

DARK MATTER IN SUSY AXION MODEL

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HIGGS & DM

- Higgs boson is discovered

$m_h = 125 \text{ GeV}$ All SM is discovered

If SM is valid up to M_P or M_{GUT} , what determines weak scale?

$$m \sim m_h \sim v \sim M_W \sim 100 \text{ GeV}$$

How to solve the hierarchy problem? $\delta m_h^2 \sim \frac{\lambda_f^2}{8\pi^2} \Lambda^2 + \dots$

- Dark Matter Existence

Cosmological & astrophysical evidence for DM

$$\Omega h^2 \simeq 0.12 \quad (26.8\% \text{ of energy density of the Universe})$$

cold & non-baryonic \longrightarrow new physics particle(s)?

SUPERSYMMETRY

Symmetry btw fermion and boson

- No quadratic div.

$$\delta m_h^2 \sim \frac{\lambda_f^2}{8\pi^2} m_{\text{soft}}^2 \log \Lambda^2$$

- Weak scale SUSY drives the radiative EWSB

$$m_{\text{soft}} \sim M_W \sim m_h$$

- Lightest SUSY particle can be DM

$$\tilde{Z}_1 = N_{1\tilde{B}} \tilde{B} + N_{1\tilde{W}} \tilde{W} + N_{1\tilde{H}_d} \tilde{H}_d + N_{1\tilde{H}_u} \tilde{H}_u$$

SUPERSYMMETRY

Symmetry btw fermion and

- No quadratic div.

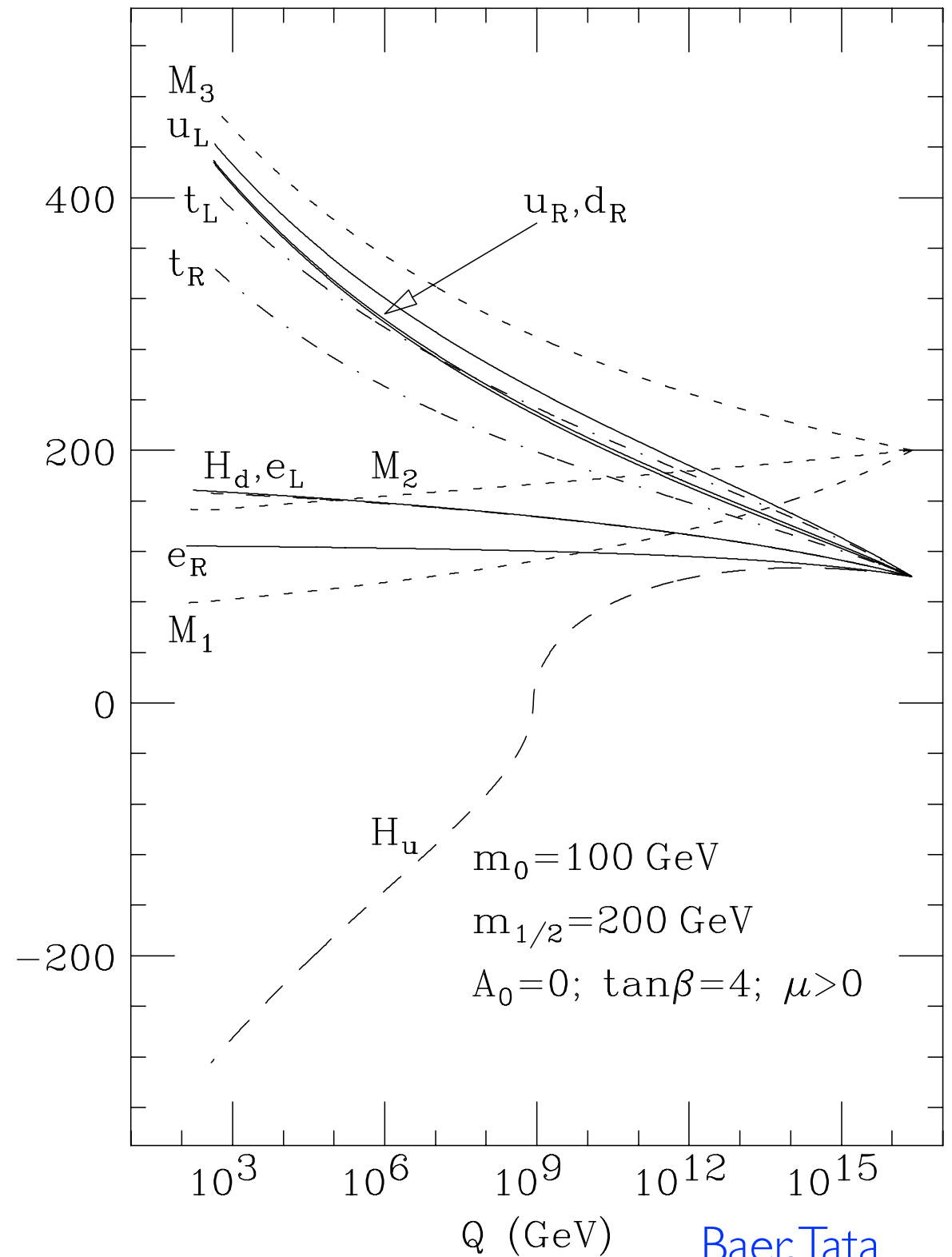
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- Lightest SUSY particle can be

$$\tilde{Z}_1 = N_{1\tilde{B}} \tilde{B} + N_{1\tilde{W}} \tilde{W} + \dots$$



SUPERSYMMETRY

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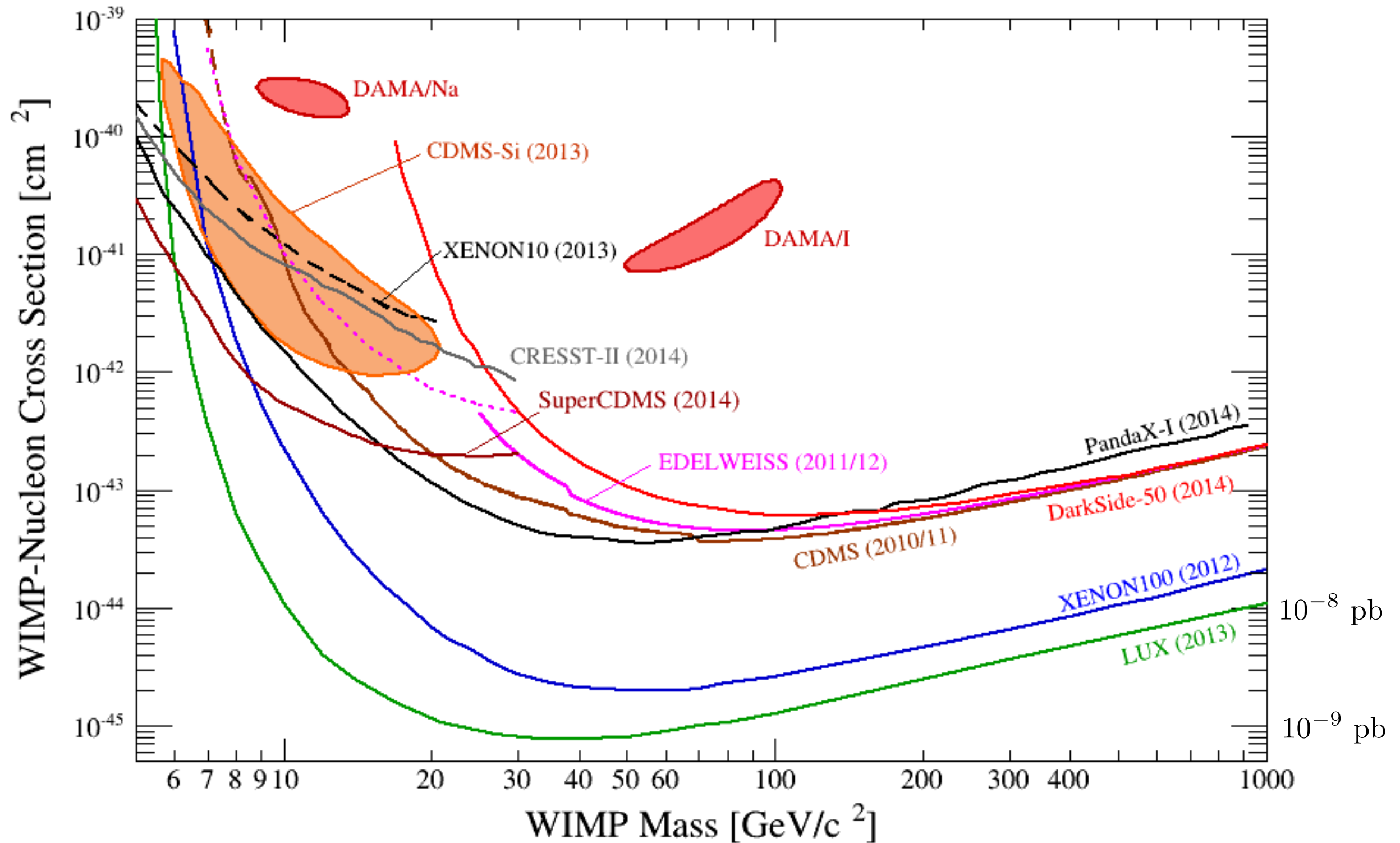
- Lightest SUSY particle can be DM

$$\tilde{Z}_1 = N_{1\tilde{B}} \tilde{B} + N_{1\tilde{W}} \tilde{W} + N_{1\tilde{H}_d} \tilde{H}_d + N_{1\tilde{H}_u} \tilde{H}_u$$

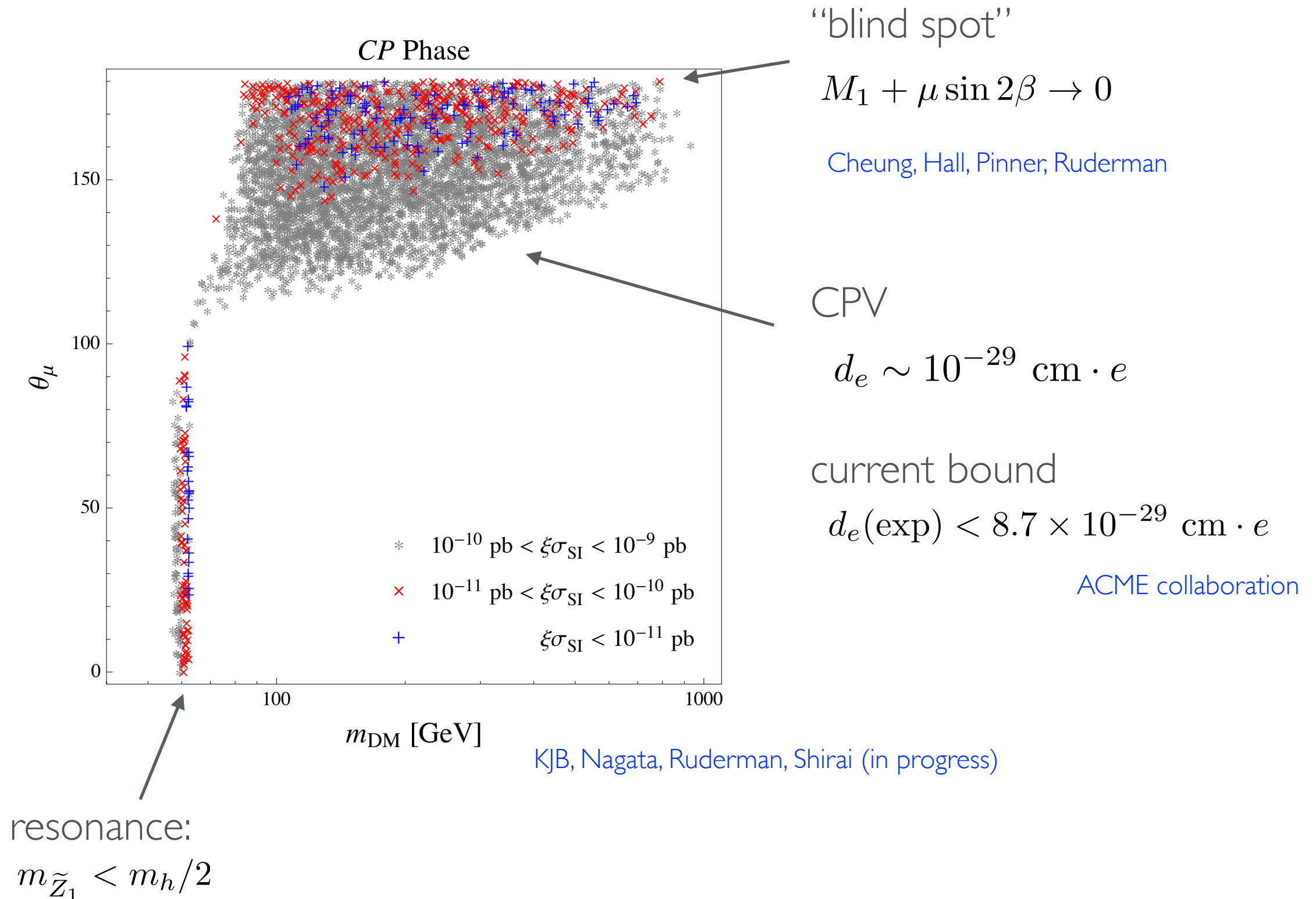
EXPERIMENTAL TEST

Upper limit for σ_{SI} is getting smaller

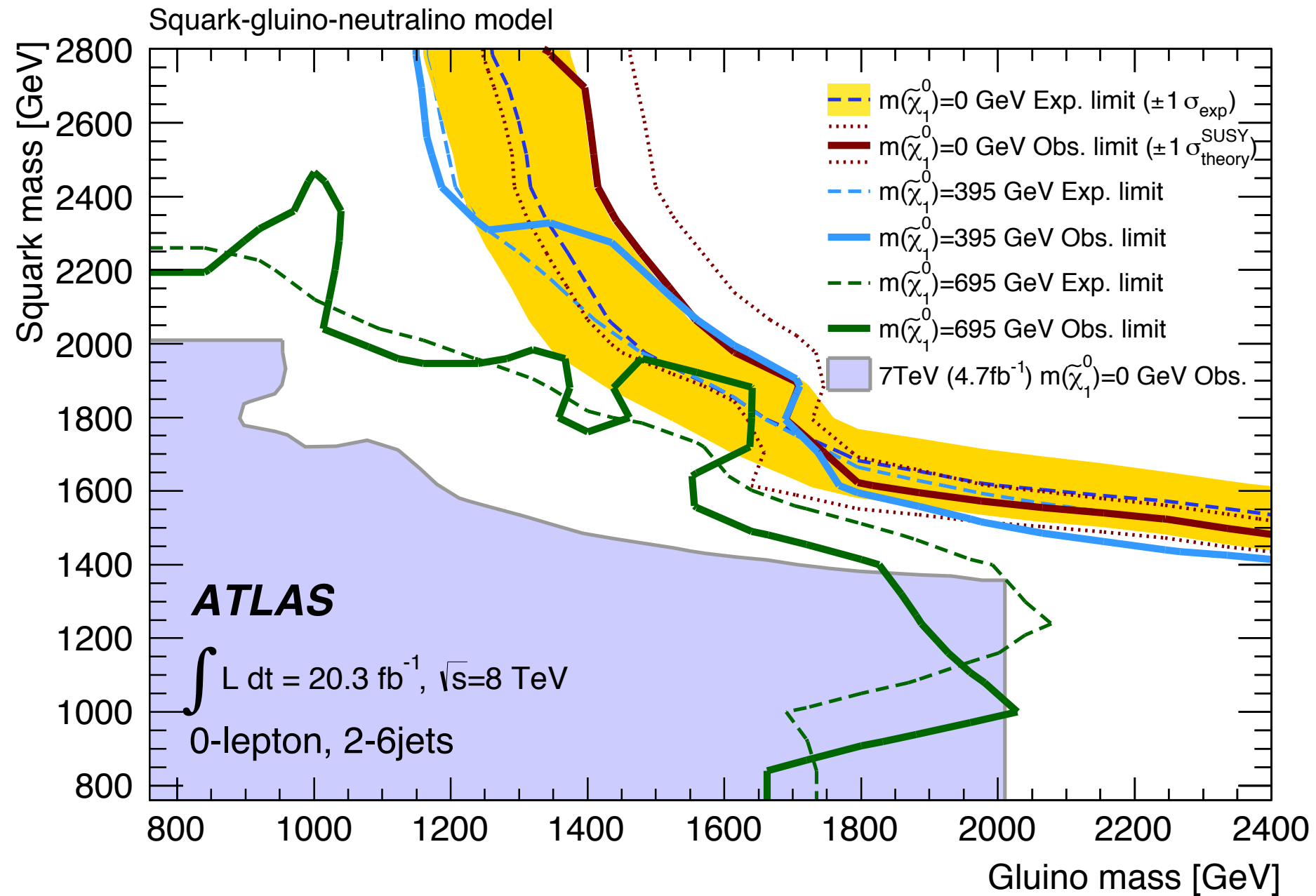
arXiv:1501.01200



Bino-Higgsino neutralino is in the corner



Scale of “weak scale SUSY” is getting higher



$$m_{\tilde{g}} > 1.2 \text{ TeV}$$

$$m_{\tilde{q}} > 1.4 \text{ TeV}$$

TeV scale SUSY ?

Natural EWSB

$$\frac{M_Z^2}{2} \simeq -\mu^2 - m_{H_u}^2$$

Natural EWSB requires $\mu^2 \sim M_Z^2$

—————→ $\mu \sim M_Z \ll m_{\text{soft}} \sim \mathcal{O}(\text{TeV})$

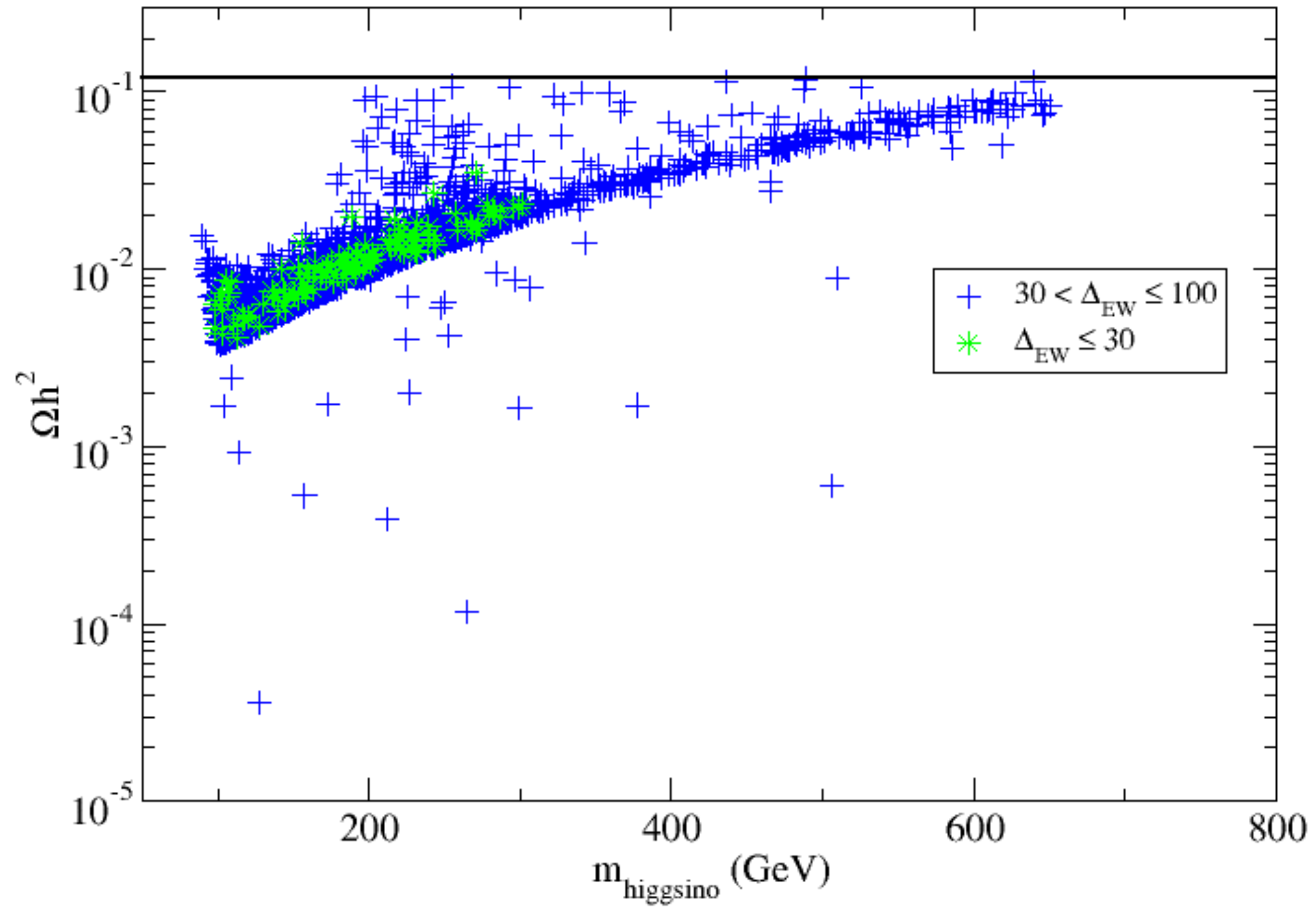
—————→ mostly **higgsino-like** neutralino

Baer, Barger, Huang, Mickelson, Mustafayev, Tata

Higgsino is generally underabundant

$$\Omega h^2 \simeq 0.1 \left(\frac{\mu}{1 \text{ TeV}} \right)^2$$

Underabundant higgsino



Extension for DM

- another DM component(s)?
 - introducing **new symm.** → new (quasi-)stable particle
- non-thermal production for WIMP?
 - long-lived heavy particle → decay into neutralino
- Super WIMP?
 - neutralino is NLSP → decay into LSP (swimp)
 - e.g. gravitino LSP (discussed later)

AXION

- Introducing $U(1)_{PQ}$: broken at $f_a > 10^9$ GeV
- Solution to the strong CP problem

$$\mathcal{L}_{\text{eff}} \supset \frac{g_s^2}{32\pi^2} \left(\frac{a}{f_a} + \bar{\theta} \right) G_{\mu\nu}^a \tilde{G}^{a\mu\nu} \longrightarrow \left\langle \frac{a}{f_a} + \theta \right\rangle = 0$$

- Axion is pseudo-Nambu-Goldstone boson

$$f_a > 10^9 \text{ GeV} \longrightarrow \tau(a \rightarrow 2\gamma) \simeq \frac{10^9 t_U}{C_{a\gamma\gamma}^2} \left(\frac{f_a}{10^9 \text{ GeV}} \right)$$

- SUSY partners: axino/saxion

$$f_a > 10^9 \text{ GeV} \longrightarrow \text{long-lived: } T_{\text{dec}} \sim \text{MeV} - \text{TeV}$$

We will consider SUSY axion model!

OUTLINE

- Introduction
- Supersymmetric Axion Model
- Dark Matter
- Summary & Future Plan

SUSY AXION MODEL

SUSY AXION MODEL

Peccei-Quinn symm. + SUSY

→ MSSM + axion sector (a. k. a. PQMSSM)

supersymmetrizing axion

$$a \quad \longrightarrow \quad A = \frac{1}{\sqrt{2}}(s + ia) + \sqrt{2}\theta\tilde{a} + \theta^2 F_A$$

axion couplings

$$\begin{aligned} \text{KSVZ: } W \supset m_Q e^{A/f_a} Q Q^c &\quad \longrightarrow \quad \mathcal{L} \supset -\frac{\sqrt{2}\alpha_s}{8\pi(f_a/N)} \int d^2\theta A W^a W^a + \text{h.c.} \\ \text{DFSZ: } W \supset \mu e^{-2A/f_a} H_u H_d & \end{aligned}$$

axion mass: $m_a = 6 \text{ meV} (10^9 \text{ GeV}/f_a)$

saxion/axino mass is generated by SUSY breaking

AXINO MASS

Goto, Yamaguchi;
Chun, Kim, Nilles;
Chun, Lukas

- No additional zero mode:

$$W = Z(XY - f_0^2) \quad \text{SUSY VEV: } Z_0 = 0, \quad X_0 Y_0 = f_0^2$$

$XY = f_0^2$: flat direction in SUSY limit \longrightarrow axion mode!

$$X = f_0 e^{A/f_0}, \quad Y = f_0 e^{-A/f_0}$$

$$V_{\text{soft}} = m_Z^2 |Z|^2 + m_X^2 |X|^2 + m_Y^2 |Y|^2 + A_Z ZXY - C_Z Z f_0^2$$

soft term scale $\sim m_{3/2} \longrightarrow m_s \sim m_{3/2}$

$m_{\tilde{a}} \sim \langle Z \rangle \longleftarrow \langle F_X/X \rangle \sim \langle F_Y/Y \rangle \sim \langle Z \rangle$

$\langle X \rangle \sim \langle Y \rangle \sim f_0 \quad \langle Z \rangle \sim m_{3/2} \quad \text{for} \quad A_Z \neq C_Z$

$\langle Z \rangle \sim \mathcal{O}(m_{3/2}^2/f_0) \quad \text{for} \quad A_Z = C_Z$

typical axino (saxion) mass is at gravitino mass scale or smaller

AXINO MASS (CONT.)

- Additional zero mode:

Chun, Lukas;
KJB, Baer, Chun, Shin

$$W = S(\lambda_x XY - \lambda_z Z^2) + \lambda_f (Z - f_0)^3$$

$$\longrightarrow \text{SUSY VEV: } S_0 = 0, \quad Z_0 = f_0, \quad X_0 Y_0 = (\lambda_z / \lambda_x) f_0^2$$

$$XY = (\lambda_z / \lambda_x) f_0^2 \quad \text{axion direction} \quad \frac{2X_0}{f_0} X + Z \quad \text{additional zero mode!}$$

$$V_{\text{soft}} = m_S^2 |S|^2 + m_X^2 |X|^2 + m_Y^2 |Y|^2 + m_Z^2 |Z|^2 \\ + A_x SXY - A_z SZ^2 + A_f Z^3 + B_f Z^2 + C_f Z$$

gravity mediation $m_{\text{soft}} \sim m_{3/2}$

$$m_s \sim m_{\tilde{a}} \sim \sqrt{2} \lambda_x \langle S \rangle \sim \left(\lambda_f m_{3/2}^2 f_0 \right)^{1/3}$$

$m_{\tilde{a}} \sim m_s \gg m_{3/2}$ can be realized!

DARK MATTER

Depending on axino mass

$m_{\tilde{a}} \ll m_{3/2}$ axino/axion DM (not considered here)

$m_{\tilde{a}} \sim m_{3/2} \sim m_{\text{soft}}$ neutralino/axion DM

higgsino-like neutralino:

TP and NTP (from axino/saxion decay)

$m_{3/2} \ll m_{\text{soft}} \ll m_{\tilde{a}}$ gravitino/axion DM

TP and

NTP (from axino/saxion and neutralino decay)

NEUTRALINO/AXION DM

DM in SUSY axion models: $m_{\text{soft}} < m_{\tilde{a},s} < m_{3/2}$

- Axion DM

- quasi-stable $\tau \gg t_U$
- bosonic coherent motion at $T \sim 1 \text{ GeV}$
- determined by θ_i :

$$\Omega h^2 \sim 0.1 \theta_i^2 \left(\frac{f_a}{10^{12} \text{ GeV}} \right)^{1.18}$$

- Neutralino DM

- stable (assuming R -parity)
- thermal freeze-out at $T \sim 5\text{--}10 \text{ GeV}$

- Saxion/Axino components

- thermally produced: scattering and (inverse-)decay (“freeze-in”)
- unstable \rightarrow decay into neutralinos $T_{\text{dec}} \sim \text{MeV} - \text{TeV}$

\longrightarrow *solving the coupled Boltzmann equations!*

BOLTZMANN EQ.

- Neutralino density:

scattering

$$\frac{dn_{\tilde{Z}_1}}{dt} + 3Hn_{\tilde{Z}_1} = \langle \sigma v \rangle (\bar{n}_{\tilde{Z}_1}^2 - n_{\tilde{Z}_1}^2)$$

BOLTZMANN EQ.

- Neutralino density:

scattering

heavy particle decay/inverse decay
into/from neutralino

$$\frac{dn_{\tilde{Z}_1}}{dt} + 3Hn_{\tilde{Z}_1} = \langle \sigma v \rangle (\bar{n}_{\tilde{Z}_1}^2 - n_{\tilde{Z}_1}^2) + \sum_{i,k} \Gamma_{i \rightarrow \tilde{Z}_1 + k} m_i \frac{n_i}{\rho_i} \left(n_i - \bar{n}_i \frac{n_{\tilde{Z}_1}}{\bar{n}_{\tilde{Z}_1}} \frac{n_k}{\bar{n}_k} \right)$$

$i \in \{\tilde{a}, s, \tilde{G}\}$

BOLTZMANN EQ.

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- For decaying particles, we need to know $\Gamma_{i \rightarrow \tilde{Z}_1 + k}, n_i, \rho_i$ $i \in \{\tilde{a}, s, \tilde{G}\}$

$$\frac{dn_i}{dt} + 3Hn_i = \sum_{j \in \text{MSSM}} \langle \sigma v \rangle_{ij} (\bar{n}_i \bar{n}_j - n_i n_j)$$

scattering

$$- \sum_{j,k} \Gamma_{i \rightarrow j+k} m_i \frac{n_i}{\rho_i} \left(n_i - \bar{n}_i \frac{n_j}{\bar{n}_j} \frac{n_k}{\bar{n}_k} \right)$$

$i \in \{\tilde{a}, s, \tilde{G}\}$ decay/inverse decay
into/from light particles

$$+ \sum_{j,k} \Gamma_{j \rightarrow i+k} m_j \frac{n_j}{\rho_j} \left(n_j - \bar{n}_j \frac{n_i}{\bar{n}_i} \frac{n_k}{\bar{n}_k} \right)$$

heavy particle decay/inverse decay
into/from $i \in \{\tilde{a}, s, \tilde{G}\}$

BOLTZMANN EQ.

- Neutralino density:

scattering

heavy particle decay/inverse decay
into/from neutralino

$$\frac{dn_{\tilde{Z}_1}}{dt} + 3Hn_{\tilde{Z}_1} = \langle \sigma v \rangle (\bar{n}_{\tilde{Z}_1}^2 - n_{\tilde{Z}_1}^2) + \sum_{i,k} \Gamma_{i \rightarrow \tilde{Z}_1 + k} m_i \frac{n_i}{\rho_i} \left(n_i - \bar{n}_i \frac{n_{\tilde{Z}_1}}{\bar{n}_{\tilde{Z}_1}} \frac{n_k}{\bar{n}_k} \right)$$

$i \in \{\tilde{a}, s, \tilde{G}\}$

- For decaying particles, we need to know $\Gamma_{i \rightarrow \tilde{Z}_1 + k}, n_i, \rho_i$

$$\frac{dn_i}{dt} + 3Hn_i = \sum_{j \in \text{MSSM}} \langle \sigma v \rangle_{ij} (\bar{n}_i \bar{n}_j - n_i n_j) \quad \text{scattering}$$

$$- \sum_{j,k} \Gamma_{i \rightarrow j+k} m_i \frac{n_i}{\rho_i} \left(n_i - \bar{n}_i \frac{n_j}{\bar{n}_j} \frac{n_k}{\bar{n}_k} \right) \quad i \in \{\tilde{a}, s, \tilde{G}\} \text{ decay/inverse decay into/from light particles}$$

$$+ \sum_{j,k} \Gamma_{j \rightarrow i+k} m_j \frac{n_j}{\rho_j} \left(n_j - \bar{n}_j \frac{n_i}{\bar{n}_i} \frac{n_k}{\bar{n}_k} \right) \quad \text{heavy particle decay/inverse decay into/from } i \in \{\tilde{a}, s, \tilde{G}\}$$

- need to know $\langle \sigma v \rangle_{ij}, \Gamma$ to determine production/decay of axino/saxion

EFFECTIVE INT.

2 types of realization:

$$\int d^2\theta \, m_Q e^{A/f_a} Q Q^c \quad \text{or} \quad \int d^2\theta \, \mu e^{-2A/f_a} H_u H_d$$

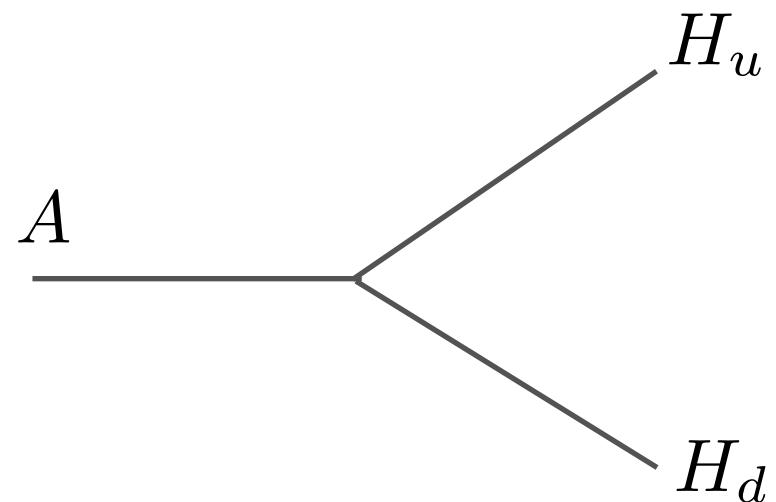
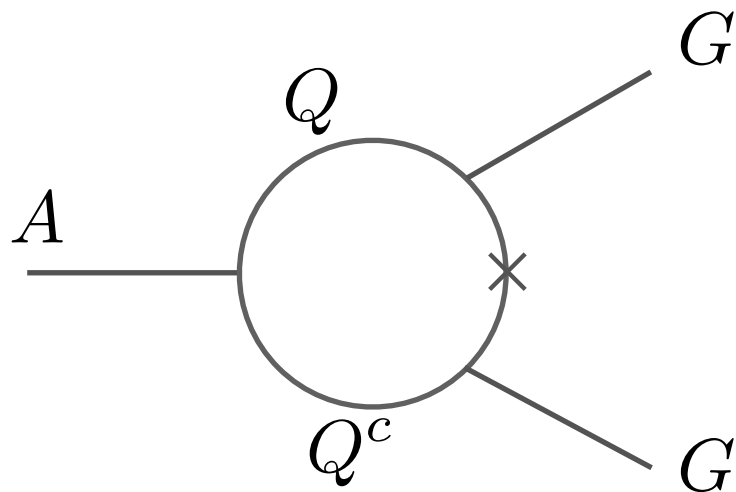


KSVZ-type



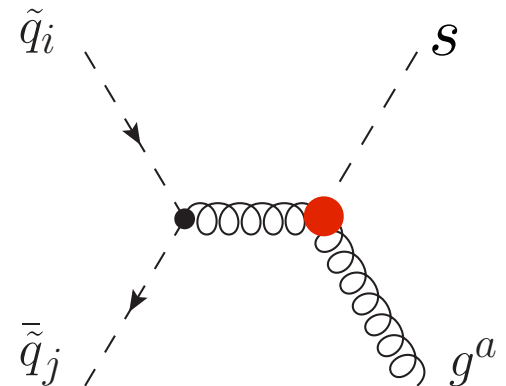
DFSZ-type

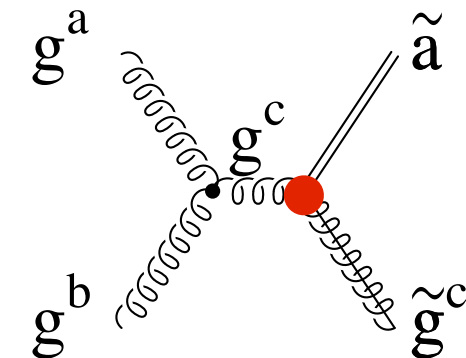
Axion multiplet interacts with MSSM via



KSVZ model

- Effective interaction:

$$\sim \frac{g_s^2}{32\pi^2} \frac{1}{f_a} s \partial_\mu G_\nu^a \partial^\mu G^{a\nu}$$


$$\sim \frac{g_s^2}{32\pi^2} \frac{1}{f_a} \bar{\tilde{a}} \gamma_5 \sigma^{\mu\nu} \partial_\nu G_\mu^a$$


- scattering cross section

saxion: $\langle \sigma v \rangle \sim \frac{9g_s^6}{128\pi^3 f_a^2}$

axino: $\langle \sigma v \rangle \sim \frac{3g_s^6}{64\pi^3 f_a^2}$

$$Y_s^{\text{TP}} \sim Y_{\tilde{a}}^{\text{TP}} \sim 10^{-5} g_s^6 \left(\frac{10^{12} \text{ GeV}}{f_a} \right)^2 \left(\frac{T_R}{10^8 \text{ GeV}} \right)$$

Graf, Steffen; Covi, Kim, Kim,
Roszkowski; Brandenburg, Steffen;
Strumia

- saxion coherent oscillation

$$\frac{\rho_s^{\text{CO}}}{s} \simeq 1.9 \times 10^{-5} \text{ GeV} \left(\frac{\min[T_R, T_s]}{10^8 \text{ GeV}} \right) \left(\frac{f_a}{10^{12} \text{ GeV}} \right)^2 \left(\frac{s_0}{f_a} \right)^2$$

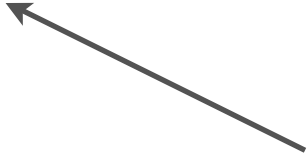
KSVZ model (cont.)

- saxion decay

$s \rightarrow gg, \gamma\gamma \Rightarrow$ produce entropy \Rightarrow dilutes axion/neutralino
 \Rightarrow larger PQ scale can be possible

$s \rightarrow aa \Rightarrow$ produce rel. axion \Rightarrow contributes to N_{eff}

$s \rightarrow \tilde{a}\tilde{a}, \tilde{g}\tilde{g} \Rightarrow$ feeds neutralino DM


$$\frac{\xi}{f_a} s (\partial_\mu a \partial^\mu a + i \bar{\tilde{a}} \gamma^\mu \partial_\mu \tilde{a})$$

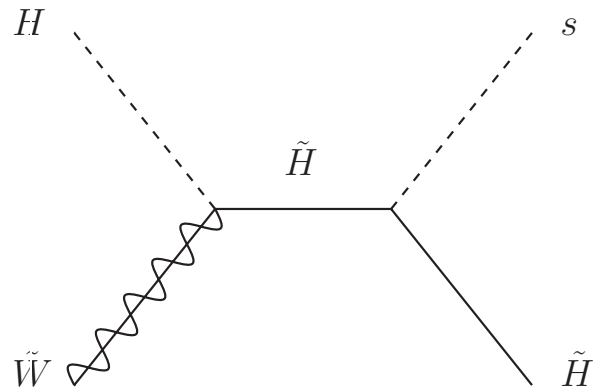
- axino decay

$\tilde{a} \rightarrow g\tilde{g}, \gamma\tilde{Z} \Rightarrow$ feeds neutralino DM and/or entropy

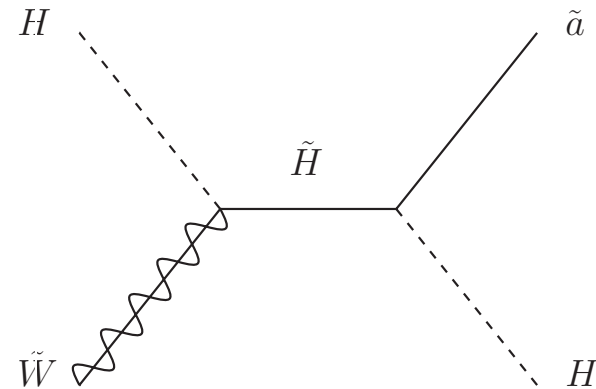
DFSZ model

- Effective interaction:

$$\sim \frac{\mu}{f_a} s \tilde{H}_u \tilde{H}_d$$



$$\sim \frac{\mu}{f_a} \tilde{a} \tilde{H}_u H_d$$



- scattering cross section

$$\langle \sigma v \rangle \sim \left(\frac{\mu}{f_a} \right)^2 \left(\frac{M_{\text{th}}^2}{T^4} \right) K_2(M_{\text{th}}/T)$$

KJB, Choi, Im; KJB,
Chun, Im

$$Y_s^{\text{TP}} \sim Y_{\tilde{a}}^{\text{TP}} \sim 10^{-5} \left(\frac{\mu}{\text{TeV}} \right)^2 \left(\frac{10^{11} \text{ GeV}}{f_a} \right)^2 \left(\frac{\text{TeV}}{M_{\text{th}}} \right)$$

No T_R dependence!

- saxion coherent oscillation also exists

DFSZ model (cont.)

- Decay

Interactions via Higgs sector:

AHH trilinear int.

tree-level decay

mixing with higgs & higgsino

decay into all SM & partners

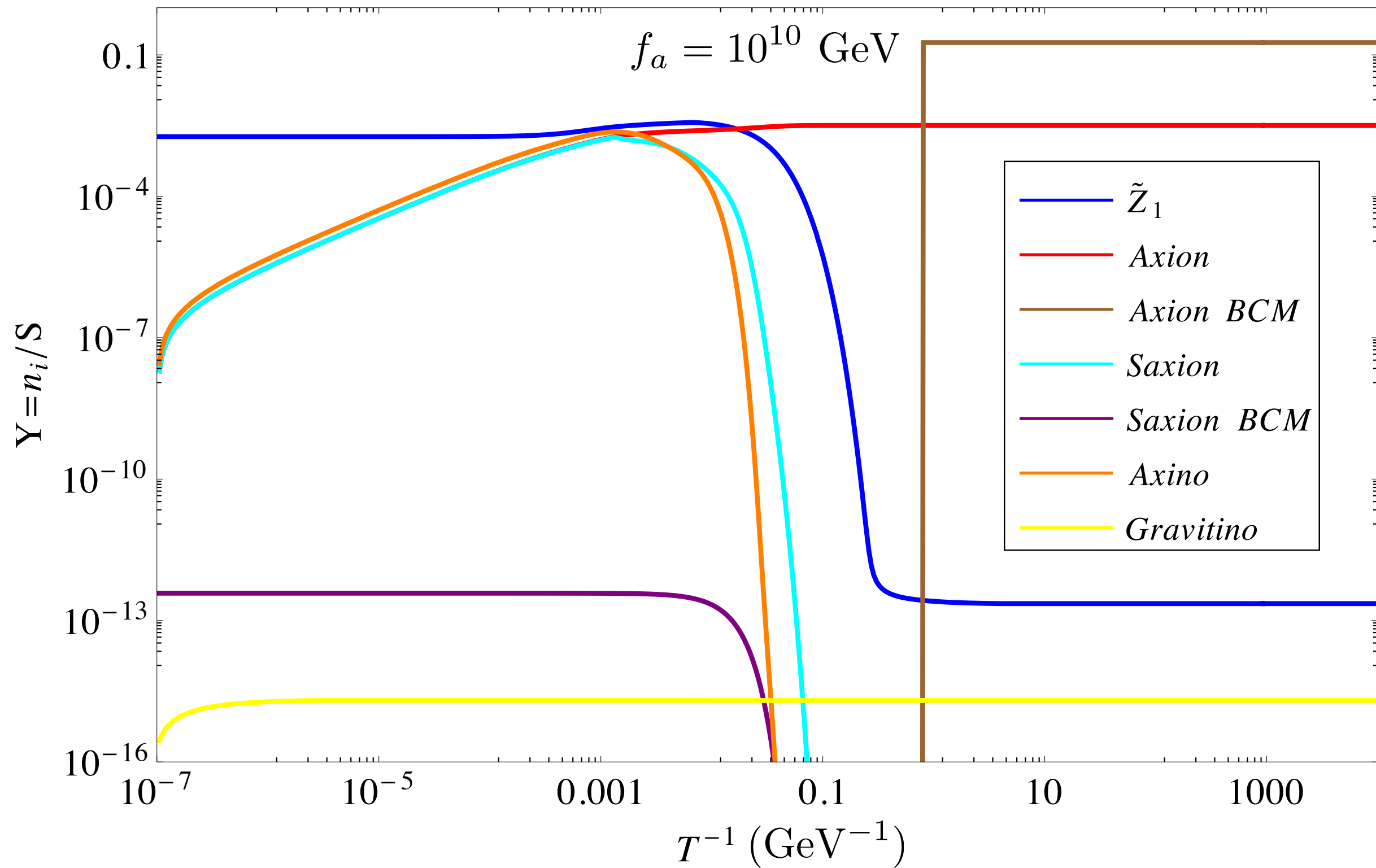
- Larger decay width and shorter life-time

Inverse decay is sizable production channel

Neutralino density tends to be smaller than in KSVZ

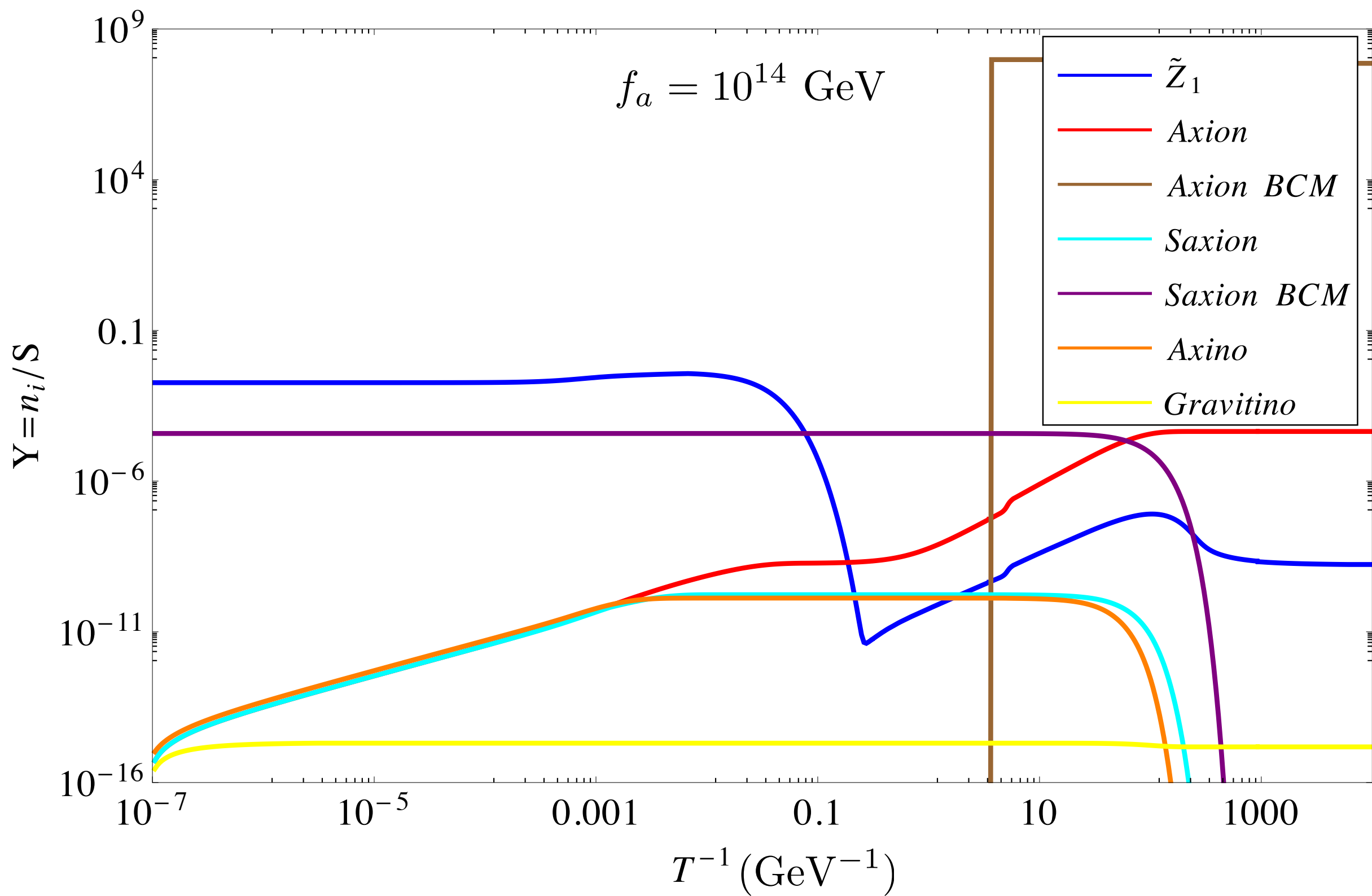
$$Y \sim \frac{(90/\pi^2 g_*)^{1/2}}{4\langle\sigma v\rangle T_{\text{dec}}}$$

Axino/Saxion decay before freeze-out

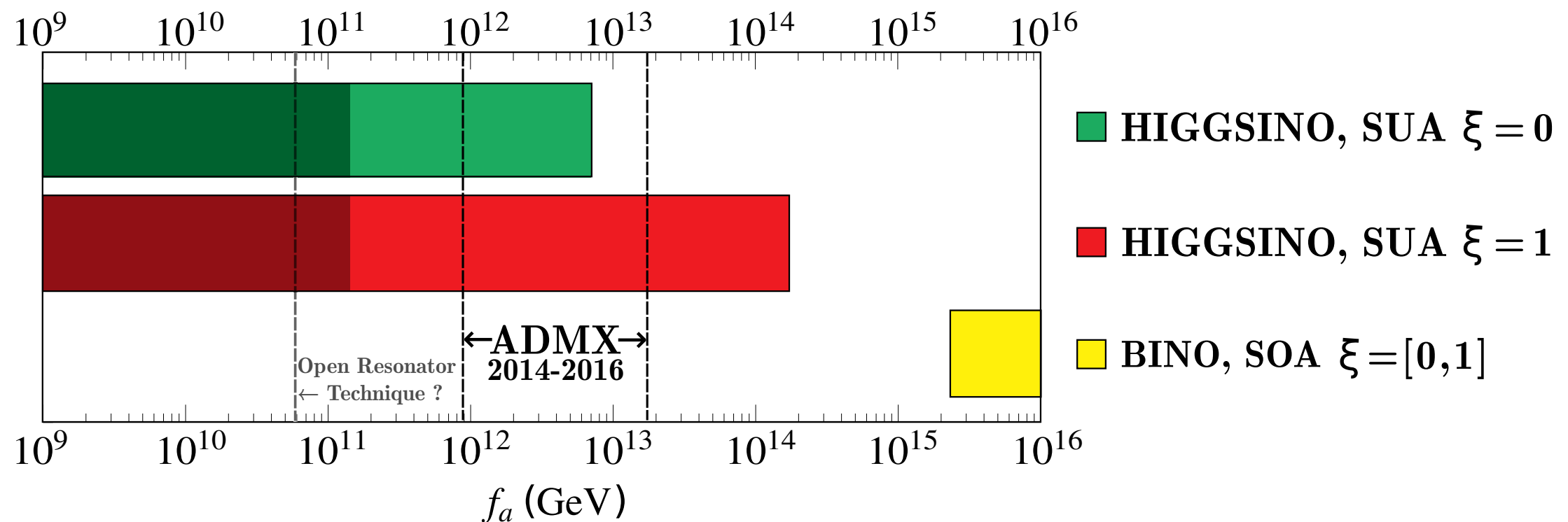
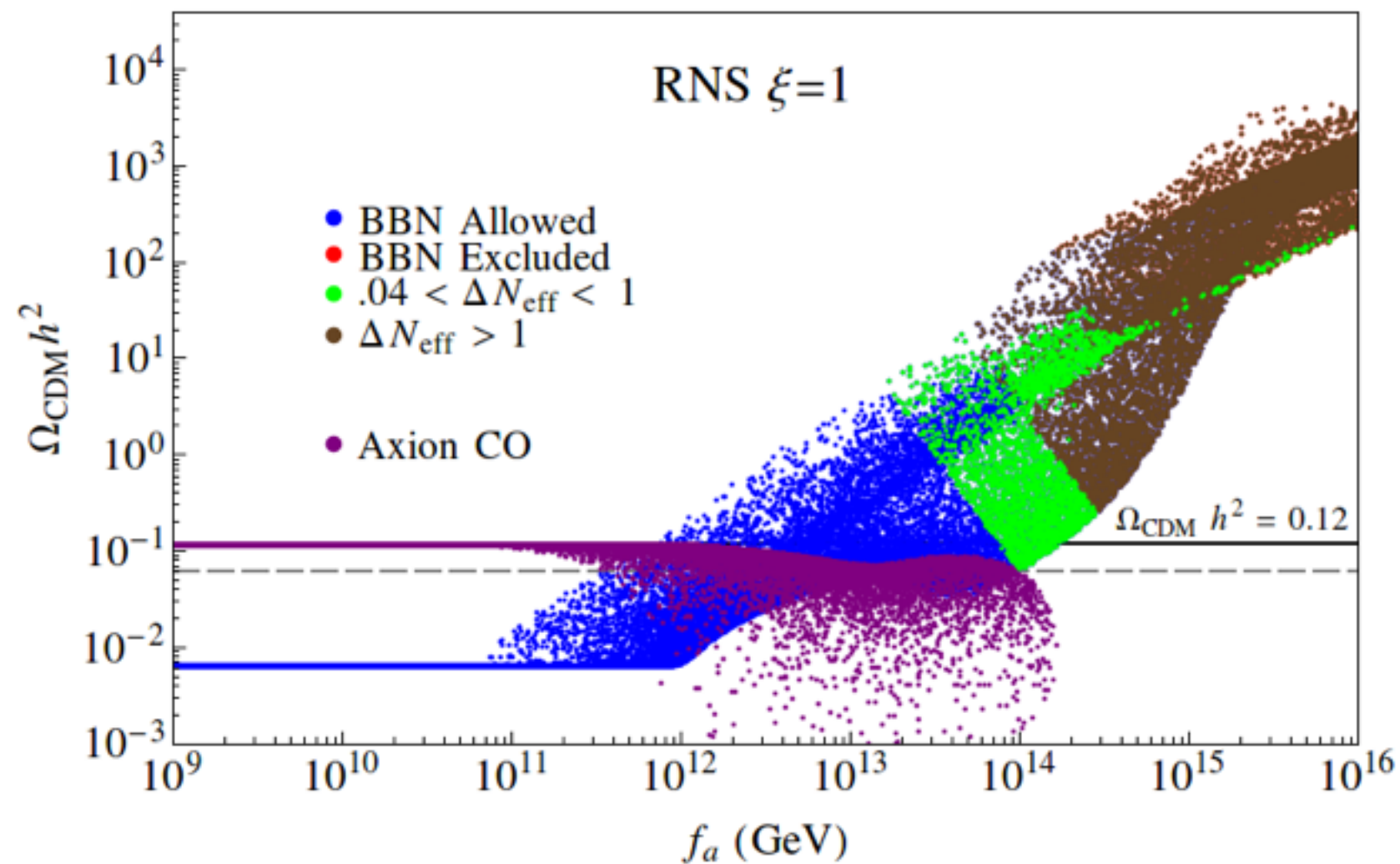


Axino/Saxion decay after freeze-out

$f_a = 10^{14} \text{ GeV}$



Result: DFSZ



GRAVITINO/AXION DM

Gravitino Dark Matter

- In models with $m_{3/2} \ll m_{\text{soft}} \ll m_{\tilde{a},s}$
- Gravitino DM
 - thermally produced: scattering and decay (“freeze-in”)

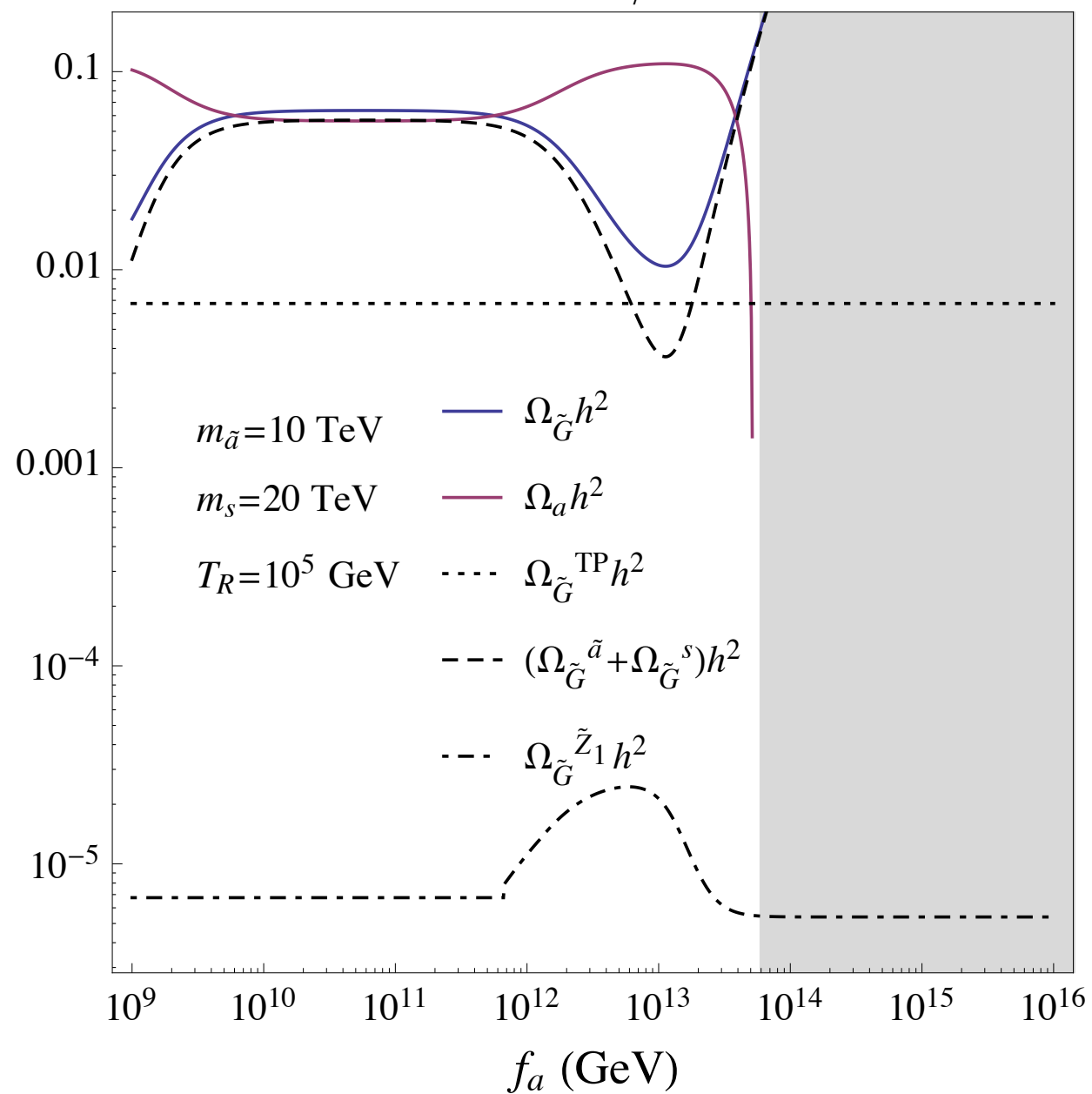
$$\Omega_{\tilde{G}}^{\text{TP}} h^2 = 0.21 \left(\frac{m_{\tilde{g}}}{1 \text{ TeV}} \right)^2 \left(\frac{1 \text{ GeV}}{m_{3/2}} \right) \left(\frac{T_R}{10^8 \text{ GeV}} \right)$$

Bolz, Brandenburg,
Buchmuller; Rychkov,
Strumia

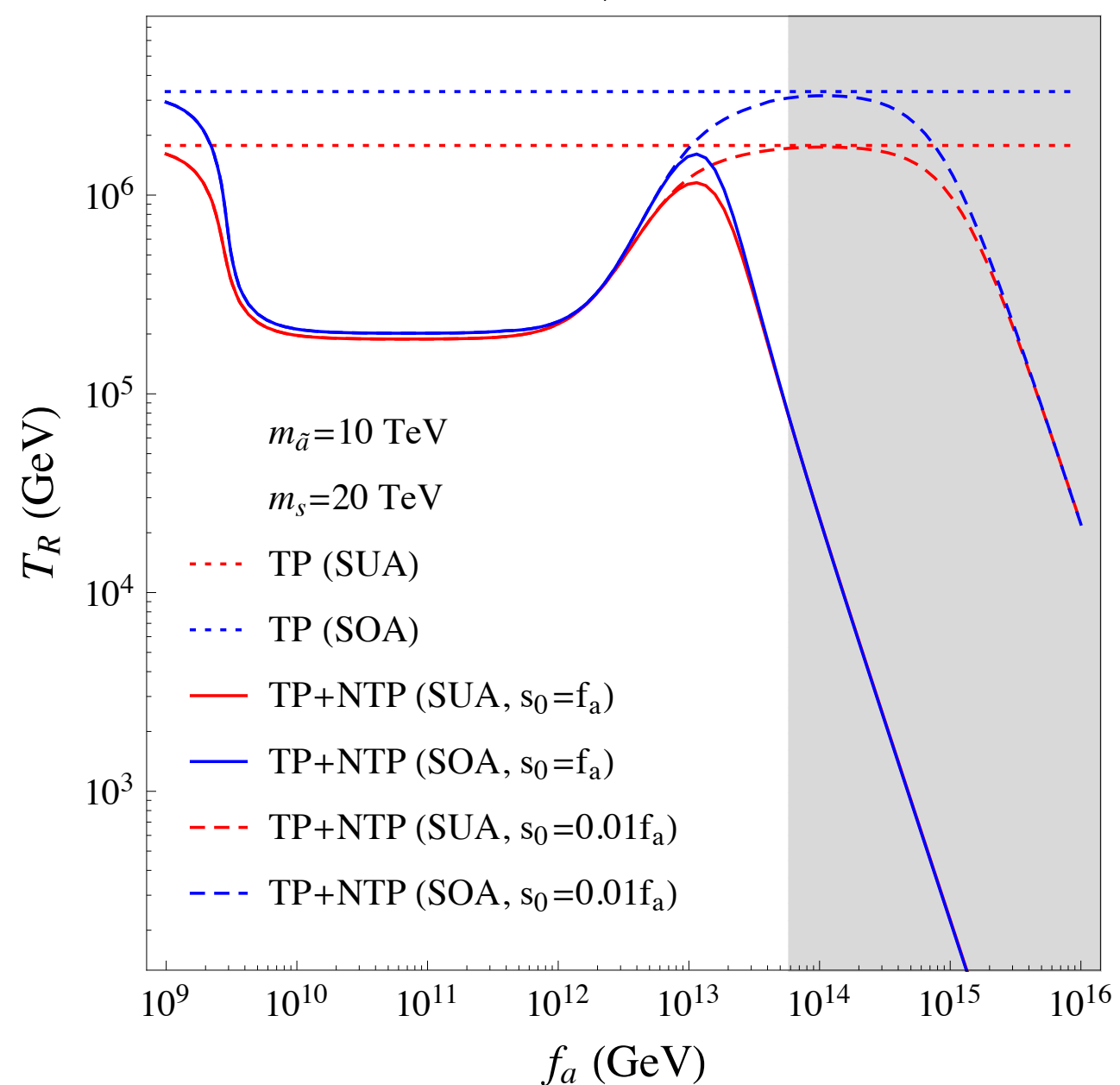
- one more step for decay chain
 - $\left\{ \begin{array}{l} \text{axino/saxion} \rightarrow \text{neutralino} \rightarrow \text{re-annihil.} \rightarrow \text{gravitino} \\ \text{axino/saxion} \rightarrow \text{gravitino} \end{array} \right.$

Result

KSVZ, SUA, $m_{3/2}=100$ MeV



KSVZ, $m_{3/2}=100$ MeV



SUMMARY

- SUSY axion model provide 2 DM as well as thermal and non-thermal production of DM.
- Depending on UV model for PQ breaking, mixed neutralino/axion or gravitino/axion DM is considered.
- To obtain precise DM density, extended Boltzmann eqs. are considered. As their ingredients, $\langle\sigma v\rangle$, Γ are calculated.
- $10^{11} \text{ GeV} \lesssim f_a \lesssim 10^{14} \text{ GeV}$ is favored in mixed neutralino/axion DM scenario. (similar region can be covered by future axion searches.)
- Mixed gravitino/axion DM depends on T_R , upper limit is obtained.

FUTURE PLAN

AXION & SUSY

Axion and SUSY

PQ & SUSY: solutions to fine-tuning problems

scale of theory: f_a, m_{soft} \longrightarrow symmetry breaking!

f_a determines axion interaction

m_{soft} scale of SUSY particles

DM in SUSY axion

DM density is determined by *both* f_a, m_{soft}

\longrightarrow *interplay* btw PQ & SUSY breaking is the key on DM physics

\longrightarrow implies model building & collider signal

test of the model from observations & experiments!

DARK MATTER

Precision for Axino/Saxion

f_a will be determined by ADMX & CAPP

determines axion DM (mass, density, interaction, ...)

→ determines axino/saxion properties (up to masses)

To examine SUSY model we need to calculate precise density of SUSY DM $(\Omega_a + \Omega_{\text{SUSY}})h^2 = 0.12$

→ requires precise calculations for general MSSM

- currently $\langle\sigma v\rangle$ is obtained in SUSY limit or simplified spectrum
 - Γ 's contain only 2-body decays
 - need to develop an automatized tool (including thermal effects)
- important for axino DM scenario

DARK MATTER (CONT.)

Improving Boltzmann eqs.

- We assumed Maxwellian dist. \longrightarrow eqs. for number density n_i
- easy to obtain DM density & portion (ordinary diff. eqs.)
- hard to extract DM velocity dist.

How cold is DM?

- improving eqs. to address *phase space density* $f(E, t)$
 - \longrightarrow warm dark matter from heavy particle decay
- important for non-thermal DM from decay
 - e.g. $\tilde{a} \rightarrow \tilde{G}$ mixed (warm+cold) DM scenario?
- can be examined by structure formation

MODEL BUILDING

Exploring the relation btw ~~PQ~~ & ~~SUSY~~

- *PQ breaking can be triggered by SUSY breaking*
- *mu term is generated in DFSZ*

Murayama, Suzuki, Yanagida;
Choi, Chun, Kim; Martin; KJB,
Baer, Serce

SUSY breaking can be mediated by axion sector

- PQ charged field $PQ(X) \neq 0$

$$\begin{aligned} \langle F_X / X \rangle &\sim m_{\tilde{a}} \gg m_{3/2} \\ \langle X \rangle &\sim f_a \end{aligned} \longrightarrow \text{“axion mediation”}$$

- ~~PQ~~ & axino mass correlates with SUSY spectrum
 - distinctive signals
 - may observe nature of DM in collider

COLLIDER STUDY

Direct SUSY search

- SUSY particle production at Collider
- identifying new particle (mass, spin, ...)
- involving DM physics (missing E_T , ...)

Indirect SUSY search

- measurement of couplings (Higgs, gauge, Yukawa, ...)
- new physics contribution via loop & mixing

e.g. loop-induced higgs decay $h \rightarrow \gamma\gamma$

triple gauge couplings $\gamma W^+ W^-, ZW^+ W^-$