beta,$$

$$m_{12}^2 \simeq M_H^2 / \tan \beta + (M_h^2 - \lambda_1 v^2) / \tan^3 \beta.$$

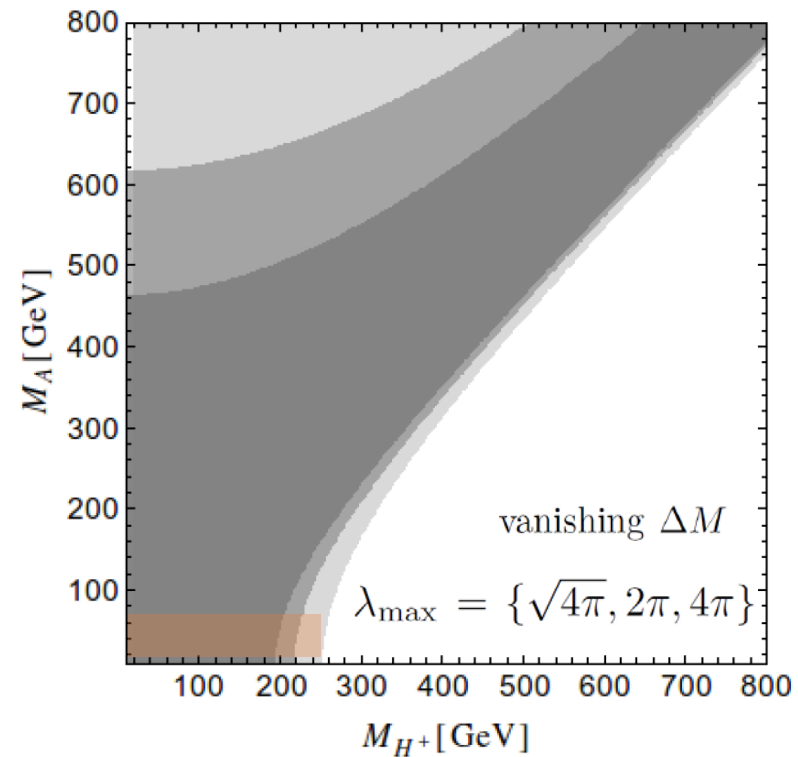
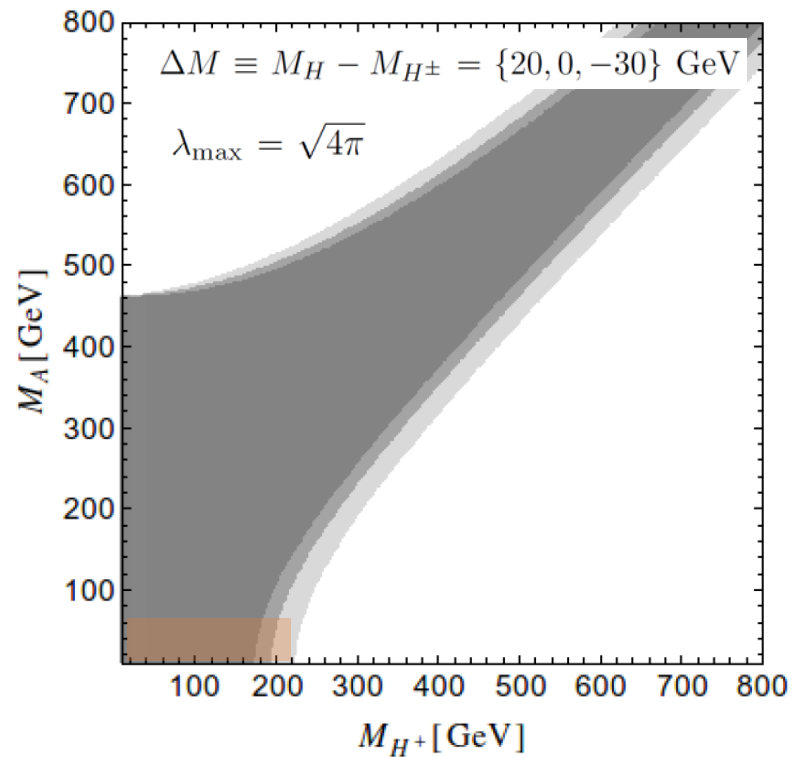
$$\lambda_2 v^2 \approx M_h^2$$

$$\lambda_3 v^2 \approx 2M_{H^\pm}^2 - 2M_H^2 + M_h^2$$

$$\lambda_4 v^2 \approx M_H^2 - 2M_{H^\pm}^2 + M_A^2$$

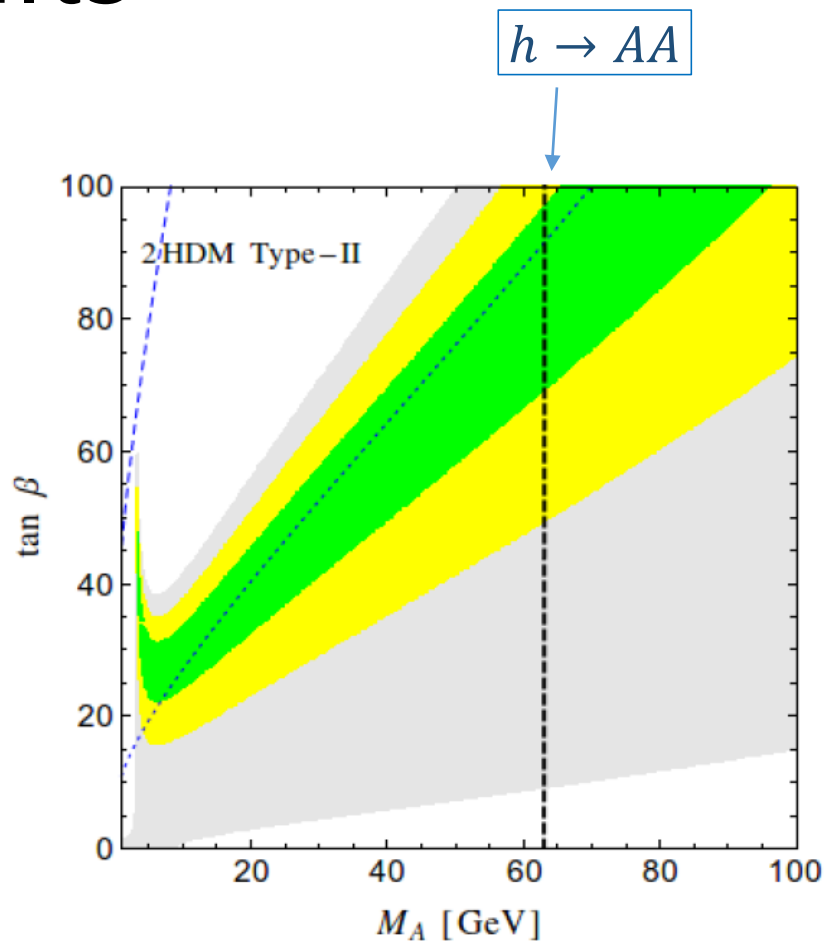
$$\lambda_5 v^2 \approx M_H^2 - M_A^2$$

Vacuum stability & perturbativity

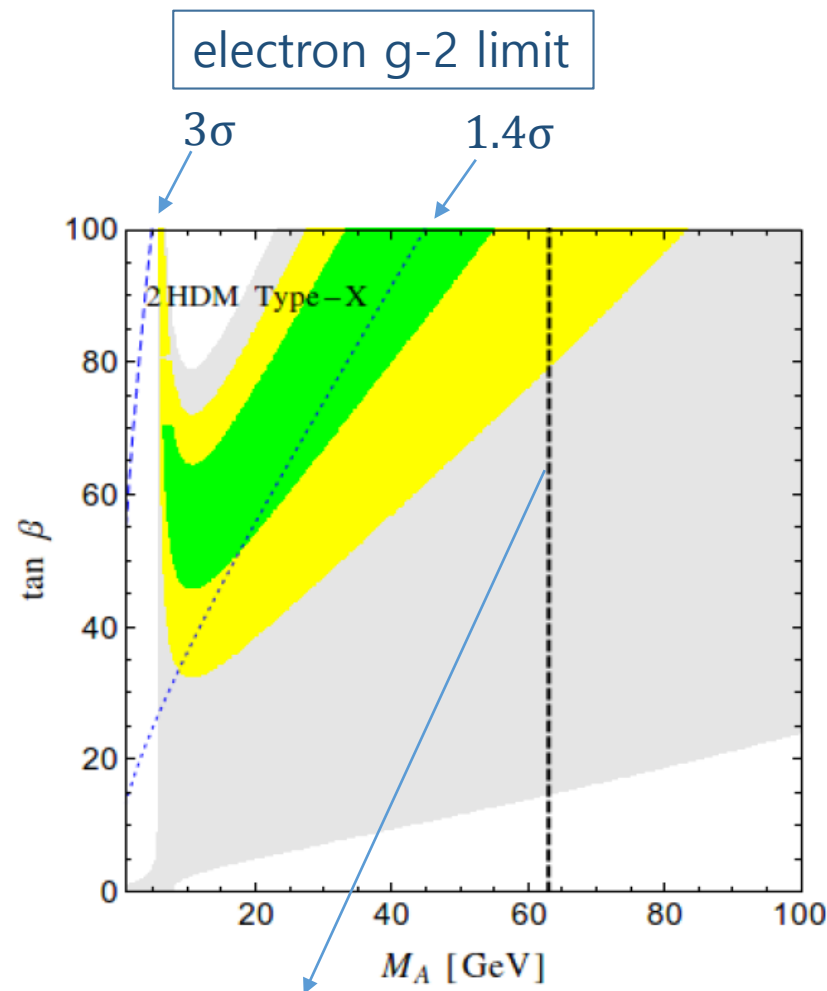


In the SM limit: $\sin(\beta - \alpha) = 1$

Results



$$m_h (m_H) = 126 (200) \text{ GeV}$$



$$\lambda_{hAA} v \approx 2M_H^2 - M_h^2 - 2M_A^2 \gtrsim 0.13 v^2 \text{ (in the SM limit)}$$

Type X in the wrong-sign limit

$$\mathcal{L}_{\text{Yukawa}}^{\text{2HDM}} = -\frac{m_f}{v} \left(\xi_h^f \bar{f} h f + \xi_H^f \bar{f} H f - i \xi_A^f \bar{f} \gamma_5 A f \right) \\ - \left\{ \frac{\sqrt{2} V_{ud}}{v} \bar{u} (m_u \xi_A^u P_L + m_d \xi_A^d P_R) H^+ d + \frac{\sqrt{2} m_l}{v} \xi_A^l \bar{\nu}_L H^+ l_R + \text{H.C.} \right\}$$

$$\xi_h^u = \xi_h^d = \frac{\cos \alpha}{\sin \beta}, \quad \xi_h^l = -\frac{\sin \alpha}{\cos \beta}, \\ \xi_H^u = \xi_H^d = \frac{\sin \alpha}{\sin \beta}, \quad \xi_H^l = \frac{\cos \alpha}{\cos \beta}, \\ \xi_A^u = -\xi_A^d = \cot \beta, \quad \xi_A^l = \tan \beta.$$



$$\xi_h^q = \frac{c_\alpha}{s_\beta} = s_{\beta-\alpha} + \frac{c_{\beta-\alpha}}{t_\beta} \approx 1 \\ \xi_h^l = -\frac{s_\alpha}{c_\beta} = s_{\beta-\alpha} - t_\beta c_{\beta-\alpha} \approx \pm 1$$

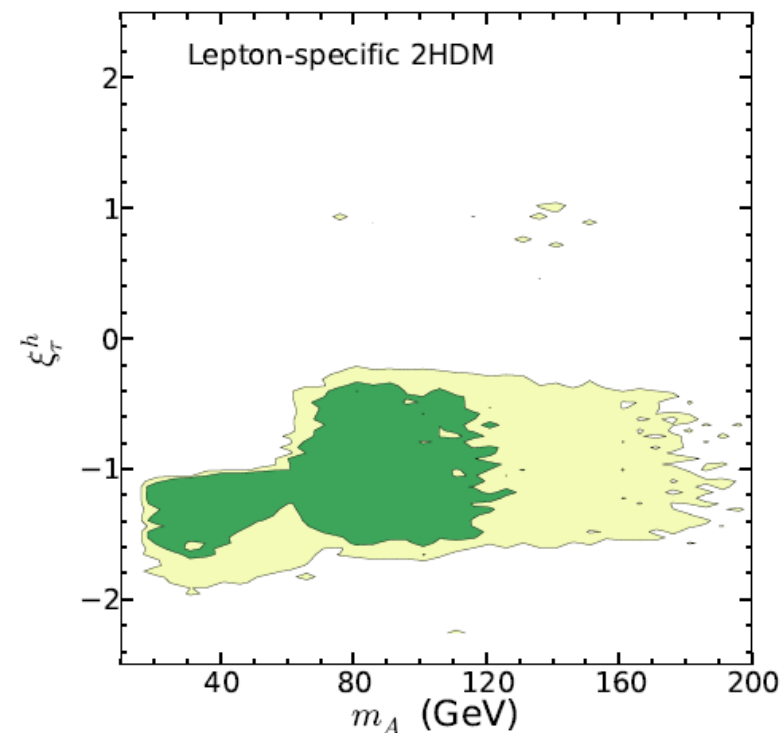
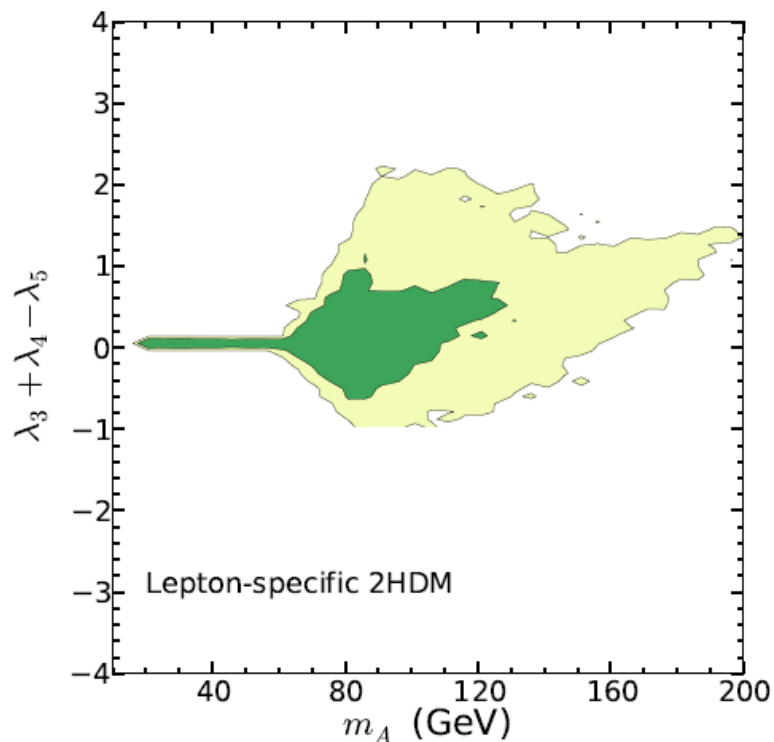
Ferreira, et.al., 1403.4736

Suppressing $h \rightarrow AA(\tau\tau)$ by $\xi_h^\tau \approx -1$

$$\begin{aligned}\lambda_1 &= \frac{m_H^2 c_\alpha^2 + m_h^2 s_\alpha^2 - m_{12}^2 t_\beta}{v^2 c_\beta^2}, \\ \lambda_2 &= \frac{m_H^2 s_\alpha^2 + m_h^2 c_\alpha^2 - m_{12}^2 t_\beta^{-1}}{v^2 s_\beta^2}, \\ \lambda_3 &= \frac{(m_H^2 - m_h^2) c_\alpha s_\alpha + 2m_{H^\pm}^2 s_\beta c_\beta - m_{12}^2}{v^2 s_\beta c_\beta}, \\ \lambda_4 &= \frac{(m_A^2 - 2m_{H^\pm}^2) s_\beta c_\beta + m_{12}^2}{v^2 s_\beta c_\beta}, \\ \lambda_5 &= \frac{m_{12}^2 - m_A^2 s_\beta c_\beta}{v^2 s_\beta c_\beta}.\end{aligned}$$

$$\begin{aligned}\lambda_{hAA} v &\approx (\lambda_3 + \lambda_4 - \lambda_5) v^2 \\ &\approx (1 + \xi_h^\tau) m_H^2 - \xi_h^\tau m_h^2 - 2m_A^2\end{aligned}$$

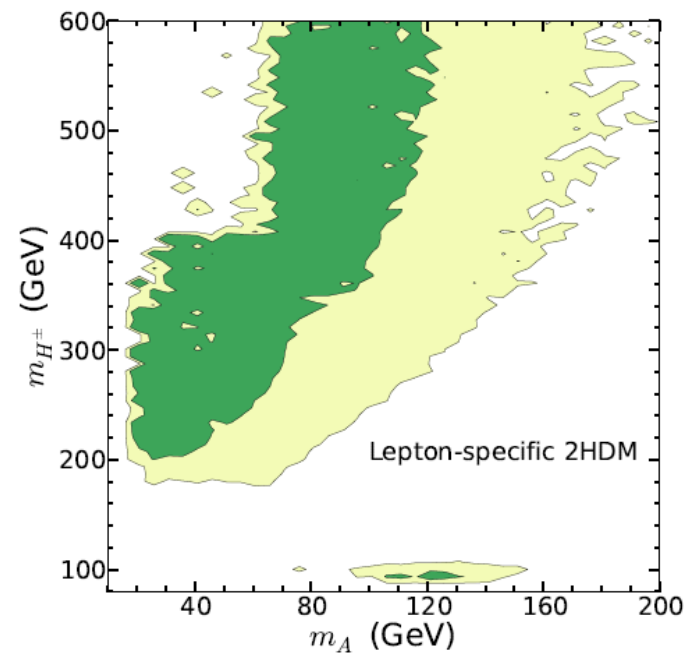
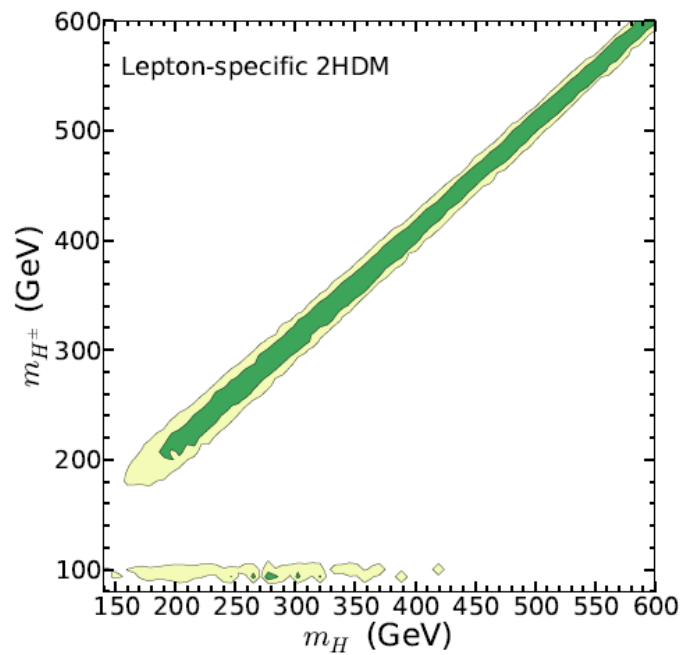
$$\xi_h^\tau \approx -\frac{m_H^2 - 2m_A^2 + \lambda_{hAA} v^2}{m_H^2 - m_h^2}$$



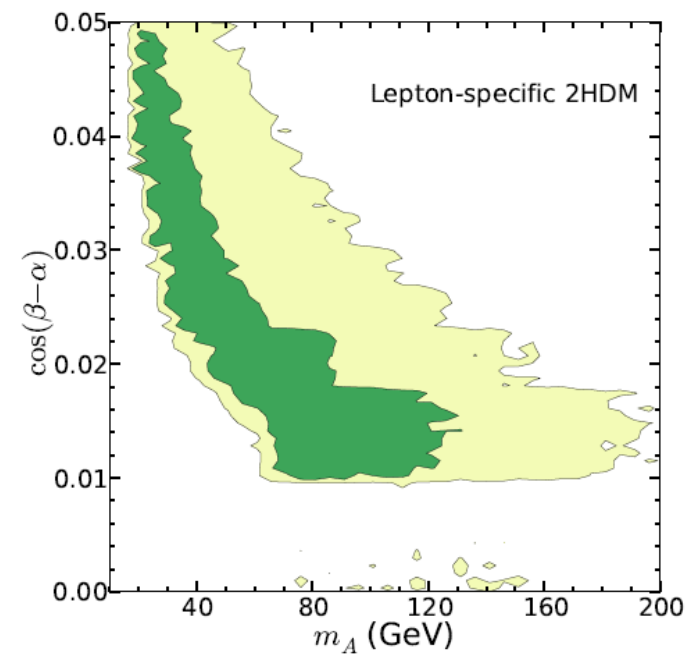
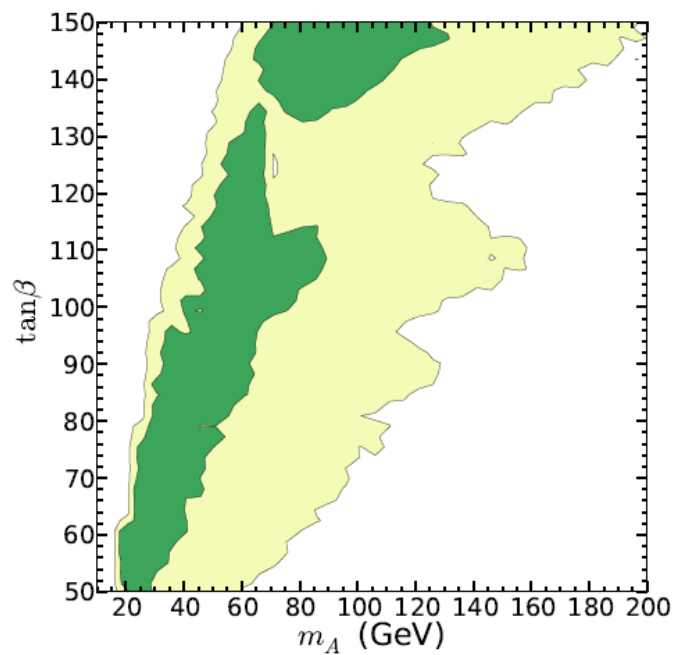
Parameter scan

Measurement	central value μ	Error: (σ , τ)	Distribution
$\delta(g-2)_\mu \times 10^{11}$	262.0	85.0, 0%	Gaussian
BR($h \rightarrow \text{EXO}$)	40%	0.0, 0%	hard-cut
S, T, U	see Ref. [?]	see Ref. [?]	Gaussian
BR($\tau \rightarrow \mu \bar{\nu} \nu$)	17.42%	0.04%, 0.07%	Gaussian
$R(h \rightarrow \tau\tau)_{\text{ATLAS}}$	1.43	0.4, 0.00%	Gaussian
$R(h \rightarrow \tau\tau)_{\text{CMS}}$	0.91	0.28, 0.00%	Gaussian
Higgs bounds	see Ref. [?]	see Ref. [?]	hard cut

2HDM Parameter	Range	Prior distribution
Scenario I: $m_h = 126 \text{ GeV}$		
Scalar Higgs mass (GeV)	$126 < m_H < 600$	Flat
Pseudoscalar Higgs mass (GeV)	$10 < m_A < 400$	Flat
Charged Higgs mass (GeV)	$94 < m_{H^\pm} < 600$	Log
$c_{\beta-\alpha}$	$0.0 < c_{\beta-\alpha} < 0.05$	Flat
t_β	$10 < t_\beta < 150$	Flat
λ_1	$0.0 < \lambda_1 < 4\pi$	Log
Scenario II: $m_H = 126 \text{ GeV}$		
Scalar Higgs mass (GeV)	$40 < m_h < 126$	Flat
Pseudoscalar Higgs mass (GeV)	$10 < m_A < 400$	Flat
Charged Higgs mass (GeV)	$94 < m_{H^\pm} < 600$	Log
$c_{\beta-\alpha}$	$0.0 < s_{\beta-\alpha} < 0.05$	Flat
t_β	$10 < t_\beta < 150$	Flat
λ_1	$0.0 < \lambda_1 < 4\pi$	Log



$$m_H^2 \approx \frac{\xi_h^\tau m_h^2 + 2m_A^2 + \lambda_{hAA} v}{1 + \xi_h^\tau}$$



Conclusion

- Imposing the muon $g-2$ singles out Type X 2HDM in a specific parameter region provable at the LHC2.
- The SM limit is allowed only at 2σ due to large $h \rightarrow AA(\tau\tau)$.
- In the wrong-sign limit, the region of $t_\beta > 50$, $m_A = 20 - 80 \text{ GeV}$, $m_H \sim m_{H^\pm} = 200 - 600 \text{ GeV}$, is viable with a tuned $\frac{\lambda_{hAA}}{v} \ll 1$.
- LHC13 prospect under investigation:
$$pp \rightarrow h, Z, W \rightarrow AA, AH, AH^\pm \rightarrow 4\tau, 3\tau + \nu.$$