

Cosmological Constraints from the Anisotropic Clustering Analysis using BOSS DR9

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UST- KASI

Astronomy and Space Science

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Contents

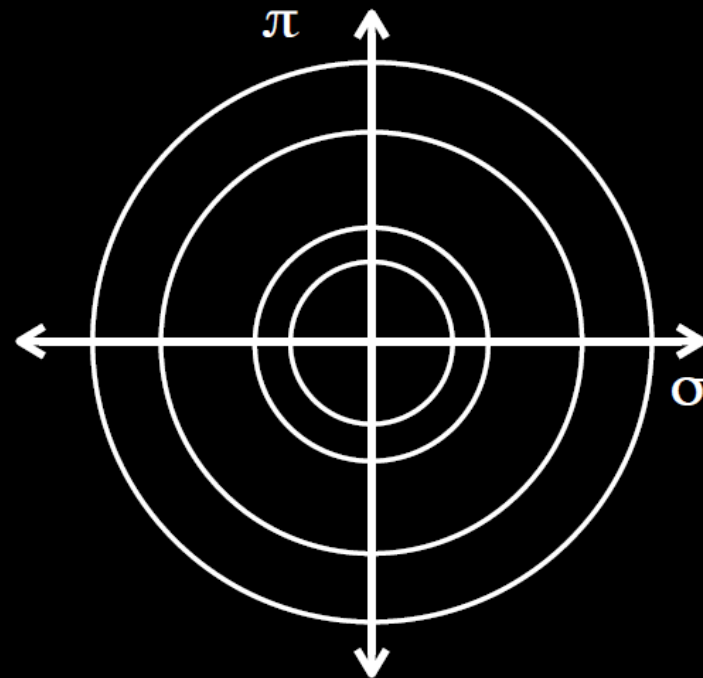
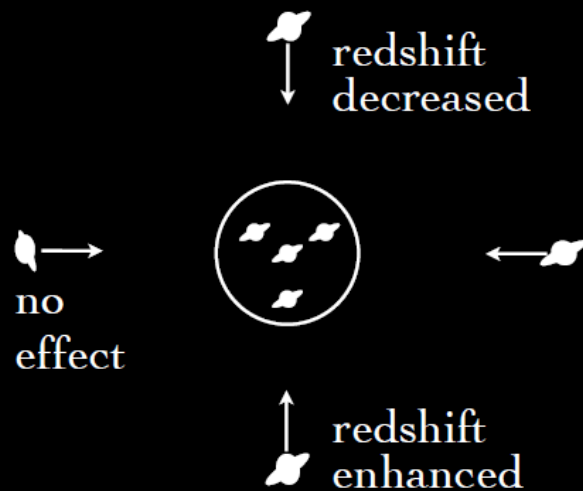
1. Introduction
2. Theoretical Model
3. Measurements
 - Measuring the correlation function
4. Results of 2D Anisotropy Analysis
 - Fitting method
 - Cut-off scales and 2D BAO circle
 - The measured distances and growth functions
5. Testing Cosmology
6. Conclusion

Cosmological Constraints from the Anisotropic Clustering Analysis
using BOSS DR9

1. INTRODUCTION

1. Introduction

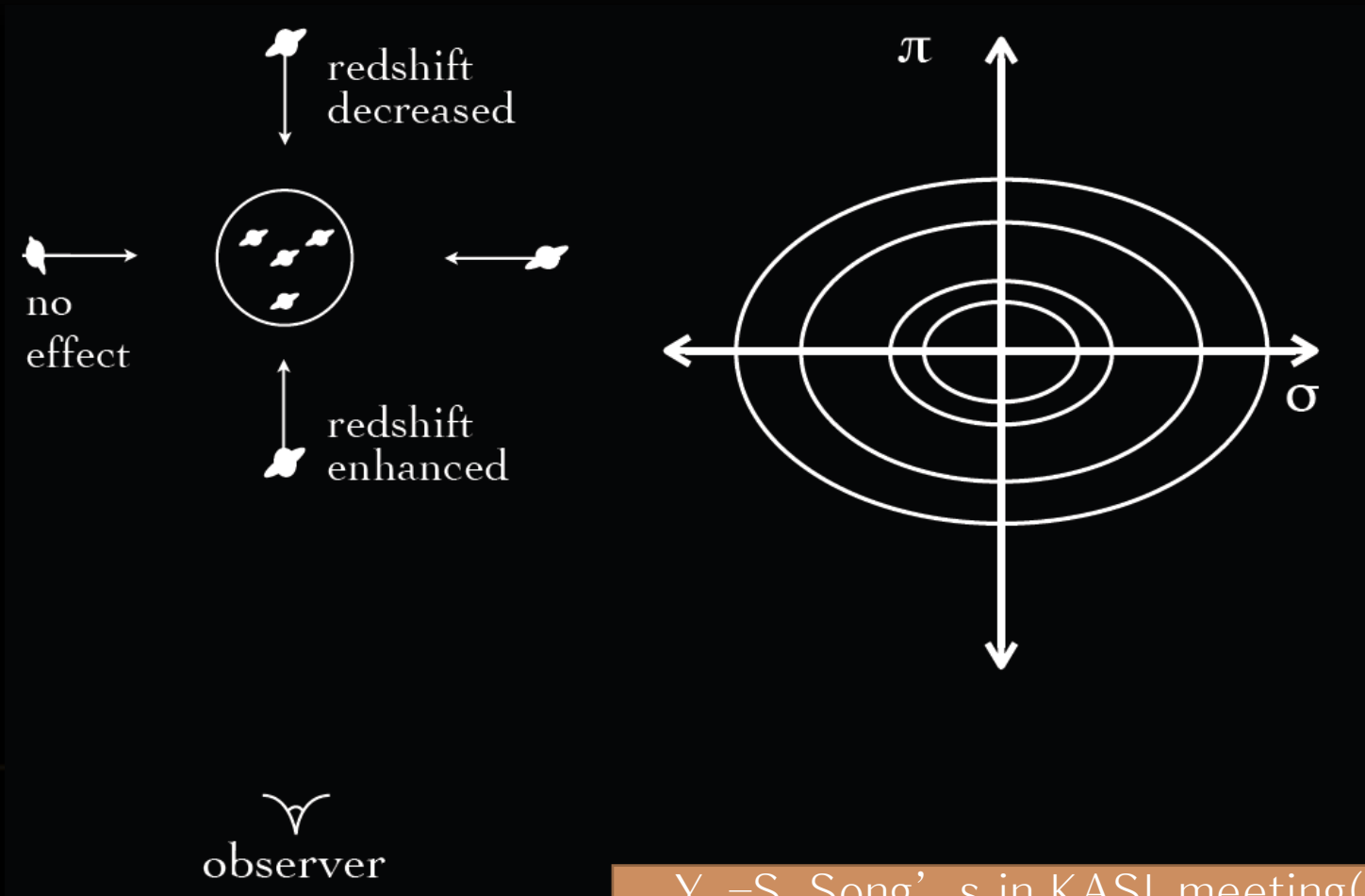
- Redshift-space distortion



observer

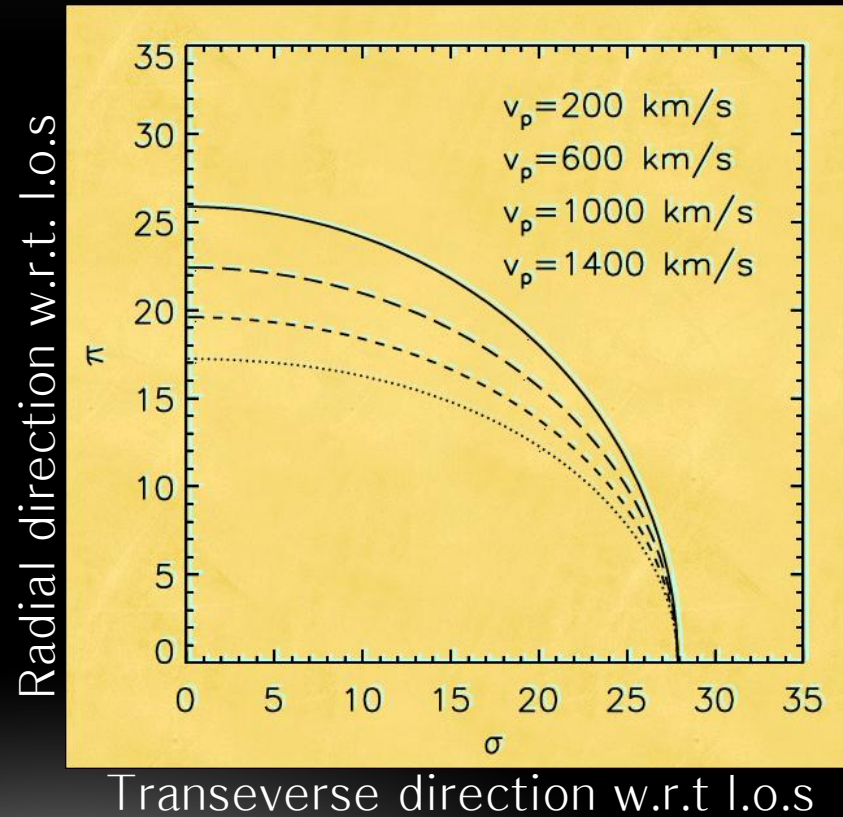
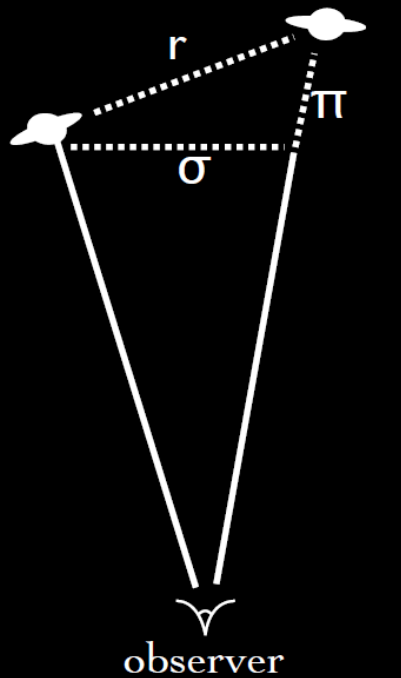
1. Introduction

- Redshift-space distortion



1. Introduction

- Redshift-space distortion



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2. THEORETICAL MODEL

2. Theoretical Model

- Redshift-space distortion(RSD)

:An anisotropic features in the clustering pattern of galaxies in redshift space

- Main features in the resultant two-point correlation function, ξ_s
 - At linear regimes,
 - Kaiser effect- squeezed clustering pattern along l.o.s
 - enhance the amplitude of the observed correlation ftn
 - At non-linear regimes,
 - Finger of God effect- elongate clustering along l.o.s
 - caused by the random virial motions of galaxies residing at halos
 - cf. BAO peak

2. Theoretical Model

- Redshift-space power spectrum

$$\tilde{P}(k, \mu) = \sum_{n=0}^4 Q_{2n}(k) \mu^{2n} G^{FoG}(k\mu\sigma_p)$$

Taruva, Nishimichi, and Saito (2010)

$$cf. P_{Kaiser}(k, \mu) = \begin{cases} (1 + f\mu^2)^2 P_{\delta\delta}(k) & ; \text{linear} \\ P_{\delta\delta}(k) + 2f\mu^2 P_{\delta\theta}(k) + f^2 \mu^4 P_{\theta\theta}(k) & ; \text{non-linear} \end{cases}$$

N. Kaiser (1987)

- Redshift-space correlation function

$$\begin{aligned} \xi^s(\sigma, \pi) &= \int \frac{d^3k}{(2\pi)^3} \tilde{P}(k, \mu) e^{i\vec{k} \cdot \vec{s}} \\ &= \sum_{\text{even } l} \xi_l(s) P_l(v) \quad \text{where } P_l \text{ is the Legendre polynomials} \end{aligned}$$

$$v = \pi / s, \quad s = (\sigma^2 + \pi^2)^{1/2}$$

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3. MEASUREMENTS

3. Measurements

- Data sample: BOSS galaxy samples, CMAS
- Coordinate transformation from (RA, dec, z) to two fiducial spatially-flat cosmological models (Planck ($w_c=0.1138$, $H_0=70$) and Planck ($w_b=0.02206$))
- Landy-Szalay estimator(2D):

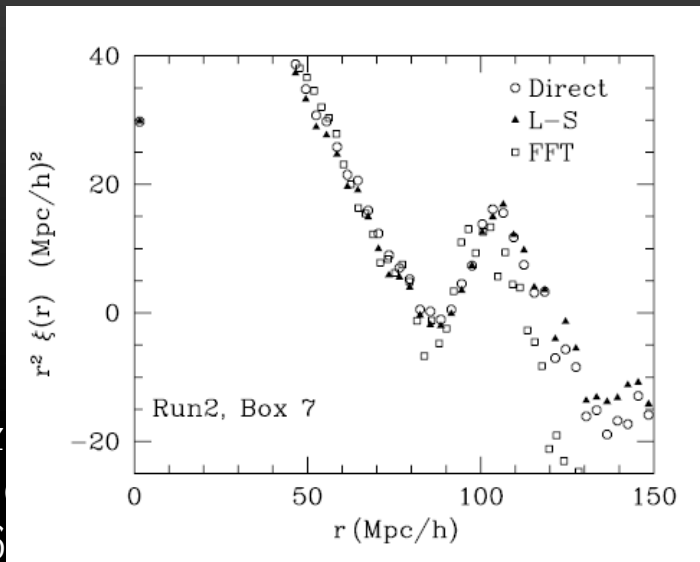
$$\xi(\sigma, \pi) = \frac{DD(\sigma, \pi) - 2DR(\sigma, \pi) + RR(\sigma, \pi)}{RR(\sigma, \pi)} \approx \frac{DD(\sigma, \pi)}{RR(\sigma, \pi)} - 1$$

correlation function

if the random map is perfectly random

Landy, S. D. & Szalay, A. S. (1993)

where $DD(\sigma, \pi)$: the number of pairs in Data with separation $\sigma \pm \delta(\sigma)$ and $\pi \pm \delta(\pi)$

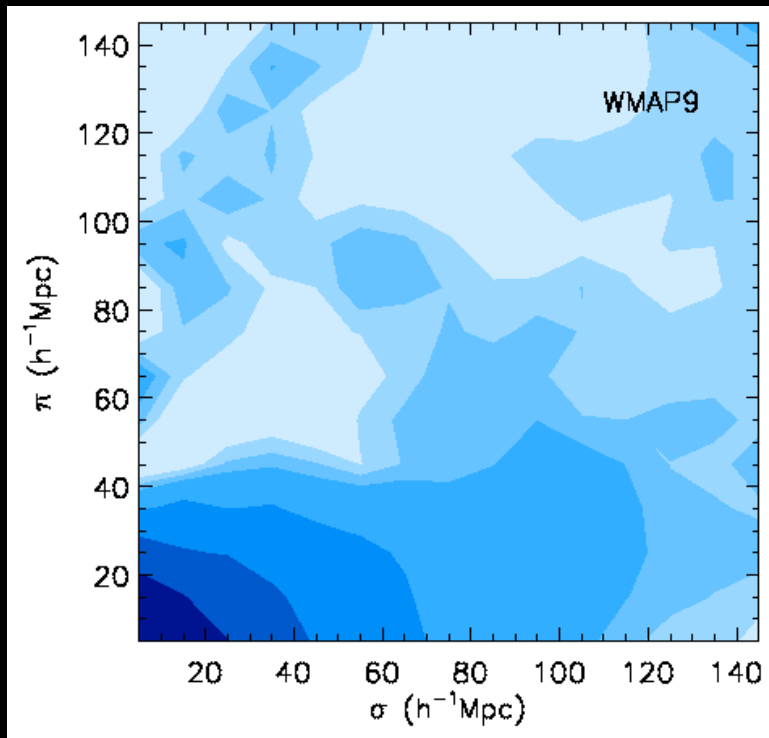


Huff, E. et al. (2007)

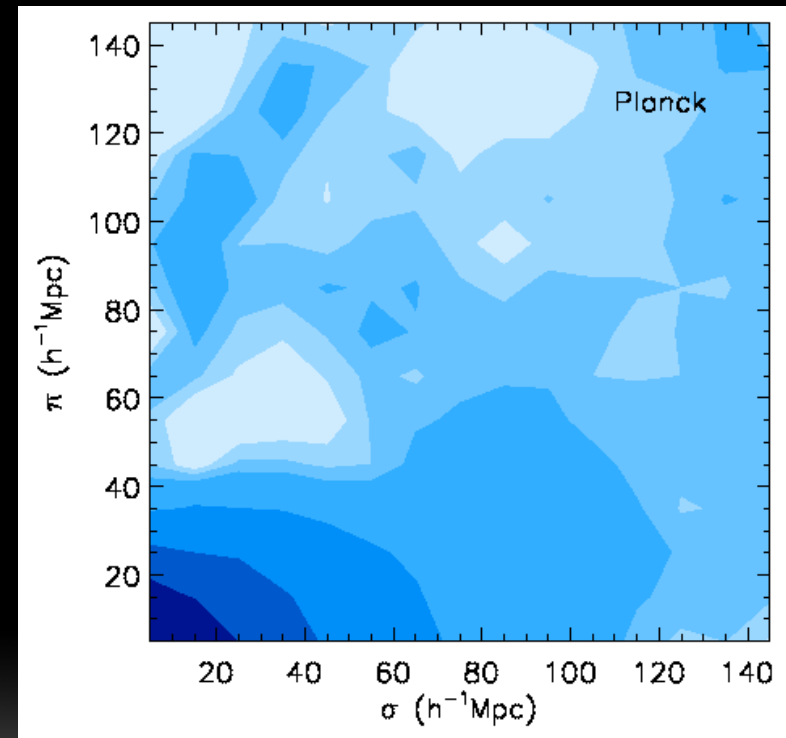
3. Measurements

:Measuring the correlation function

With WMAP9 early universe prior



With Planck early universe prior



- Kaiser effect at small σ
 - 2D BAO ring at $\sqrt{\sigma^2 + \pi^2} \sim 100 h^{-1}\text{Mpc}$
- cf. The contour level=(0.2, 0.06, 0.016, 0.005, 0.002, -0.001, -0.006) from the inner one

4. Results of 2D Anisotropy Analysis

A. FITTED METHOD

4. Results of 2D Anisotropy Analysis

A. Fitting method

- Assumption:
 - the shape of the power spectra is given by CMB experiments
 - Evolve “coherently” through all scales from the LSS

4. Results of 2D Anisotropy Analysis

A. Fitting method

- The power spectra are given by,

$$\begin{aligned}\xi^s(\sigma, \pi) &= \int \frac{d^3k}{(2\pi)^3} \tilde{P}(k, \mu) e^{i\vec{k} \cdot \vec{s}} \\ &= \sum_{\text{even } l} \xi_l(s) P_l(\nu)\end{aligned}$$

$$P_{bb}(k, a) = D_m(k) G_b^2(a)$$

$$P_{\Theta\Theta}(k, a) = D_m(k) G_{\Theta}^2(a)$$

- where G_b and G_{Θ} : the growth functions of density and peculiar velocity
- $G_b \equiv b G_{\delta_m}$ where b is the standard linear bias parameter bet. δ_g and δ_m

$$- D_m(k) = \frac{4}{9} \frac{k^4}{H_0^4 \Omega_m^2} D_{\Phi}(k) : \text{shape factor (given by CMBexp.)}$$

Song, Sabiu, Kayo and Nichol(2011)

$$\text{cf. } \Phi(\vec{k}, a) = \Phi_p(\vec{k}) \times \text{Transfer Function}(k) \times \text{Growth Function}(a)$$

4. Results of 2D Anisotropy Analysis

A. Fitting method

- Fitting by rescaling the transverse and radial distances

$$\sigma^{\text{fid}} = \frac{D_A^{\text{fid}}}{D_A^{\text{true}}} \sigma^{\text{true}}, \quad \pi^{\text{fid}} = \frac{H^{-1 \text{ fid}}}{H^{-1 \text{ true}}} \pi^{\text{true}}$$

$$\xi^{\text{fid}}(\sigma^{\text{fid}}, \pi^{\text{fid}}) \leftarrow \text{--fitted by rescaling--} \xi^{\text{true}}(\sigma^{\text{true}}, \pi^{\text{true}})$$

– ↑ The observed anisotropy correlation ftn
using ‘ΛCDM concordance model’

– The theoretical C.F. ↑

- Another fitting parameter, σ_p representing non-linear contamination to the power spectra of the density and velocity fields (FoG/Gaussian)

4. Results of 2D Anisotropy Analysis

B. CUT-OFF SCALES AND 2D BAO CIRCLE

4. Results of 2D Anisotropy Analysis

B. Cut-off scales and 2D BAO circle

- The appropriate cut-off scales:
 - 1) S_{cut} : the scales in which non-linear description of cross correlation is broken
 - 50Mpc/h
 - Allows the perfect cross-correlation between density and velocity fields
 - 2) σ_{cut} : The scales in which Gaussian FoG functional form is not appropriate
 - because the improved $\xi(\sigma, \pi)$ is not applicable at bins in which the higher order terms of non-perturbative effect are dominant along l.o.s.
 - 20Mpc/h reproduced the true values successfully for DR7 CMASS
 - ? for DR9 CMASS

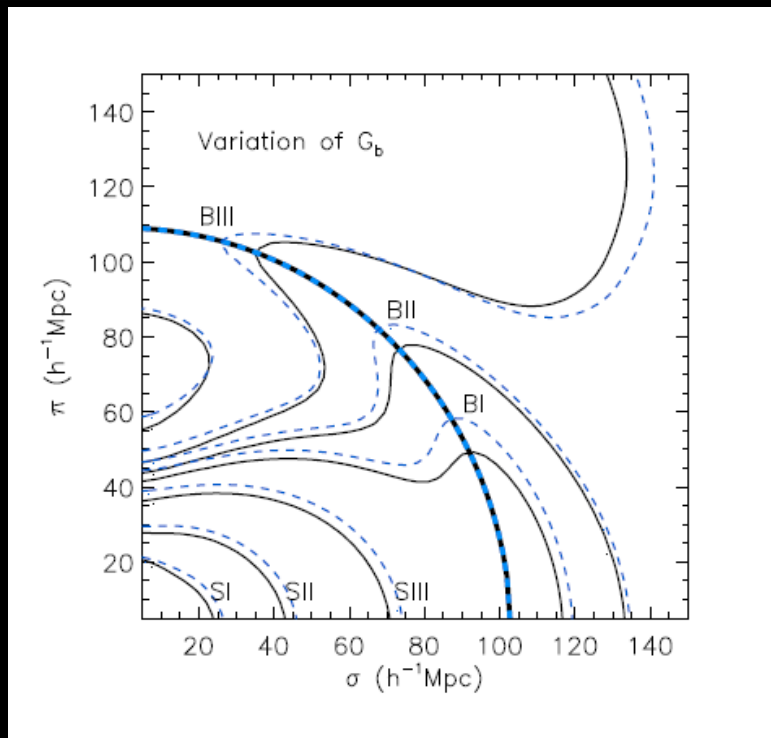
Song, Okumura and Taruya et al.(2013)

4. Results of 2D Anisotropy Analysis

B. Cut-off scales and 2D BAO circle

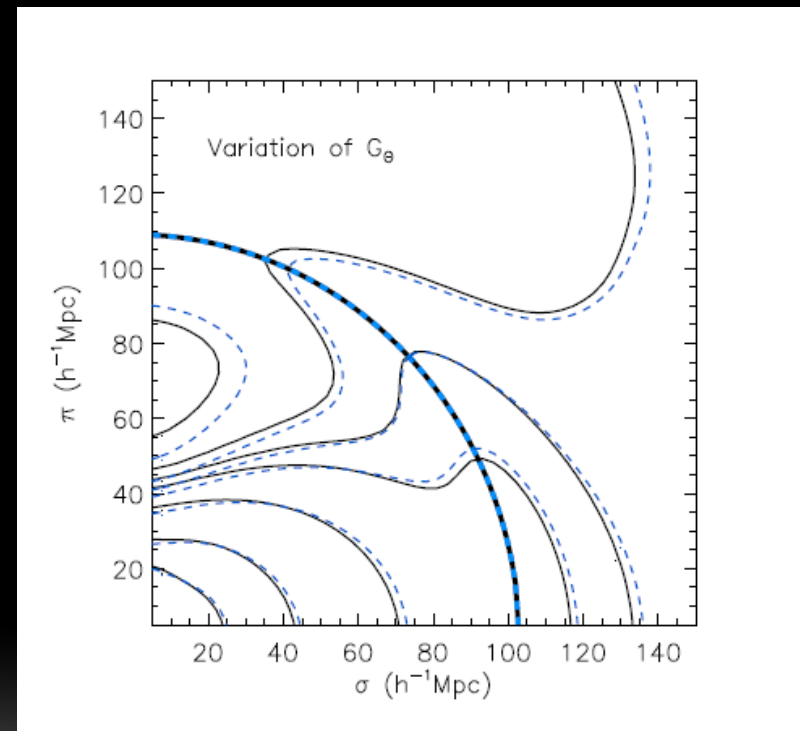
Increase G_b by 10%

(Thin black solid to thin blue dashed)



Increase G_{θ} by 10%

(Thin black solid to thin blue dashed)



- The BAO tip points move counter-clockwise
- 2D BAO circle: inv.

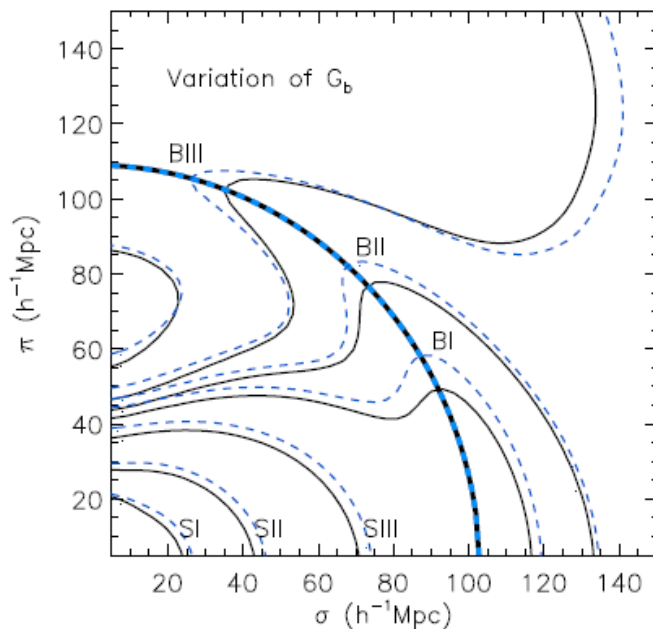
- The BAO tip points shrink toward the pivot point
- 2D BAO circle: inv.

4. Results of 2D Anisotropy Analysis

B. Cut-off scales and 2D BAO circle

Increase G_b by 10%

(Thin black solid to thin blue dashed)



$$\xi_s(\sigma, \pi)(a) = \left(g_b^2 + \frac{2}{3} g_b g_\Theta + \frac{1}{5} g_\Theta^2 \right) \xi_0(r) \mathcal{P}_0(\mu) - \left(\frac{4}{3} g_b g_\Theta + \frac{4}{7} g_\Theta^2 \right) \xi_2(r) \mathcal{P}_2(\mu) + \frac{8}{35} g_\Theta^2 \xi_4(r) \mathcal{P}_4(\mu),$$

Song, Sabiu, Kayo and Nichol(2011)

- The BAO tip points move counter-clockwise
- 2D BAO circle: inv.

4. Results of 2D Anisotropy Analysis

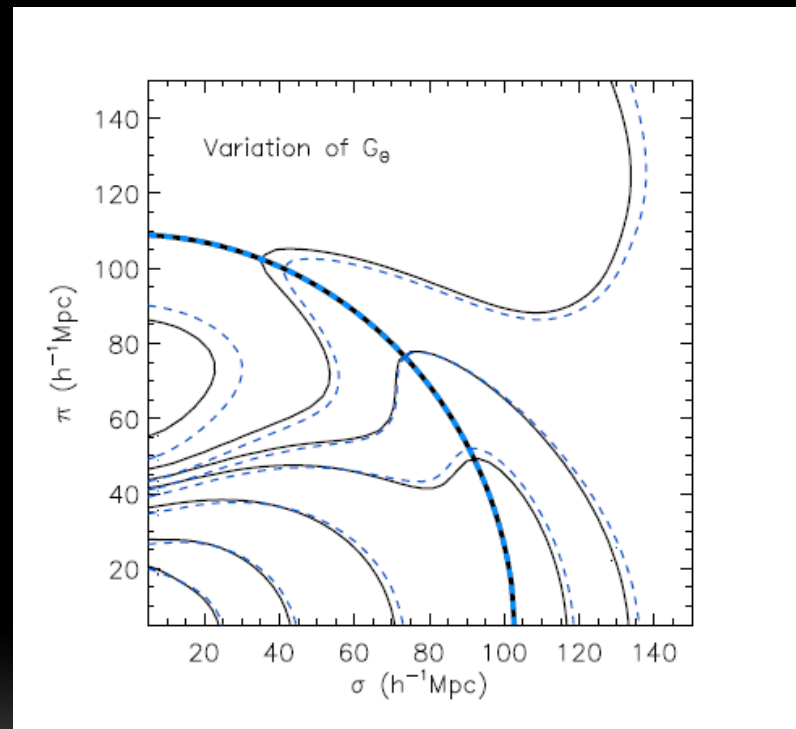
B. Cut-off scales and 2D BAO circle

Increase G_{θ} by 10%

(Thin black solid to thin blue dashed)

$$\begin{aligned}\xi_s(\sigma, \pi)(a) = & \left(g_b^2 + \frac{2}{3}g_b g_{\Theta} + \frac{1}{5}g_{\Theta}^2 \right) \xi_0(r) \mathcal{P}_0(\mu) \\ & - \left(\frac{4}{3}g_b g_{\Theta} + \frac{4}{7}g_{\Theta}^2 \right) \xi_2(r) \mathcal{P}_2(\mu) \\ & + \frac{8}{35}g_{\Theta}^2 \xi_4(r) \mathcal{P}_4(\mu),\end{aligned}$$

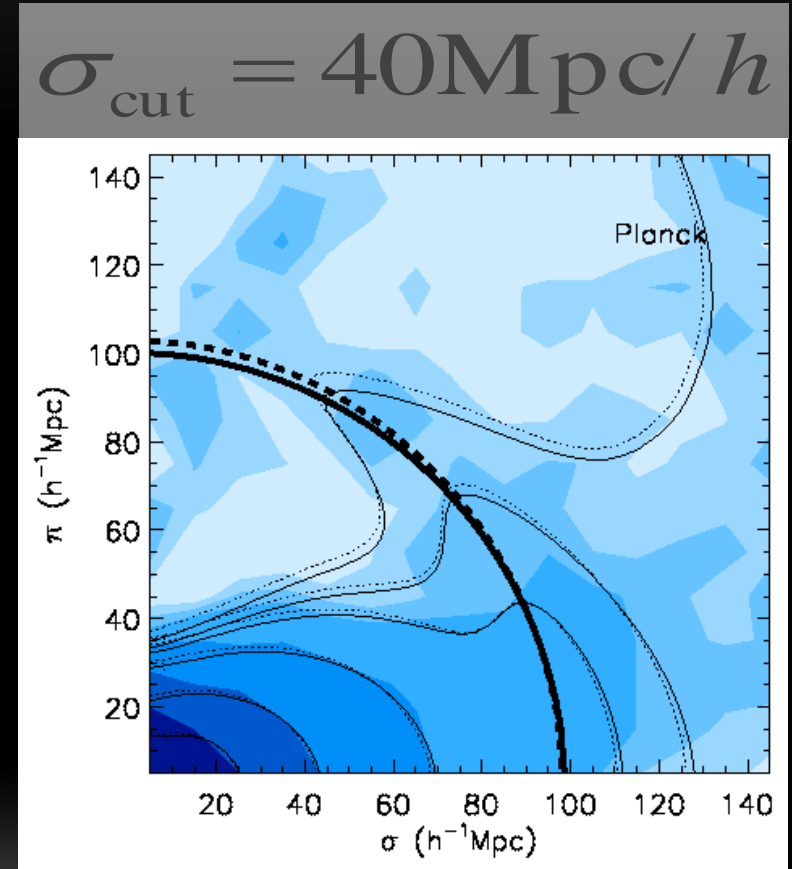
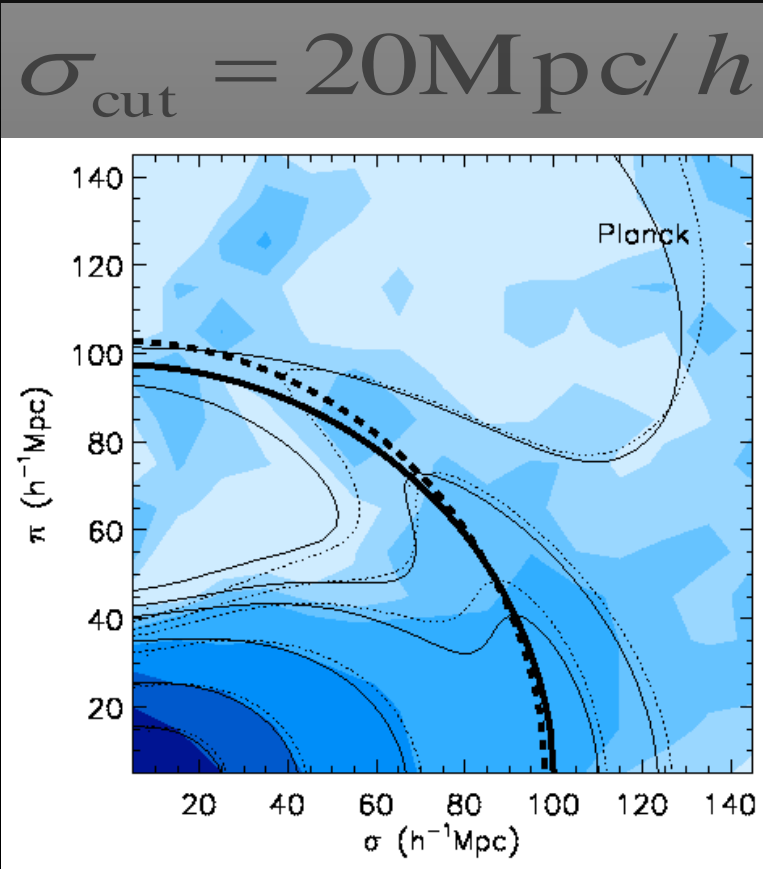
Song, Sabiu, Kayo and Nichol(2011)



- The BAO tip points shrink toward the pivot point
- 2D BAO circle: inv.

4. Results of 2D Anisotropy Analysis

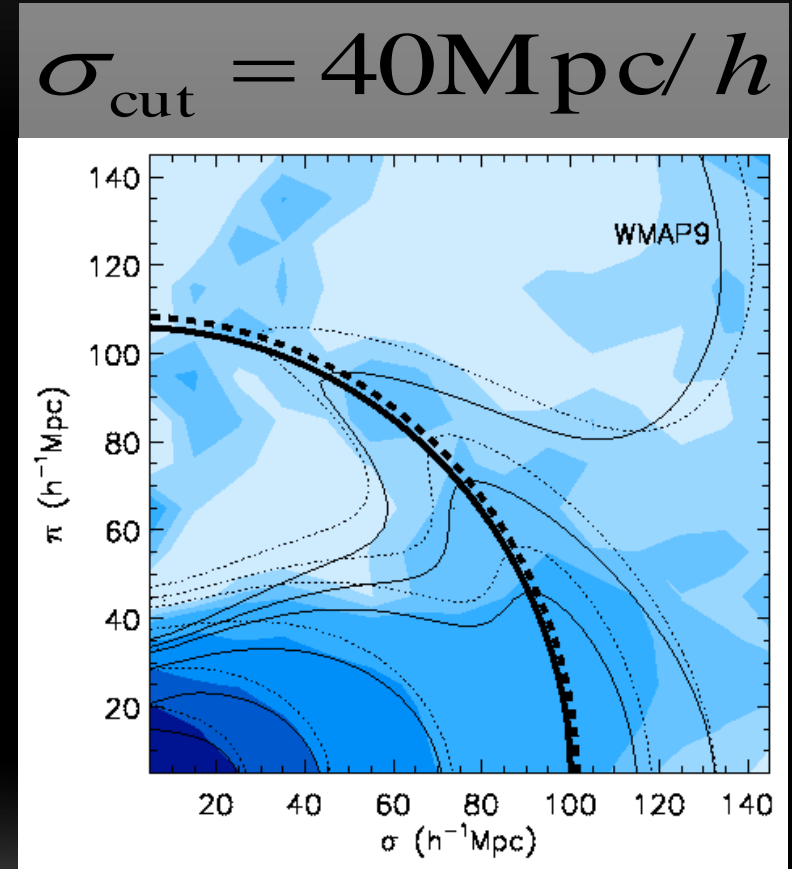
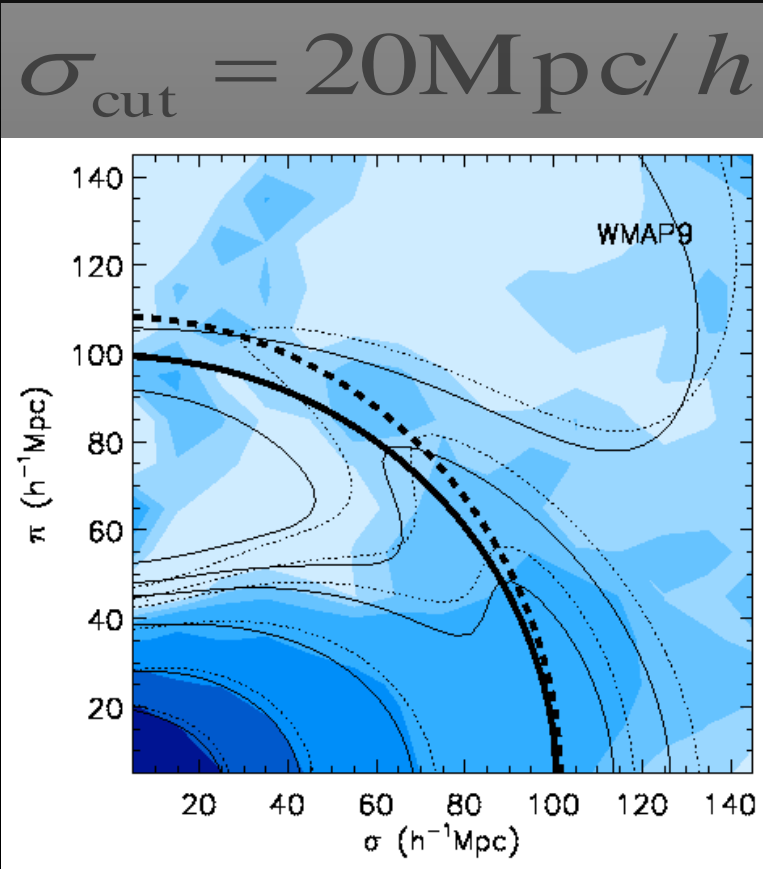
B. Cut-off scales and 2D BAO circle



where the thin black solid represents the best fit and the thin dashed 'LCDM concordance' model cf. The contour level=(0.2, 0.06, 0.016, 0.005, 0.002, -0.001, -0.006) from the inner one

4. Results of 2D Anisotropy Analysis

B. Cut-off scales and 2D BAO circle



where the thin black solid represents the best fit and the thin dashed 'LCDM concordance' model cf. The contour level=(0.2, 0.06, 0.016, 0.005, 0.002, -0.001, -0.006) from the inner one

4. Results of 2D Anisotropy Analysis

C. The measured distances and growth fn

Parameters	Fiducial values	Measurements
With WMAP9 prior		
$D_A (h^{-1} \text{ Mpc})$	946.0	$916.2^{+27.2}_{-25.4}$ ☹️
$H^{-1} (h^{-1} \text{ Mpc})$	2241.5	$2163.1^{+102.0}_{-85.8}$ 😊
G_b	—	$1.07^{+0.07}_{-0.09}$ 😊
G_Θ	0.44	$0.51^{+0.09}_{-0.08}$ 😊
$\sigma_p (h^{-1} \text{ Mpc})$	—	$1.0^{+4.6}$
Parameters	Fiducial values	Measurements
With Planck prior		
$D_A (h^{-1} \text{ Mpc})$	932.6	$939.7^{+26.7}_{-32.6}$ 😊
$H^{-1} (h^{-1} \text{ Mpc})$	2177.5	$2120.5^{+82.3}_{-100.6}$ 😊
G_b	—	$1.11^{+0.07}_{-0.10}$ 😊
G_Θ	0.46	$0.47^{+0.10}_{-0.07}$ 😊
$\sigma_p (h^{-1} \text{ Mpc})$	—	$1.2^{+4.0}$

- For WMAP9,
 - Consistent with LCDM prediction
 - exits a little Tension, relative to Planck
- For Planck,
 - Consistent with LCDM prediction

The applied cut –off

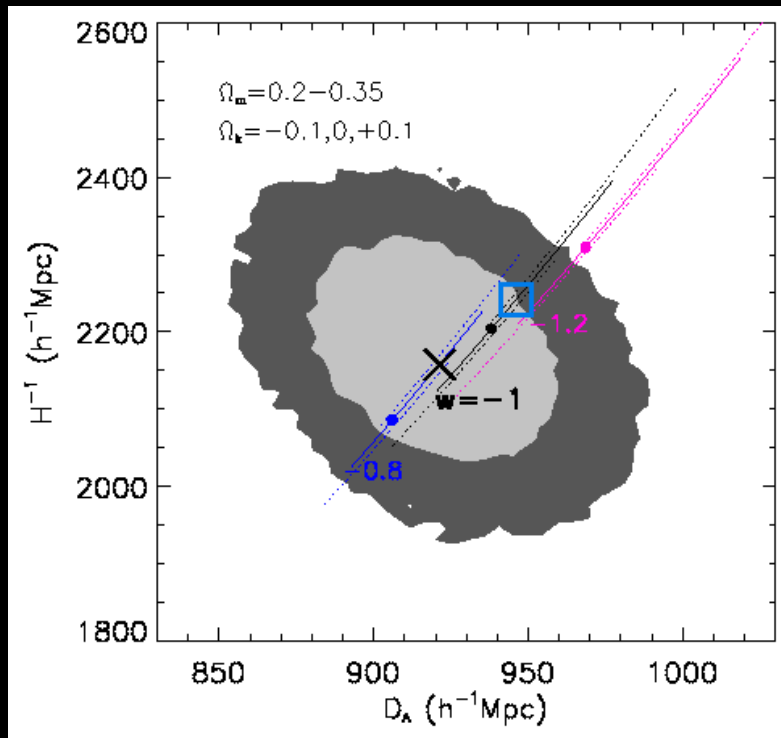
- $S_{\text{cut}}=50\text{Mpc}/h$
- $\sigma_{\text{cut}}=40\text{Mpc}/h$

2D Clustering Anisotropy Analysis using BOSS DR9

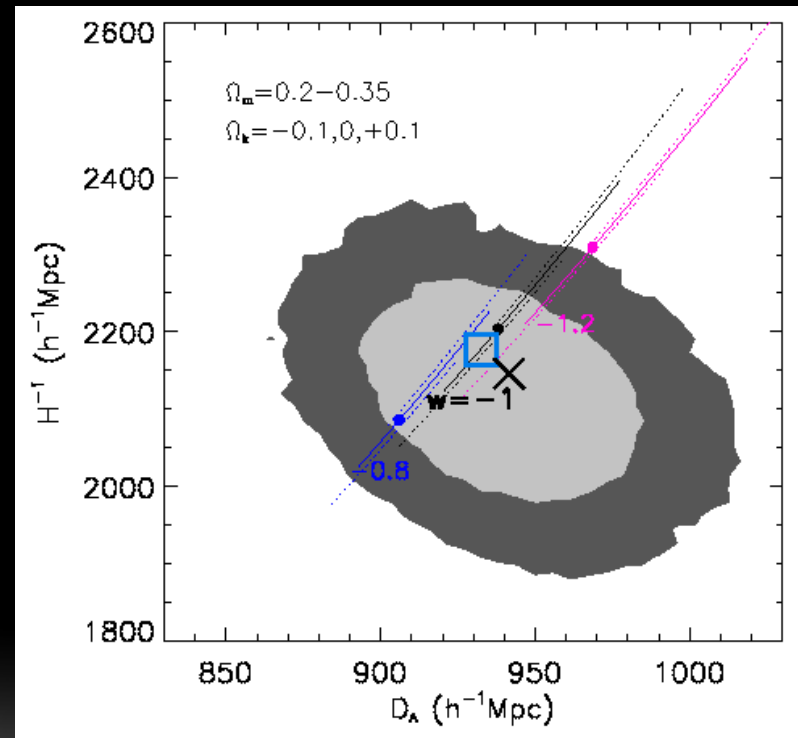
5. TESTING COSMOLOGY

5. Testing Cosmology

WMAP9 (D_A - H_{inv} plane)

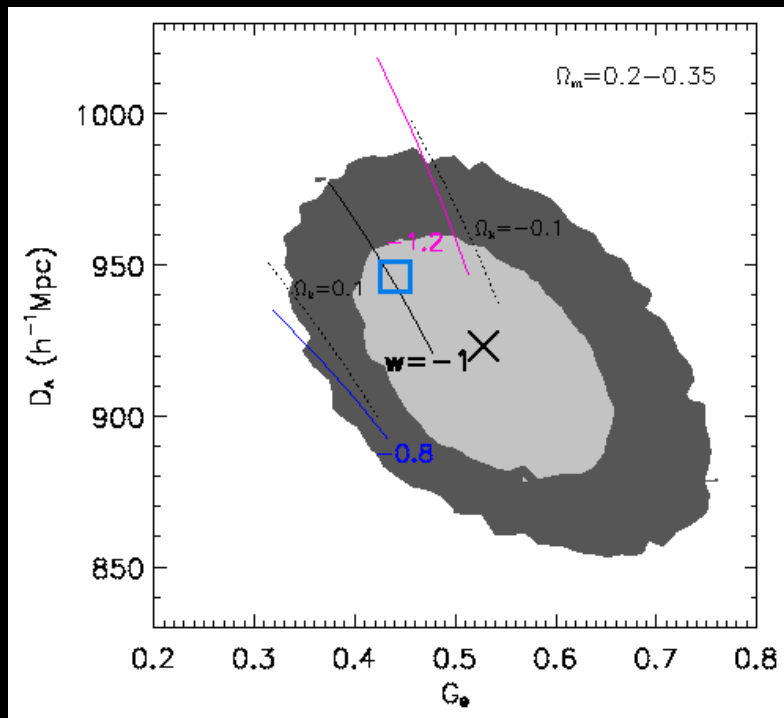


Planck (D_A - H_{inv} plane)

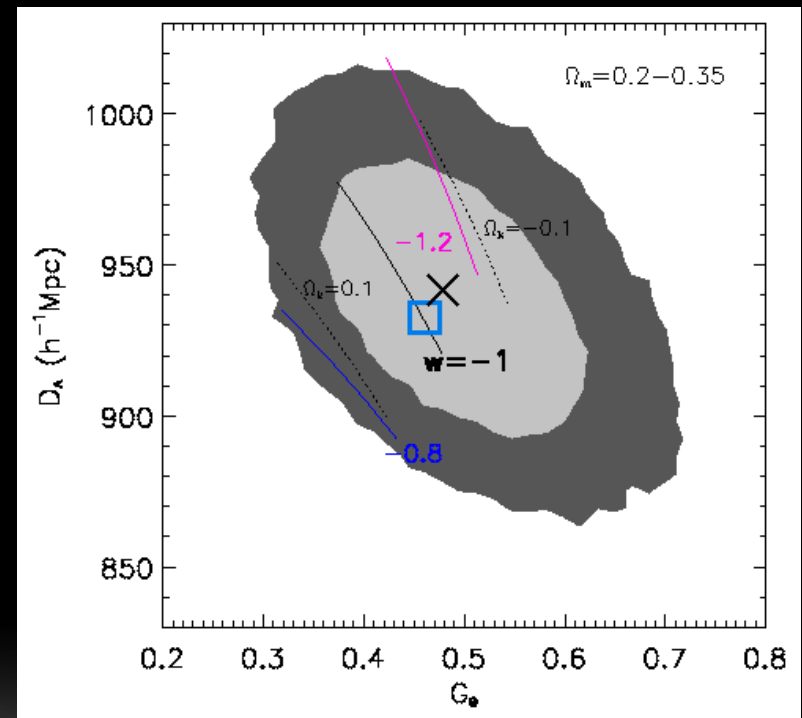


5. Testing Cosmology

WMAP9 ($G_{\text{theta}}-D_A$ plane)

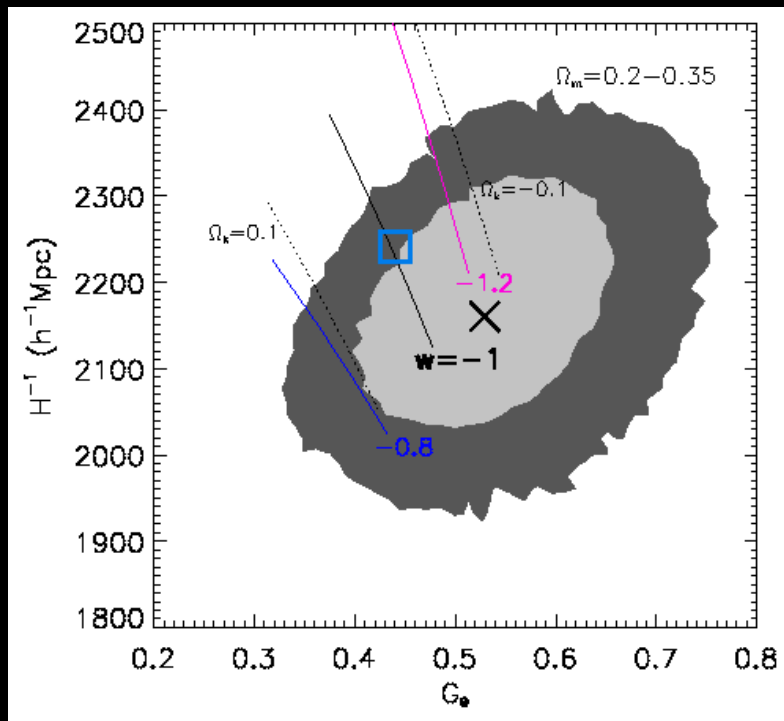


Planck ($G_{\text{theta}}-D_A$ plane)

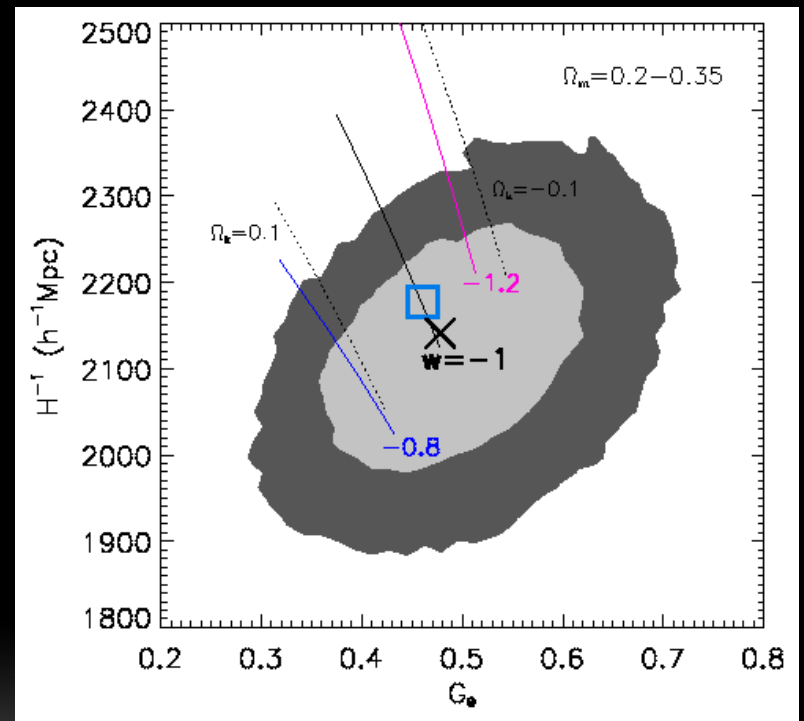


5. Testing Cosmology

WMAP9 ($G_{\text{theta}}\text{-}H_{\text{inv}}$ plane)



Planck ($G_{\text{theta}}\text{-}H_{\text{inv}}$ plane)



5. Testing Cosmology

- Testing Cosmology suggests
 - In D_A - H_{inv} ,
 - The cosmological models all lie within a narrow region, somewhat separated from the best fit point in the Planck case
 - However, the 68% confidence level contour of the measurements overlaps the Λ CDM model
 - In G_{θ} - D_A & G_{θ} - H_{inv} ,
 - The cosmologies span a wider range of the space
 - The measurements are consistent with Λ CDM model at the 68% level confidence level
 - No sign of significant deviation from Λ CDM in either distances or growth, and hence no sign of deviation from general relativity either?

5. Testing Cosmology

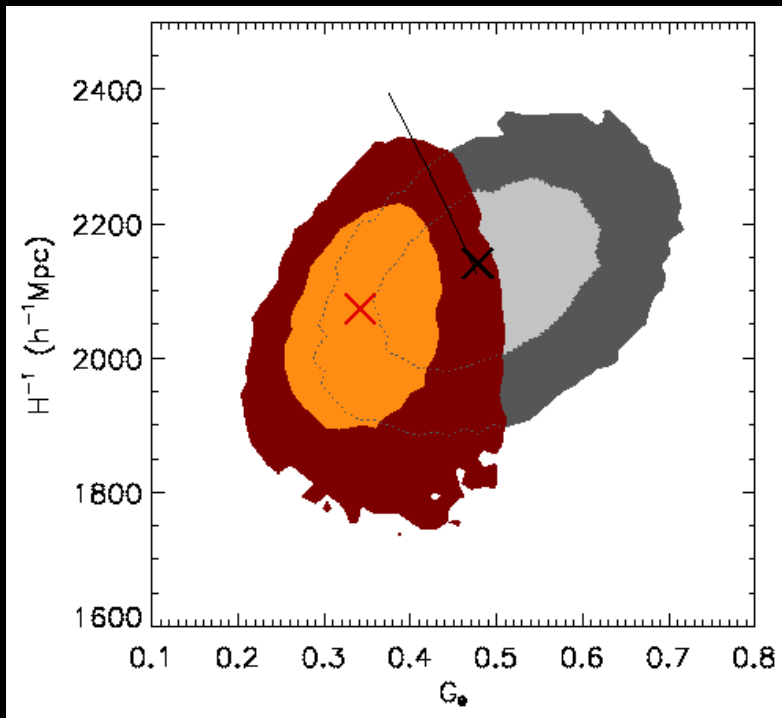
- Testing Cosmology suggests
 - However, for smaller cut-off, allowing using data in small scales, we do find deviation.
 - $G\theta$: underestimated 0.42, 0.34 for smaller cut-off = 30Mpc/h, 20Mpc/h, respectively. But, above 40Mpc/h, invariant, indicating convergence
- No cosmology giving good fits to the measurement contour
- And evidence for a violation of general relativity.
 - The strong growth suppression in the measured growth rate would yield an apparent gravitational growth index > 0.7 , in contrast to the value 0.55 for general relativity.

Linder. E. V.(2005)

5. Testing Cosmology

Planck

(Cut-off=20Mpc/h with 40Mpc/h)



- The shifting of the best fit values & the reduction in the uncertainty of G_{theta}
 - Indicating:
 - Substantial information to fit cosmology is coming from small scales, not just the BAO rings.
- Sensitivity of the results to low cut-off
 - Indicating:
 - Modeling on small scales is inadequate.

2D Clustering Anisotropy Analysis using BOSS DR9

6. CONCLUSION

6. Conclusion

- Using BOSS CMASS DR9 galaxies with CMB prior,
- From the clustering correlation function,
- We can extract the angular diameter distance D_A , Hubble scale H_{inv} , and growth rate G_{θ} , consistent with Λ CDM
- And by comparing expansion of comoving distance with growth of cosmic structure, we also test general relativity, consistent.
- But, improvement is necessary in using small scales data to obtain more robust result.
- The sensitivity of low cut-off to the results gives a spurious signature of breakdown of GR.

Thank you