

# Cosmological Constraints from the Anisotropic Clustering Analysis using BOSS DR9

(w/ E. V. Linder, T. Okumura, C. G. Sabiu, Y. -S. Song)

UST- KASI

Astronomy and Space Science

MinJi Oh

# Contents

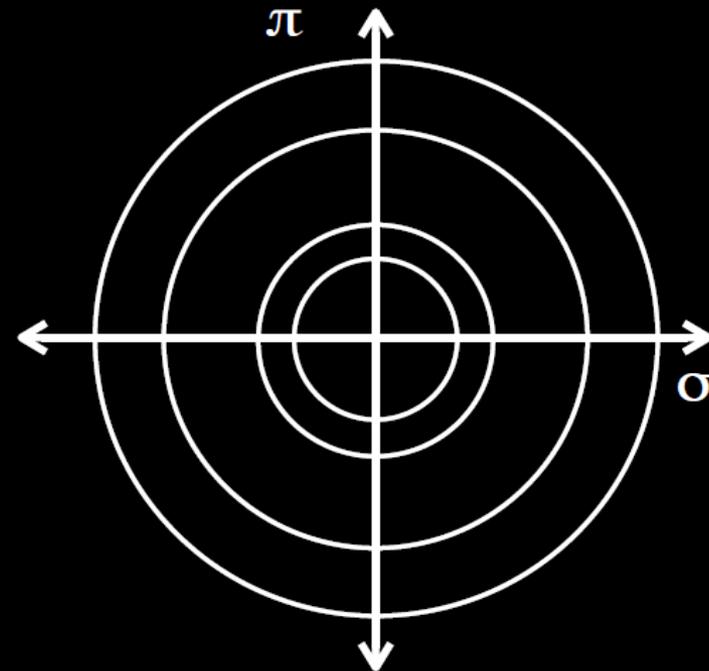
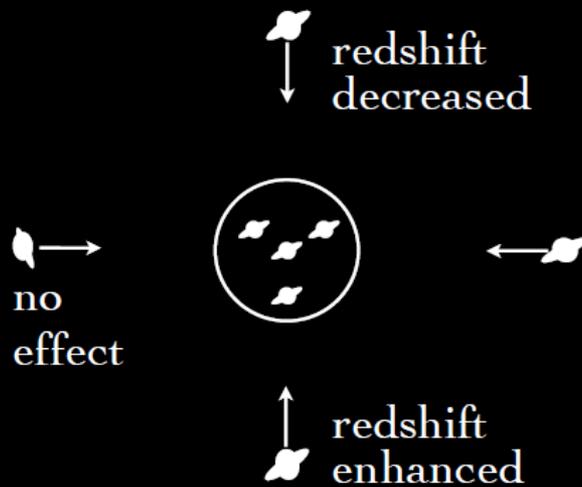
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Cosmological Constraints from the Anisotropic Clustering Analysis  
using BOSS DR9

# 1. INTRODUCTION

# 1. Introduction

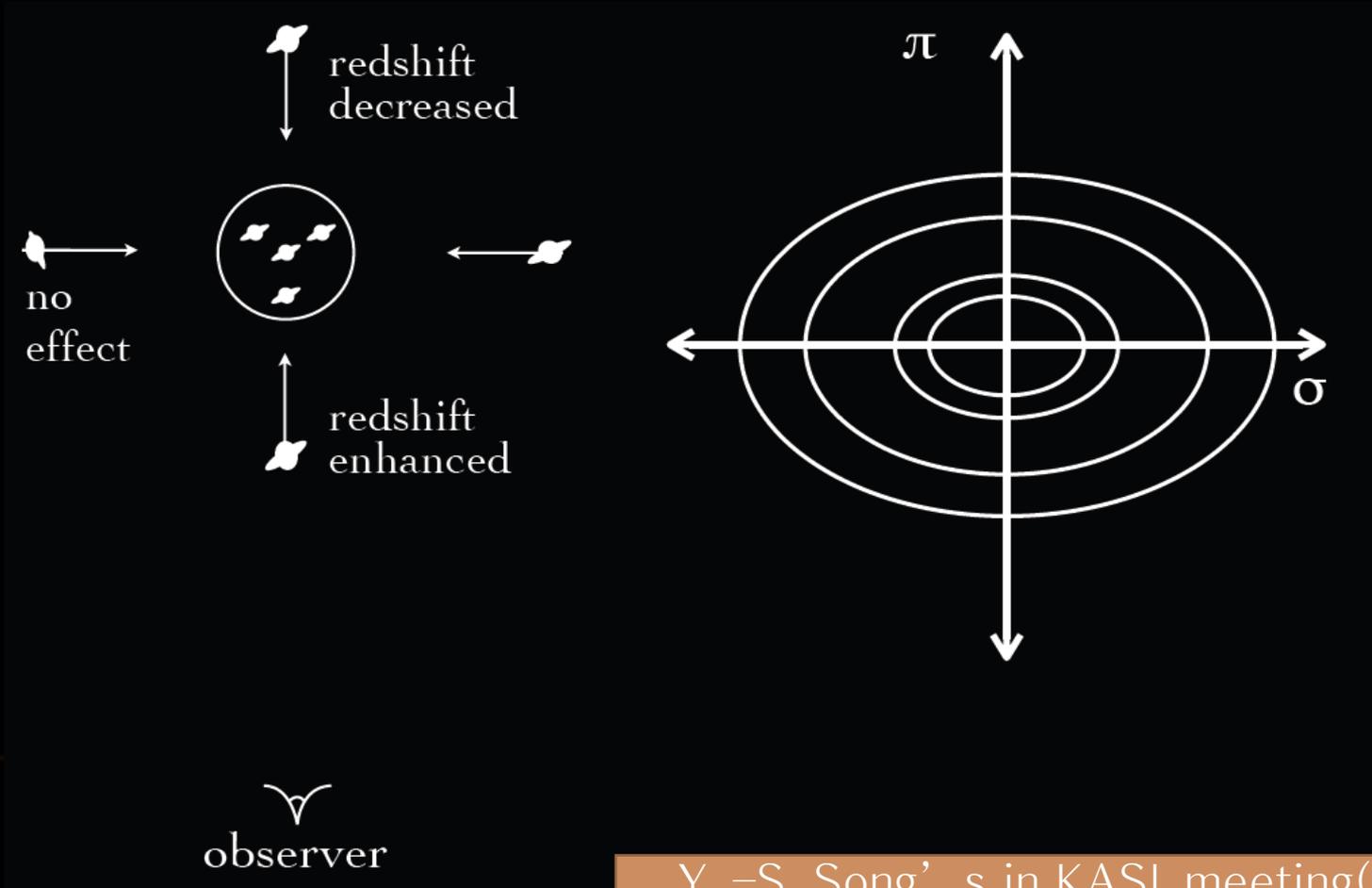
- Redshift-space distortion



  
observer

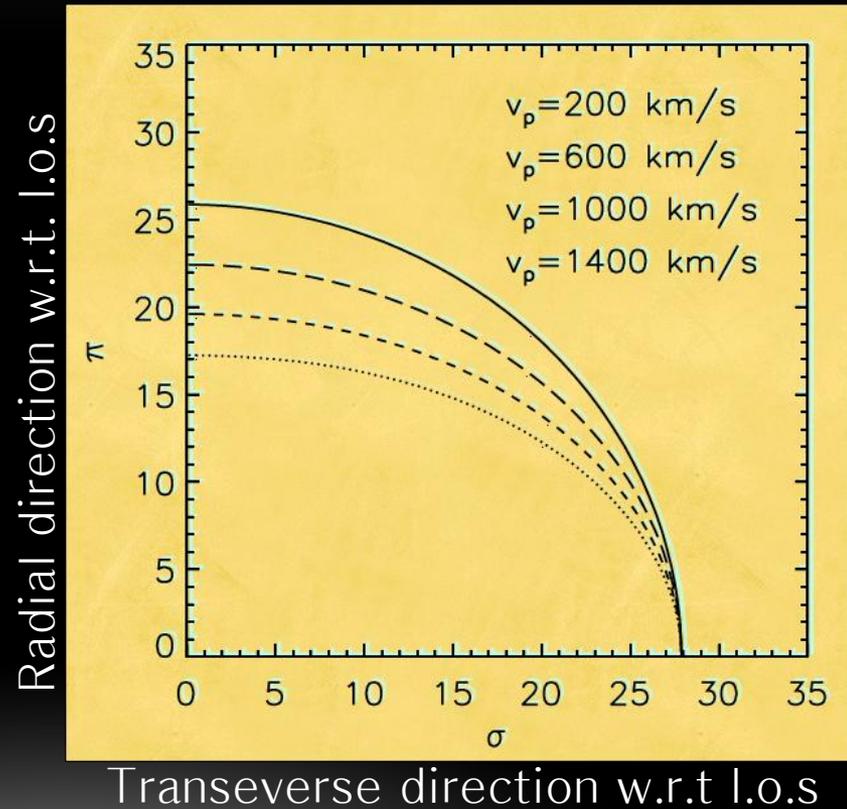
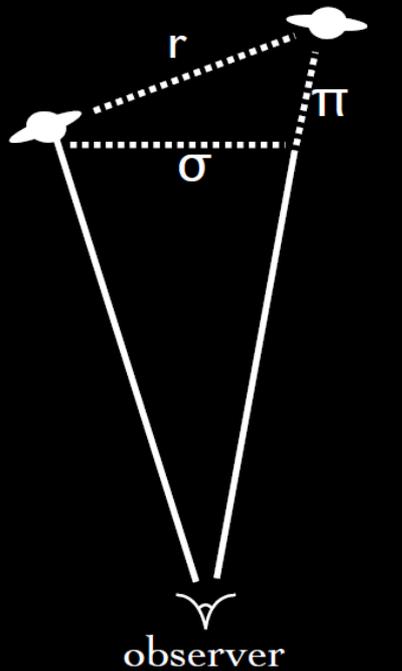
# 1. Introduction

- Redshift-space distortion



# 1. Introduction

- Redshift-space distortion



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## 2. THEORETICAL MODEL

## 2. Theoretical Model

- Redshift-space distortion(RSD)

:An anisotropic features in the clustering pattern of galaxies in redshift space

- Main features in the resultant two-point correlation function,  $\xi_s$ 
  - At linear regimes,
    - Kaiser effect- squeezed clustering pattern along l.o.s
    - enhance the amplitude of the observed correlation ftn
  - At non-linear regimes,
    - Finger of God effect- elongate clustering along l.o.s
    - caused by the random virial motions of galaxies residing at halos
  - cf. BAO peak

## 2. Theoretical Model

- Redshift-space power spectrum

$$\tilde{P}(k, \mu) = \sum_{n=0}^4 Q_{2n}(k) \mu^{2n} G^{FoG}(k\mu\sigma_p)$$

Taruva, Nishimichi, and Saito (2010)

$$cf. P_{Kaiser}(k, \mu) = \begin{cases} (1 + f\mu^2)^2 P_{\delta\delta}(k) & ; \text{linear} \\ P_{\delta\delta}(k) + 2f\mu^2 P_{\delta\theta}(k) + f^2 \mu^4 P_{\theta\theta}(k) & ; \text{non-linear} \end{cases}$$

N. Kaiser (1987)

- Redshift-space correlation function

$$\xi^s(\sigma, \pi) = \int \frac{d^3k}{(2\pi)^3} \tilde{P}(k, \mu) e^{i\vec{k}\cdot\vec{s}}$$

$$= \sum_{\text{even } l} \xi_l(s) P_l(v) \quad \text{where } P_l \text{ is the Legendre polynomials}$$

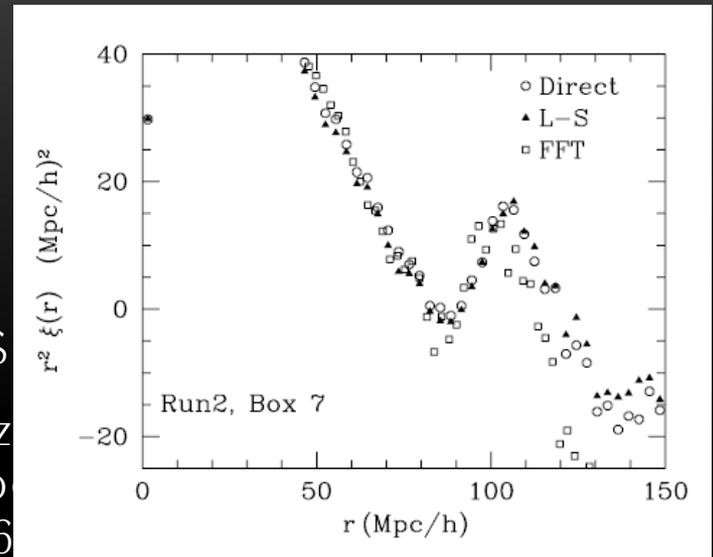
$$v = \pi / s, \quad s = (\sigma^2 + \pi^2)^{1/2}$$

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## 3. MEASUREMENTS

### 3. Measurements

- Data sample: BOSS galaxy samples, CMAS
- Coordinate transformation from (RA, dec, z) to two fiducial spatially-flat cosmological models (Planck (w<sub>c</sub>=0.1138, H<sub>0</sub>=70) and Planck (w<sub>b</sub>=0.02206))
- Landy-Szalay estimator(2D):



Huff, E. et al. (2007)

$$\xi(\sigma, \pi) = \frac{DD(\sigma, \pi) - 2DR(\sigma, \pi) + RR(\sigma, \pi)}{RR(\sigma, \pi)} \approx \frac{DD(\sigma, \pi)}{RR(\sigma, \pi)} - 1$$

↑  
correlation function

↑  
if the random map is perfectly random

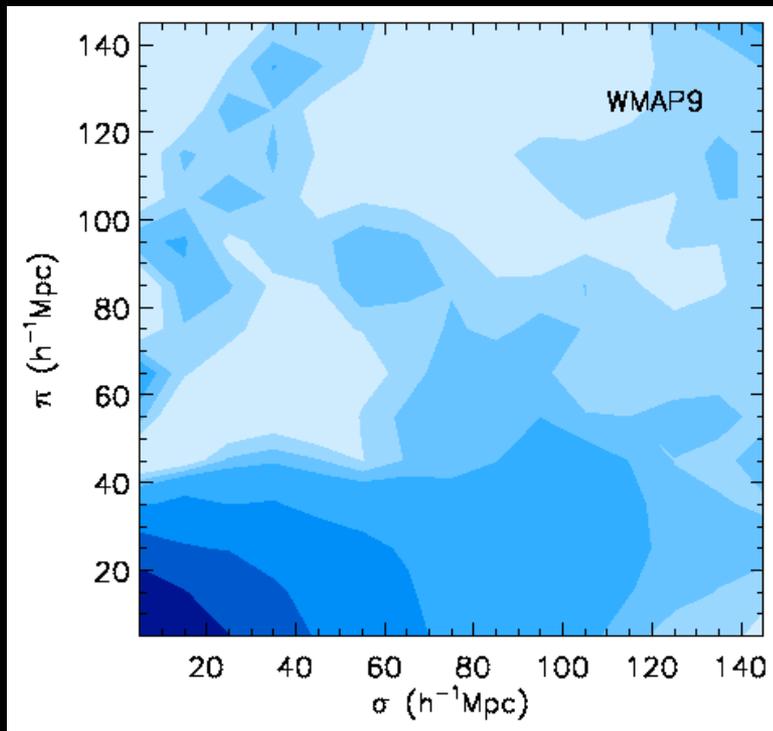
Landy, S. D. & Szalay, A. S. (1993)

where DD(σ, π): the number of pairs in Data with separation σ±Δσ and π±Δπ

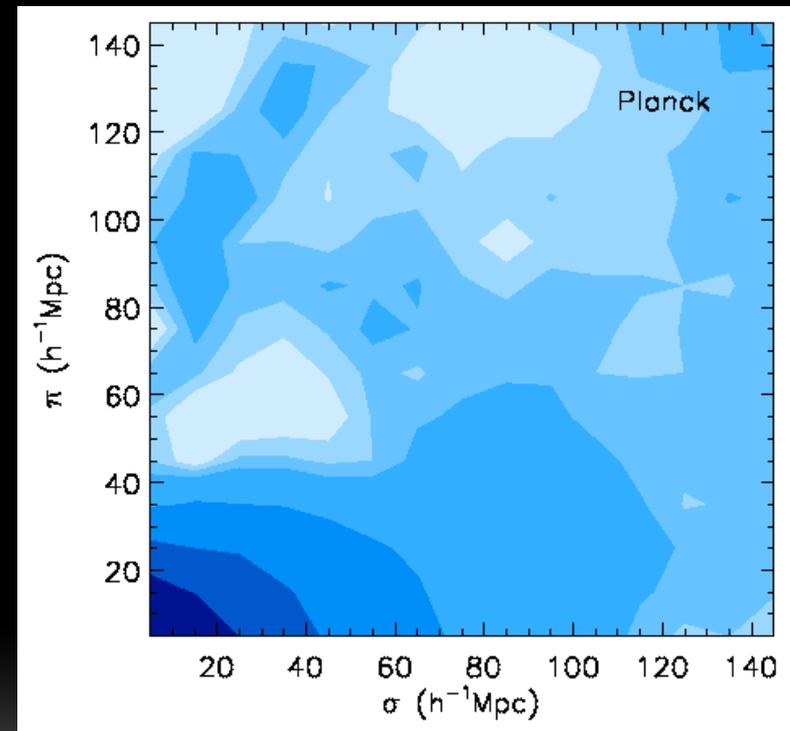
### 3. Measurements

## :Measuring the correlation function

With WMAP9 early universe prior



With Planck early universe prior



- Kaiser effect at small sigma
  - 2D BAO ring at  $\sqrt{\sigma^2 + \pi^2} \sim 100 \text{Mpc}/h$
- cf. The contour level = (0.2, 0.06, 0.016, 0.005, 0.002, -0.001, -0.006) from the inner one

## 4. Results of 2D Anisotropy Analysis

### A. FITTED METHOD

## 4. Results of 2D Anisotropy Analysis

### A. Fitting method

- Assumption:
  - the shape of the power spectra is given by CMB experiments
  - Evolve “coherently” through all scales from the LSS

## 4. Results of 2D Anisotropy Analysis

### A. Fitting method

- The power spectra are given by,

$$\begin{aligned}\xi^s(\sigma, \pi) &= \int \frac{d^3k}{(2\pi)^3} \tilde{P}(k, \mu) e^{i\vec{k} \cdot \vec{s}} \\ &= \sum_{\text{even } l} \xi_l(s) P_l(\nu)\end{aligned}$$

$$P_{bb}(k, a) = D_m(k) G_b^2(a)$$

$$P_{\Theta\Theta}(k, a) = D_m(k) G_{\Theta}^2(a)$$

- where  $G_b$  and  $G_{\Theta}$  : the growth functions of density and peculiar velocity
- $G_b \equiv bG_{\delta_m}$  where  $b$  is the standard linear bias parameter bet.  $\delta_g$  and  $\delta_m$

- $D_m(k) = \frac{4}{9} \frac{k^4}{H_0^4 \Omega_m^2} D_{\Phi}(k)$  : shape factor (given by CMB exp.)

Song, Sabiu, Kayo and Nichol(2011)

cf.  $\Phi(\vec{k}, a) = \Phi_p(\vec{k}) \times \text{Transfer Function}(k) \times \text{Growth Function}(a)$

## 4. Results of 2D Anisotropy Analysis

### A. Fitting method

- Fitting by rescaling the transverse and radial distances

$$\sigma^{\text{fid}} = \frac{D_A^{\text{fid}}}{D_A^{\text{true}}} \sigma^{\text{true}}, \quad \pi^{\text{fid}} = \frac{H^{-1 \text{ fid}}}{H^{-1 \text{ true}}} \pi^{\text{true}}$$

$\xi^{\text{fid}}(\sigma^{\text{fid}}, \pi^{\text{fid}}) \leftarrow - \textit{fitted by rescaling} - \xi^{\text{true}}(\sigma^{\text{true}}, \pi^{\text{true}})$

- ↑ The observed anisotropy correlation ftn using ‘LCDM concordance model’      -The theoretical C.F. ↑

- Another fitting parameter,  $\sigma_p$  representing non-linear contamination to the power spectra of the density and velocity fields (FoG/Gaussian)

4. Results of 2D Anisotropy Analysis

B. CUT-OFF SCALES

AND 2D BAO CIRCLE

## 4. Results of 2D Anisotropy Analysis

### B. Cut-off scales and 2D BAO circle

- The appropriate cut-off scales:
  - 1)  $S_{\text{cut}}$ : the scales in which non-linear description of cross correlation is broken
    - 50Mpc/h
    - Allows the perfect cross-correlation between density and velocity fields
  - 2)  $\sigma_{\text{cut}}$ : The scales in which Gaussian FoG functional form is not appropriate
    - because the improved  $\xi(\sigma, \pi)$  is not applicable at bins in which the higher order terms of non-perturbative effect are dominant along l.o.s.
    - 20Mpc/h reproduced the true values successfully for DR7 CMASS
    - ? for DR9 CMASS

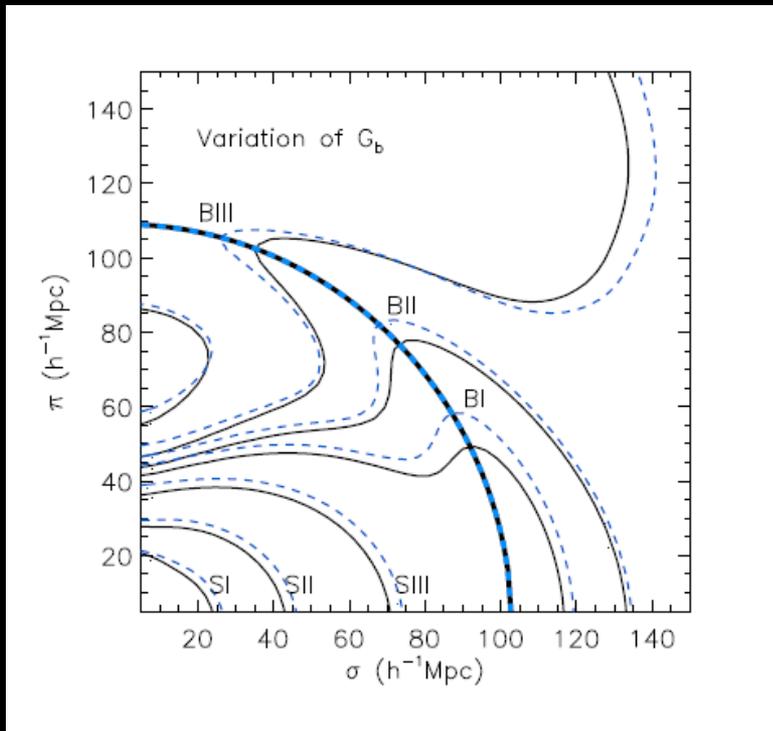
Song, Okumura and Taruya et al.(2013)

# 4. Results of 2D Anisotropy Analysis

## B. Cut-off scales and 2D BAO circle

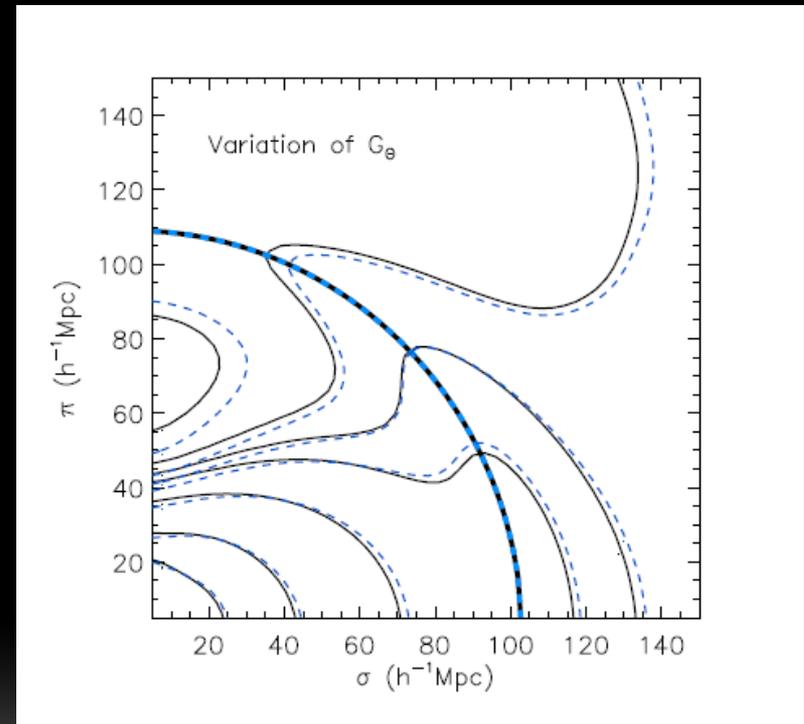
Increase  $G_b$  by 10%

(Thin black solid to thin blue dashed)



Increase  $G_{\theta}$  by 10%

(Thin black solid to thin blue dashed)



- The BAO tip points move counter-clockwise
- 2D BAO circle: inv.

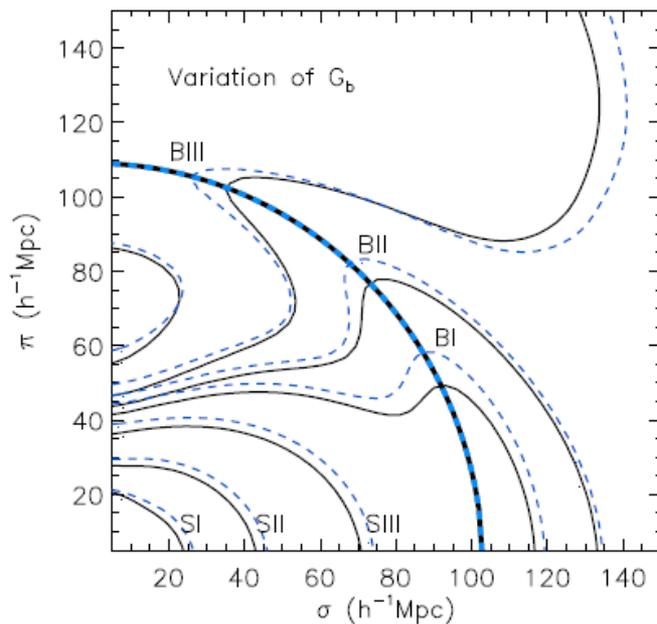
- The BAO tip points shrink toward the pivot point
- 2D BAO circle: inv.

# 4. Results of 2D Anisotropy Analysis

## B. Cut-off scales and 2D BAO circle

Increase  $G_b$  by 10%

(Thin black solid to thin blue dashed)



$$\xi_s(\sigma, \pi)(a) = \left( g_b^2 + \frac{2}{3} g_b g_\Theta + \frac{1}{5} g_\Theta^2 \right) \xi_0(r) \mathcal{P}_0(\mu) - \left( \frac{4}{3} g_b g_\Theta + \frac{4}{7} g_\Theta^2 \right) \xi_2(r) \mathcal{P}_2(\mu) + \frac{8}{35} g_\Theta^2 \xi_4(r) \mathcal{P}_4(\mu),$$

Song, Sabiu, Kayo and Nichol(2011)

- The BAO tip points move counter-clockwise
- 2D BAO circle: inv.

# 4. Results of 2D Anisotropy Analysis

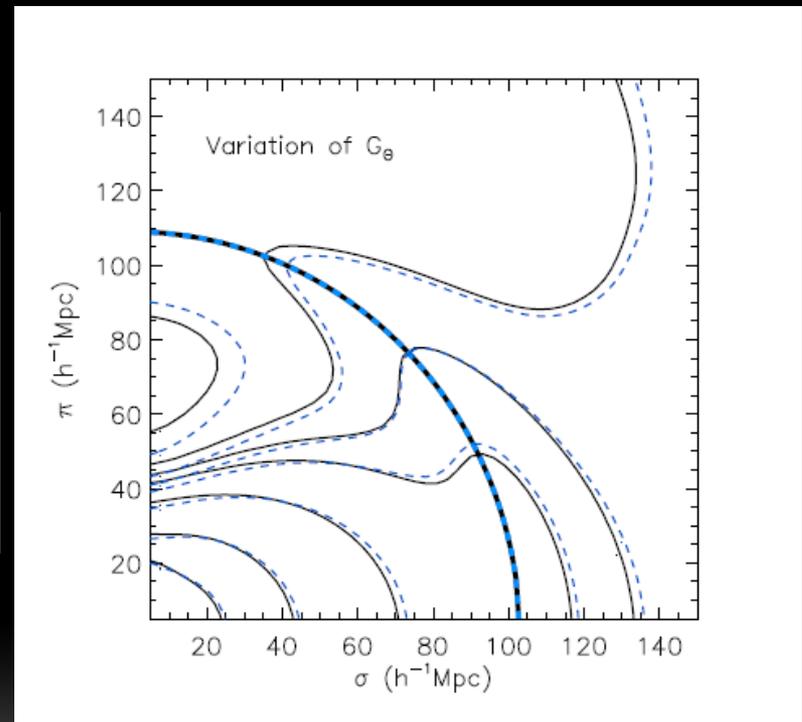
## B. Cut-off scales and 2D BAO circle

Increase  $G_{\theta}$  by 10%

(Thin black solid to thin blue dashed)

$$\begin{aligned} \xi_s(\sigma, \pi)(a) = & \left( g_b^2 + \frac{2}{3}g_b g_{\theta} + \frac{1}{5}g_{\theta}^2 \right) \xi_0(r)\mathcal{P}_0(\mu) \\ & - \left( \frac{4}{3}g_b g_{\theta} + \frac{4}{7}g_{\theta}^2 \right) \xi_2(r)\mathcal{P}_2(\mu) \\ & + \frac{8}{35}g_{\theta}^2 \xi_4(r)\mathcal{P}_4(\mu), \end{aligned}$$

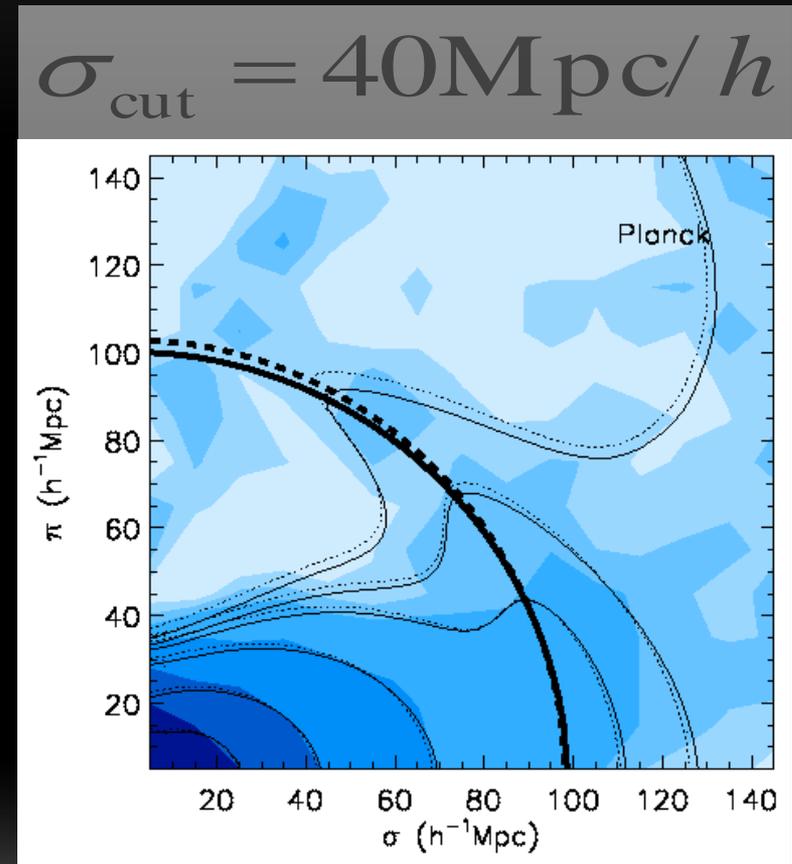
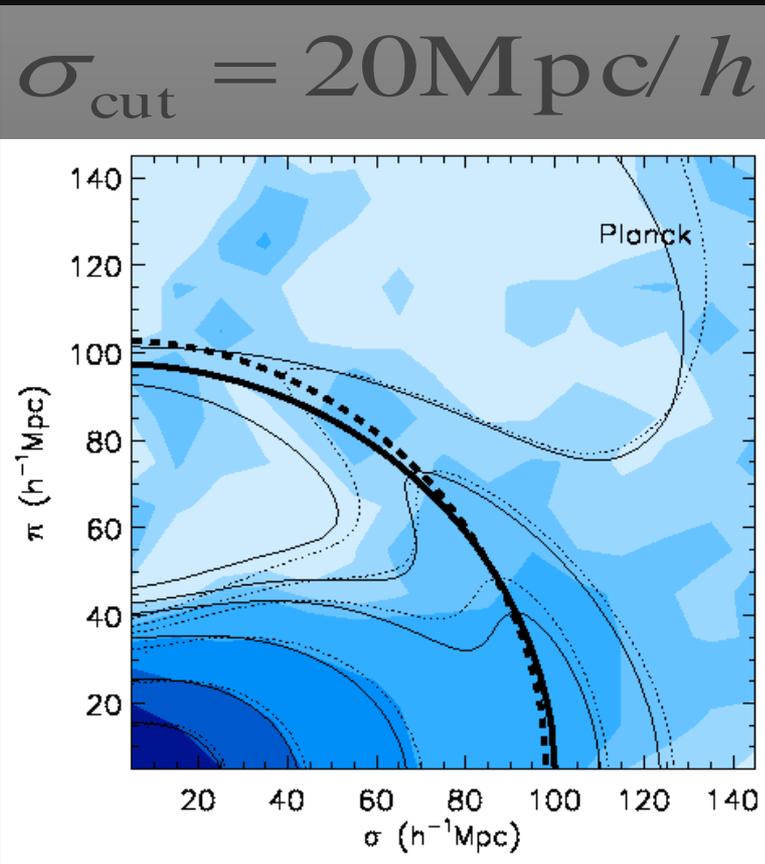
Song, Sabiu, Kayo and Nichol(2011)



- The BAO tip points shrink toward the pivot point
- 2D BAO circle: inv.

# 4. Results of 2D Anisotropy Analysis

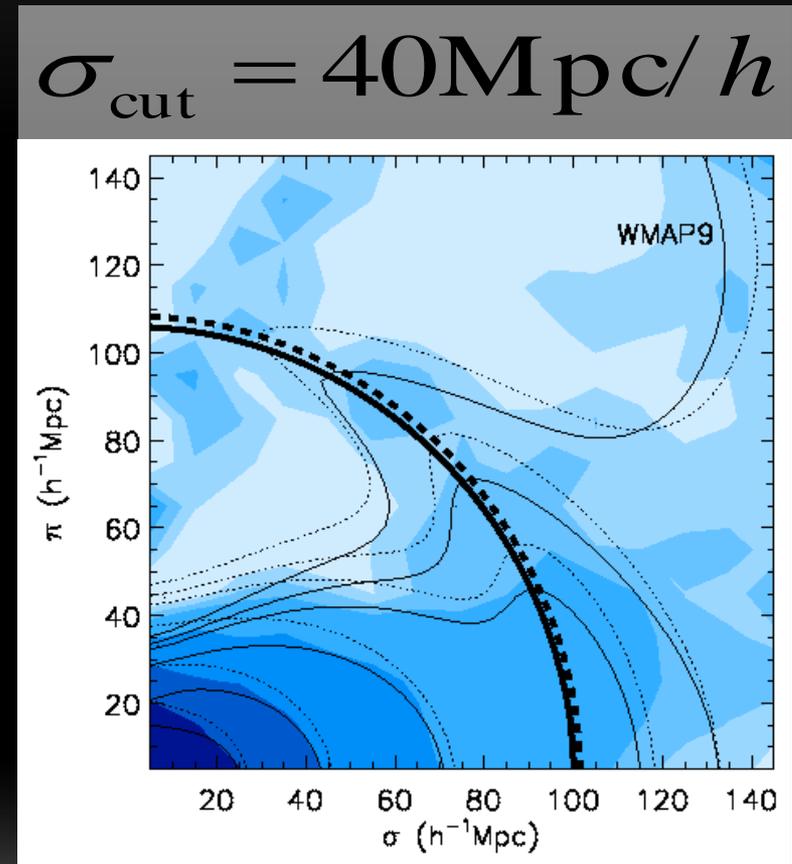
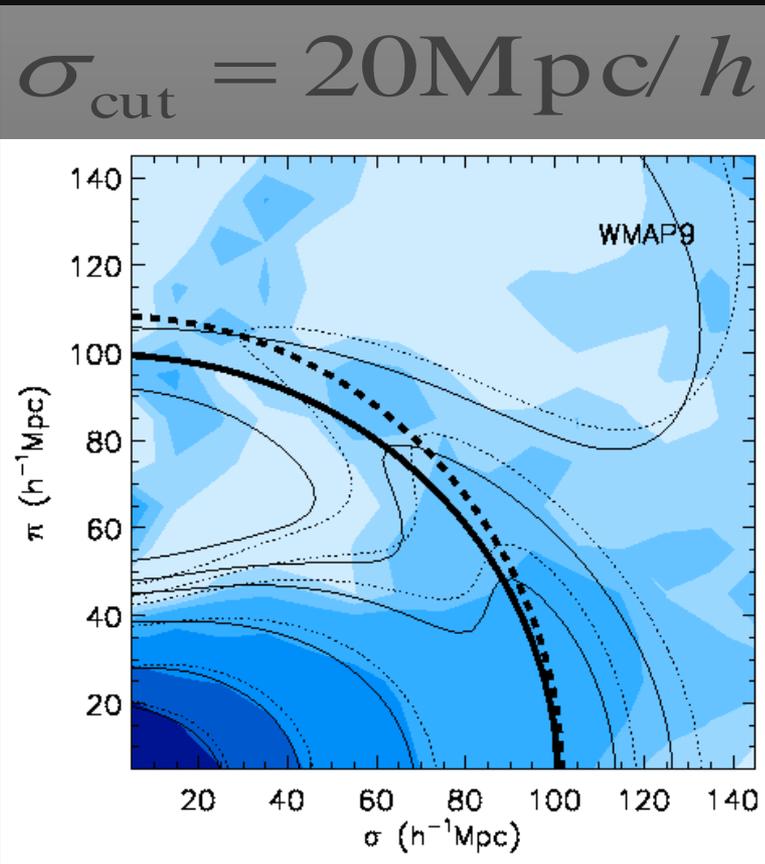
## B. Cut-off scales and 2D BAO circle



where the thin black solid represents the best fit and the thin dashed 'LCDM concordance' model cf. The contour level=(0.2, 0.06, 0.016, 0.005, 0.002, -0.001, -0.006) from the inner one

# 4. Results of 2D Anisotropy Analysis

## B. Cut-off scales and 2D BAO circle



where the thin black solid represents the best fit and the thin dashed 'LCDM concordance' model. The contour level=(0.2, 0.06, 0.016, 0.005, 0.002, -0.001, -0.006) from the inner one

## 4. Results of 2D Anisotropy Analysis

### C. The measured distances and growth fn

Parameters	Fiducial values With WMAP9 prior	Measurements
$D_A (h^{-1} \text{ Mpc})$	946.0	$916.2^{+27.2}_{-25.4}$ ☹️
$H^{-1} (h^{-1} \text{ Mpc})$	2241.5	$2163.1^{+102.0}_{-85.8}$ 😊
$G_b$	–	$1.07^{+0.07}_{-0.09}$ 😊
$G_\Theta$	0.44	$0.51^{+0.09}_{-0.08}$ 😊
$\sigma_p (h^{-1} \text{ Mpc})$	–	$1.0^{+4.6}$ 😊

Parameters	Fiducial values With Planck prior	Measurements
$D_A (h^{-1} \text{ Mpc})$	932.6	$939.7^{+26.7}_{-32.6}$ 😊
$H^{-1} (h^{-1} \text{ Mpc})$	2177.5	$2120.5^{+82.3}_{-100.6}$ 😊
$G_b$	–	$1.11^{+0.07}_{-0.10}$ 😊
$G_\Theta$	0.46	$0.47^{+0.10}_{-0.07}$ 😊
$\sigma_p (h^{-1} \text{ Mpc})$	–	$1.2^{+4.0}$ 😊

- For WMAP9,
  - Consistent with LCDM prediction
  - exits a little Tension, relative to Planck
- For Planck,
  - Consistent with LCDM prediction

The applied cut –off

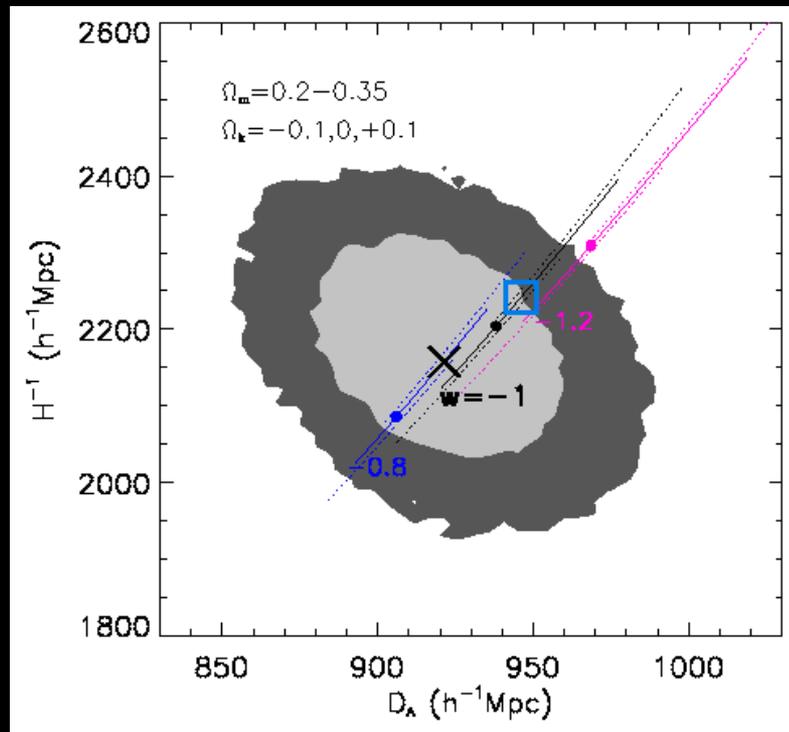
- $S_{\text{cut}}=50\text{Mpc}/h$
- $\sigma_{\text{cut}}=40\text{Mpc}/h$

2D Clustering Anisotropy Analysis using BOSS DR9

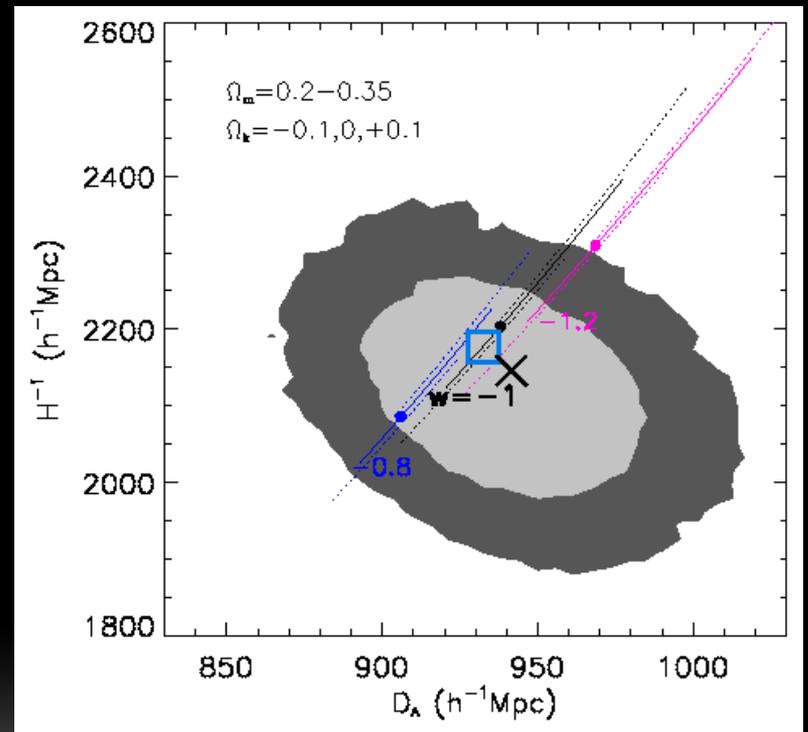
## 5. TESTING COSMOLOGY

# 5. Testing Cosmology

WMAP9 ( $D_A$ - $H_{inv}$  plane)

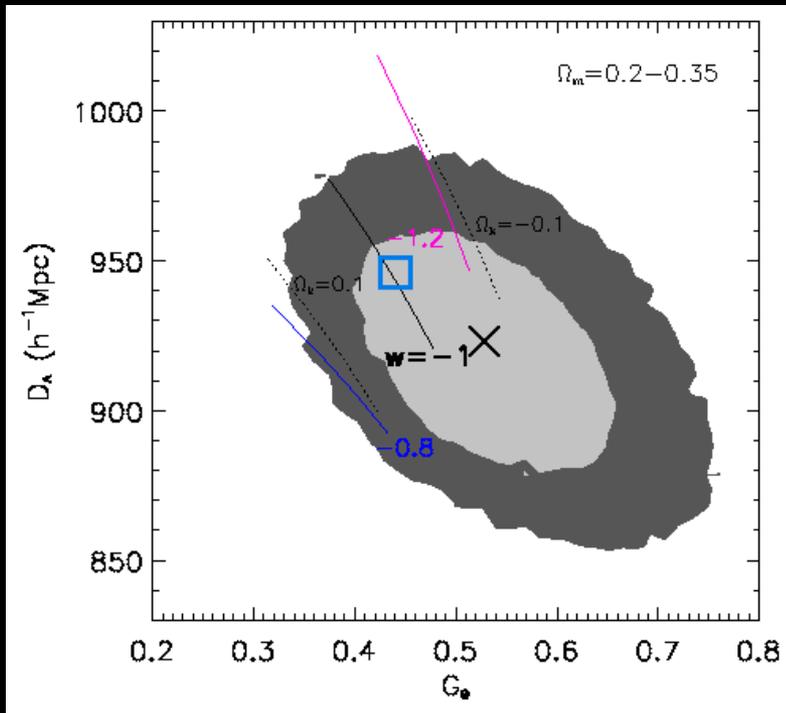


Planck ( $D_A$ - $H_{inv}$  plane)

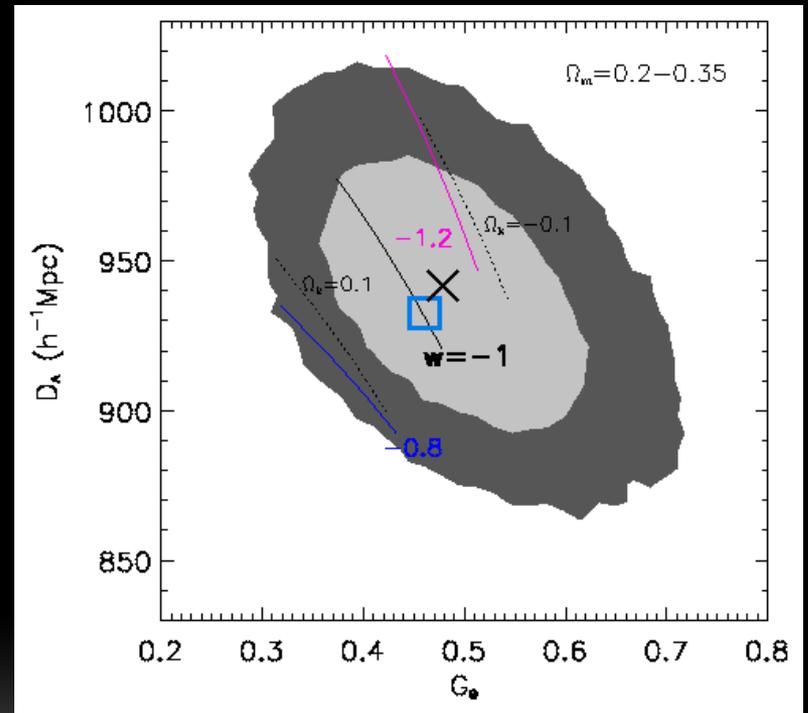


# 5. Testing Cosmology

WMAP9 ( $G_{\text{theta}}-D_A$  plane)

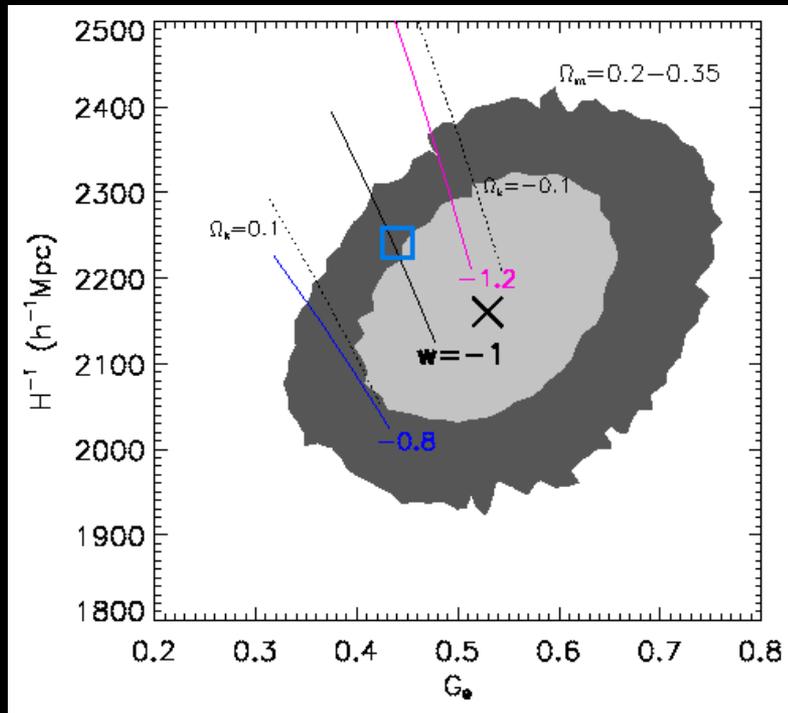


Planck ( $G_{\text{theta}}-D_A$  plane)

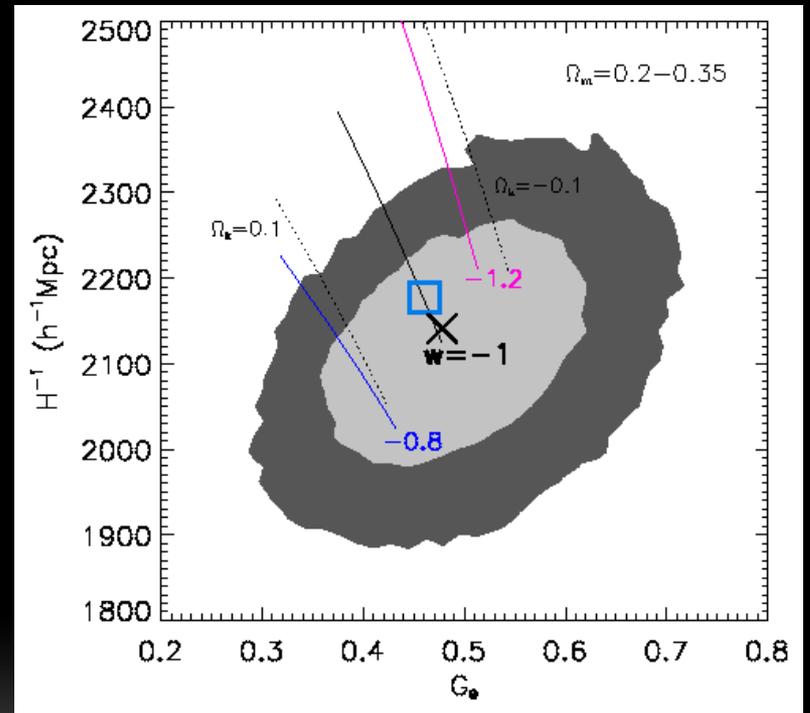


# 5. Testing Cosmology

WMAP9 ( $G_{\text{theta}}\text{-}H_{\text{inv}}$  plane)



Planck ( $G_{\text{theta}}\text{-}H_{\text{inv}}$  plane)



# 5. Testing Cosmology

- Testing Cosmology suggests
  - In  $D_A$ - $H_{inv}$ ,
    - The cosmological models all lie within a narrow region, somewhat separated from the best fit point in the Planck case
    - However, the 68% confidence level contour of the measurements overlaps the  $\Lambda$ CDM model
  - In  $G_{\theta}$ - $D_A$  &  $G_{\theta}$ - $H_{inv}$ ,
    - The cosmologies span a wider range of the space
    - The measurements are consistent with  $\Lambda$ CDM model at the 68% level confidence level
  - No sign of significant deviation from  $\Lambda$ CDM in either distances or growth, and hence no sign of deviation from general relativity either?

# 5. Testing Cosmology

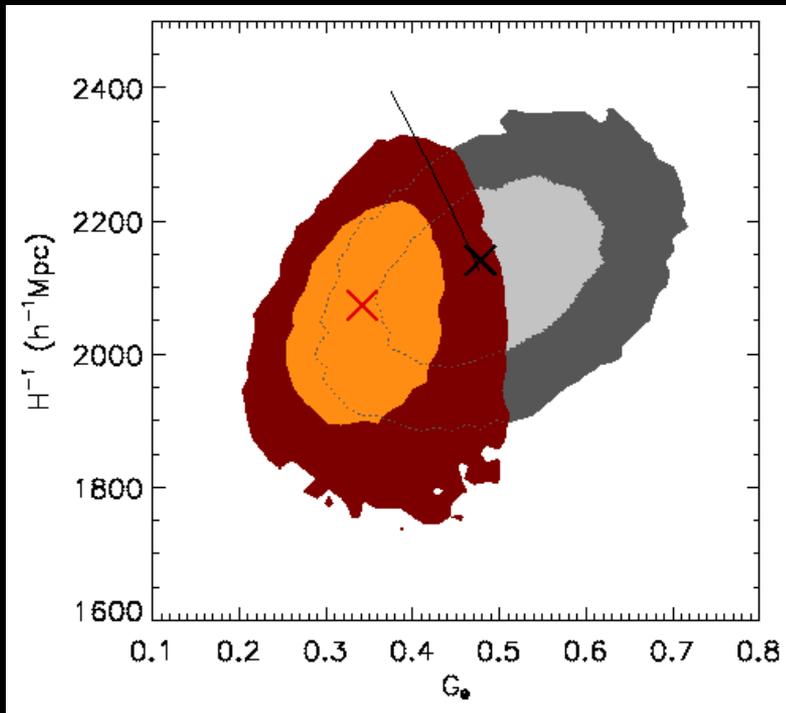
- Testing Cosmology suggests
  - However, for smaller cut-off, allowing using data in small scales, we do find deviation.
    - $G\theta$ : underestimated 0.42, 0.34 for smaller cut-off= 30Mpc/h, 20Mpc/h, respectively. But, above 40Mpc/h, invariant, indicating convergence
  - No cosmology giving good fits to the measurement contour
  - And evidence for a violation of general relativity.
    - The strong growth suppression in the measured growth rate would yield an apparent gravitational growth index  $> 0.7$ , in contrast to the value 0.55 for general relativity.

Linder, E. V.(2005)

# 5. Testing Cosmology

Planck

(Cut-off=20Mpc/h with 40Mpc/h)



- The shifting of the best fit values & the reduction in the uncertainty of  $G_{\theta}$ 
  - Indicating:
    - Substantial information to fit cosmology is coming from small scales, not just the BAO rings.
- Sensitivity of the results to low cut-off
  - Indicating:
    - Modeling on small scales is inadequate.

2D Clustering Anisotropy Analysis using BOSS DR9

## 6. CONCLUSION

## 6. Conclusion

- Using BOSS CMASS DR9 galaxies with CMB prior,
  - From the clustering correlation function,
  - We can extract the angular diameter distance  $D_A$ , Hubble scale  $H_{inv}$ , and growth rate  $G_{\theta}$ , consistent with  $\Lambda$ CDM
  - And by comparing expansion of comoving distance with growth of cosmic structure, we also test general relativity, consistent.
  - But, improvement is necessary in using small scales data to obtain more robust result.
  - The sensitivity of low cut-off to the results gives a spurious signature of breakdown of GR.
-

Thank you

