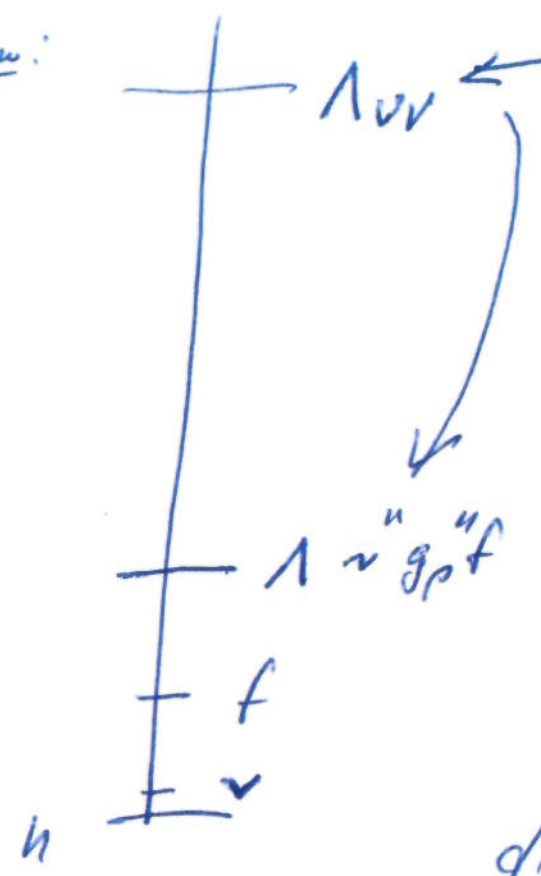


12/7/2017

"STRONG ΣWSB"

Introduction :- Per Tan's Talk - Dynamical Asymptote  
 - LARGE  $\delta$ , operators with intrinsic scaling dimension

Bergshoeff  
Review:



All flavor here  
 Flavor  
 Information from high energies  
 must feed down

$$L = \lambda_L \psi_L \partial_R + \lambda_R \psi_R \partial_L$$

$\dim \partial_{L,R} > 5/2 \rightarrow$  light fermion

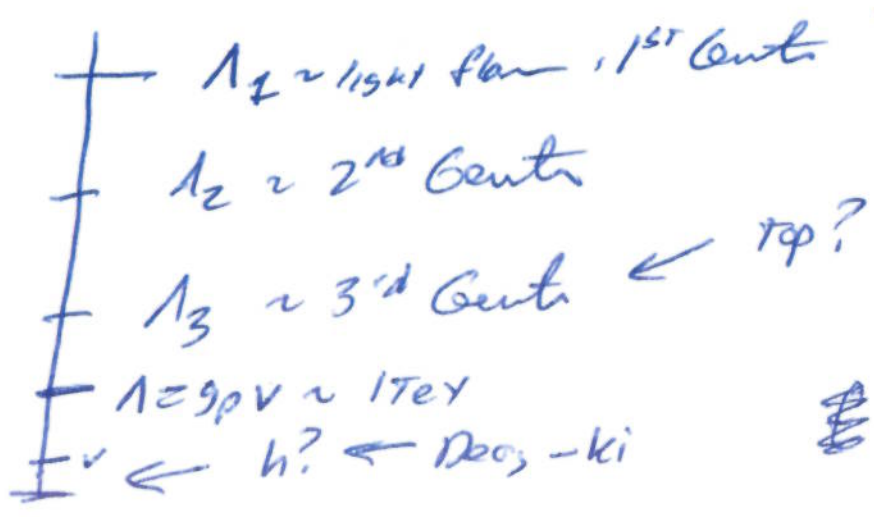
$\dim \partial_{L,R} \sim 5/2$  Top  
 $\hookrightarrow \Rightarrow \psi_{L,R} \partial_{L,R}$  marginal.

$$\dim(\psi\psi) = \frac{9}{2} - \delta$$

$\Rightarrow \delta = \underline{\underline{2}}$  for top

$? \leq \delta < 2$  for light fermions

"ETC" etc

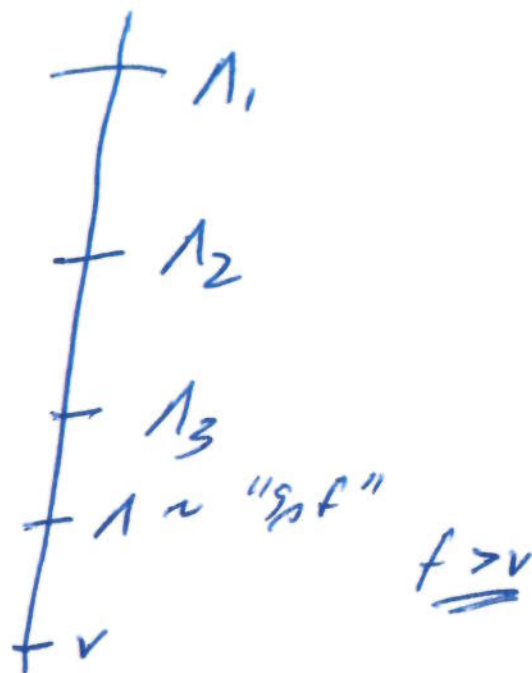


TC  
 What  $\delta_M$   
 is  
 required  
 for  
 flavor?



Composite Higgs/ETC

RSC (B)  
12/7/2017



What  $\gamma$  is used  
to keep fermions?  
 $\Rightarrow \Lambda = "g_{\text{eff}}" \lesssim 10 \text{ TeV}$

{  
ENS  $\rightarrow$  Technicolor/ETC  
RSC  $\rightarrow$  Composite Higgs/ETC  
Also: Partial Compositeness + GA  
Deeg-Ki  $\rightarrow$  Light Higgs/dilaton  
}

ENS

$\rightarrow$  RSC (follows) (GA)

$\rightarrow$  Deeg-Ki

Schematics:  
\* LADDER Approx S-D equations  
\* CJT effective potential  
\* SUSY/Seiberg duality  
\* Holographic Construction, large-N  
input vs. output?

# Walking TC and FCNC

new  $SU(N_{TC})$  gauge force felt by techniquarks

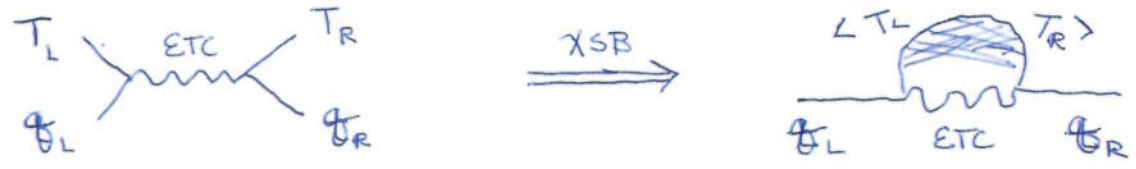
e.g.  $T_L^a \equiv \begin{pmatrix} U^a \\ D^a \end{pmatrix}_L$  and  $U_R^a, D_R^a$

so Lagrangian has  $SU(2)_L \times SU(2)_R$  chiral symmetry

when running gauge coupling becomes strong at  $\Lambda_{TC} \sim 1 \text{ TeV}$ , XSB occurs

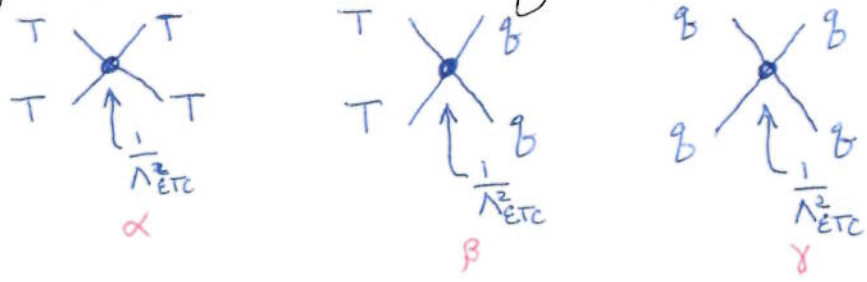
$\langle T_L T_R \rangle \neq 0$ ,  $\Pi_{TC}$  become  $W_L, Z_L$

to generate  $m_f$ , extend TC group to include ETC bosons that couple ordinary and techniquarks



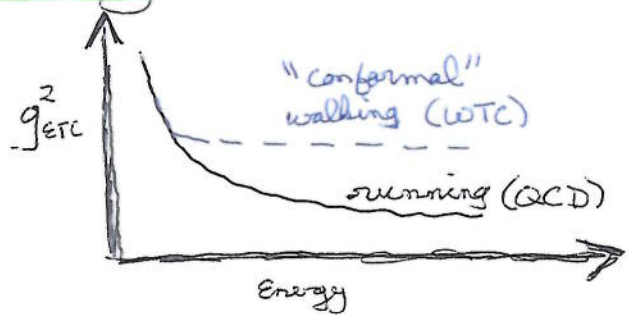
$m_f \sim \left( \frac{g_{ETC}}{M_{ETC}} \right)^2 \langle T_L T_R \rangle \cdot \text{flavor}$   
 $\uparrow \sim 1/\Lambda_{ETC}^2$

but heavy ETC bosons will yield all possible 4-fermion contact interactions among quarks and techniquarks



Since the  $\beta$  terms treat  $q$  of same gauge charges differently to yield varied  $m_f$   
 $\dots$   $\gamma$  terms will be allowed  $\Rightarrow$  FCNC  
 $\Rightarrow$  make  $\Lambda_{ETC}$  too large to produce  $m_f$ !

Walking TC intervenes  $\equiv$



$m_f \approx \frac{g_{ETC}^2}{m_{ETC}^2} \langle \bar{T} T \rangle \equiv \frac{1}{\Lambda_{ETC}^2} \langle \bar{T} T \rangle$

is now larger for a given  $\langle \bar{T} T \rangle$

[flavor symmetry breaking pushed to higher scale]

$$\boxed{\text{Condensate} \rightarrow m_{\delta}}$$

ETC operator  $\frac{1}{\Lambda_{\text{ETC}}^2} (\bar{Q}_L^i \gamma^\mu q_L^j) (\bar{U}_R^i \gamma_\mu U_R^j)$

yields mass term:  $\langle \bar{U}_L U_R \rangle_{\Lambda_{\text{ETC}}} \cdot \Lambda_{\text{ETC}}^{-2}$   
value

But what we know in TC is  $\langle \bar{U}_L U_R \rangle_{\Lambda_{\text{TC}}}$ !

$$\langle \bar{U}_L U_R \rangle_{\Lambda_{\text{ETC}}} = \exp \left( \int_{\Lambda_{\text{TC}}}^{\Lambda_{\text{ETC}}} \gamma_m(\mu) \frac{d\mu}{\mu} \right) \langle \bar{U}_L U_R \rangle_{\Lambda_{\text{TC}}}$$

↑ anomalous dimension of TF mass operator

in extreme walking  $\gamma_m = \text{constant}$

$$\langle \bar{U}_L U_R \rangle_{\Lambda_{\text{ETC}}} = \left( \frac{\Lambda_{\text{ETC}}}{\Lambda_{\text{TC}}} \right)^{\gamma_m} \langle \bar{U}_L U_R \rangle_{\Lambda_{\text{TC}}}$$

$$m_{\delta} = \frac{1}{\Lambda_{\text{ETC}}^2} \left( \frac{\Lambda_{\text{ETC}}}{\Lambda_{\text{TC}}} \right)^{\gamma_m} \langle \bar{U}_L U_R \rangle_{\Lambda_{\text{TC}}}$$

2 common estimates of size of  $\langle \bar{U}_L U_R \rangle_{\Lambda_{\text{TC}}}$

NDA :  $\Lambda_{\text{TC}} \equiv \Lambda_{\chi\text{SB}} = 4\pi v_{\text{ew}}$

$$\langle \bar{U}_L U_R \rangle_{\Lambda_{\text{TC}}} = \left( \frac{\Lambda_{\chi\text{SB}}^3}{(4\pi)^2} \right)$$

$$\Rightarrow m_{\delta}^{\text{NDA}} = \left( \frac{\Lambda_{\chi\text{SB}}}{(4\pi)^2} \right) \left( \frac{\Lambda_{\chi\text{SB}}}{\Lambda_{\text{ETC}}} \right)^{2-\gamma_m}$$

DA :  $\Lambda_{\text{TC}} = 1 \text{ TeV}$

$$\langle \bar{U}_L U_R \rangle_{\Lambda_{\text{TC}}} = \Lambda_{\text{TC}}^3$$

$$\Rightarrow m_{\delta}^{\text{DA}} = \Lambda_{\text{TC}} \left( \frac{\Lambda_{\text{TC}}}{\Lambda_{\text{ETC}}} \right)^{2-\gamma_m}$$

# UTFit Collaboration Limits

Notation :

$$C_{meson}^i = (\bar{q}_L \gamma^\mu q_L') (\bar{q}_L \gamma_\mu q_L')$$

| w/o GIM

| for tree-level FCNC

F<sub>qq'</sub>

L<sub>qq'</sub>

Λ<sup>2</sup>

≡ Λ<sub>ETC</sub><sup>2</sup> in this context

## Reported Limits

CP conserving (ETC not involved in CPV)

$$\text{Re}(C_k^i) \text{ (2016)}, \quad |C_D^i| \text{ (2010)}, \quad |C_{B_d}^i| \text{ (2016)} \quad \rightarrow \quad \Lambda_{ETC} \gtrsim 1,000 \text{ TeV}$$

$$|C_{B_s}^i| \text{ (2016)} \quad \rightarrow \quad \Lambda_{ETC} \gtrsim 200 \text{ TeV}$$

## CP violating

$$\text{Im}(C_k^i) \text{ (2016)} \quad \rightarrow \quad \Lambda_{ETC} \gtrsim 20,000 \text{ TeV}$$

$$\text{Im}(C_D^i) \text{ (2016)} \quad \rightarrow \quad \Lambda_{ETC} \gtrsim 7,000 \text{ TeV}$$

Required  $\gamma_m$  ?

In CP-conserving scenario, UTFIT data on K, D, B<sub>d</sub> all set similar  $\Lambda_{ETC} \geq 1000 \text{ TeV}$

But  $\gamma_m$  required for walking ETC to generate associated quark mass is quite different

	$m_s$	$m_c$	$m_b$
NDA	0.75	1.5	1.75
DA	0.4	1.0	1.25

In CPV scenario, UTFIT finds K data sets highest limit  $\Lambda_{ETC} > 20,000 \text{ TeV}$

⇒  $\gamma_m^{NDA}$  needed for  $m_s$  is 1.25  
 $\gamma_m^{DA}$  " " " " 0.9

Yet, CPV limit from D data saying  $\Lambda_{ETC} > 7,000 \text{ GeV}$  requires higher  $\gamma_m$  to generate the heavier charm mass

⇒  $\gamma_m^{NDA}$  needed for  $m_c$  is 1.625  
 $\gamma_m^{DA}$  " " " " 1.25

## Conclusions

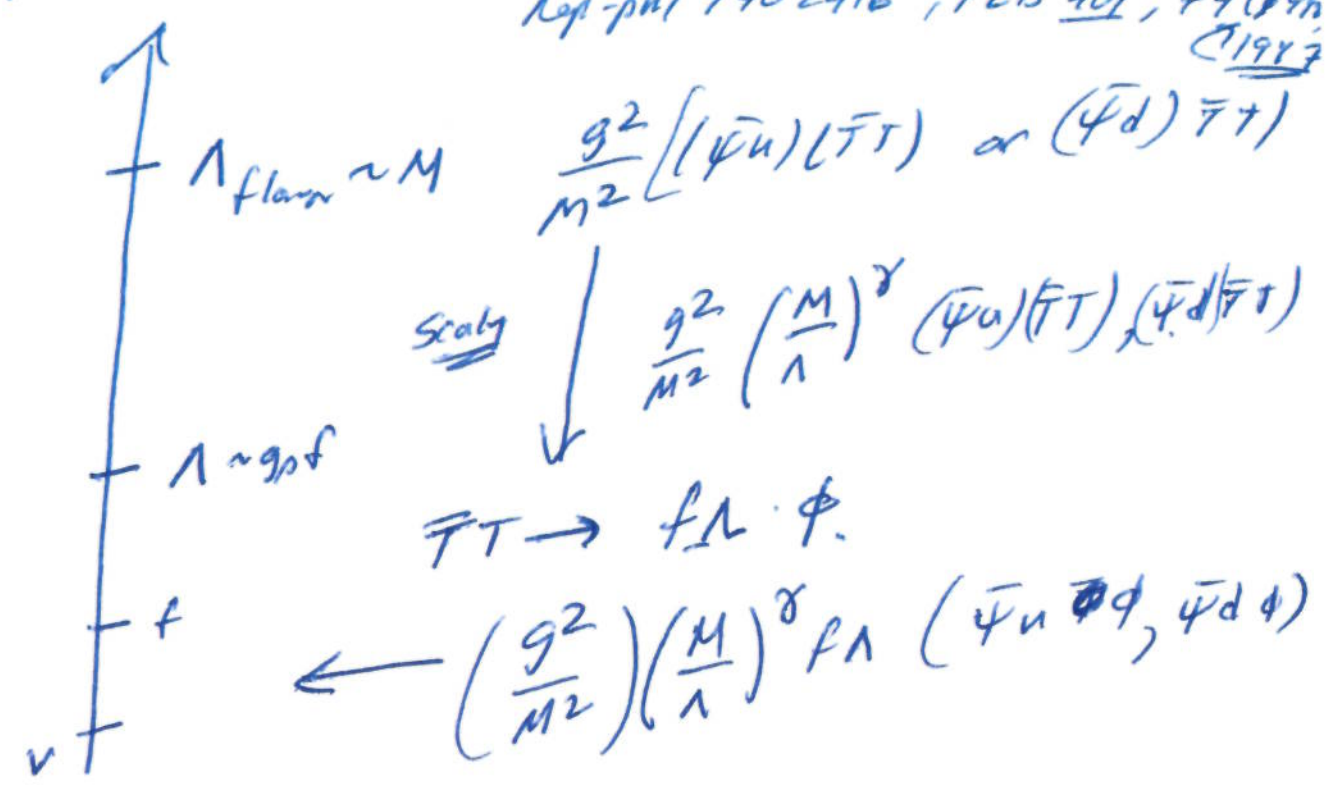
Even with lower DA estimates, using walking ETC to produce  $m_g$  requires  $\gamma_m \gtrsim 1$

- we've neglected details like  $N_{TC}$  effects, # weak doublets in TC sector, and possibility of less extreme walking ... all of which would lower produced  $m_g$
- need lattice to determine feasible  $\gamma_m$  in specific WTC theories, & if  $\gamma_m < 1$  one would need to incorporate flavor symmetries into theory
- also interesting to know more @ composite scalars that can be part of WTC with high  $\gamma_m$  (how light? how broad?)

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Note -  $\gamma_m$  scheme-independent strictly only at conformal point & but WTC is nearly conformal so one could extrapolate

"Composite Higgs/ETC", RSC, Dolan, EHS 12/7/2017  
 hep-ph/9702416, PLB 401, 74 (1998) 1983



$M_{\text{gluon}} \sim \frac{g^2}{M^2} \left(\frac{M}{\Lambda}\right)^\gamma f \Lambda \approx \frac{\sqrt{2} M g}{v}$

delta\_20: "TC-like" Composite Higgs vs.  $g_p v^3 \leftarrow TC$   
 $m_g \sim \frac{g^2}{M^2} f \Lambda v = g_p f^2 v$

$\Rightarrow$  Enhanced by  $\left(\frac{f^2}{v^2}\right)$  wrt Technicolor or Mixing Angles

TAW  $\Lambda$  fixed  $\sim 10 \text{ TeV}$ ,  $\frac{M}{g} \gtrsim 100 \text{ TeV}$   
 $f \sim 1 \text{ TeV}$

$M_g \sim \frac{g^2}{(100 \text{ TeV})^2} 10 \cdot (1 \text{ TeV})^2 \frac{250 \text{ GeV}}{\sqrt{2}}$

Need delta for heavy quarks  $\sim 9 \cdot 10^{-4} \cdot 2500 \text{ GeV} \approx 200 \text{ MeV} \cdot g^2$   
M\_s on! Not charm or strange

$\delta = 1$

$M = 100 \text{ TeV}, f = 1 \text{ TeV}$   
 $\Lambda = 10 \text{ TeV}$

(D)

$M_q \approx \frac{v}{\sqrt{2}} \frac{g^2}{M^2} \left(\frac{M}{\Lambda}\right) f \Lambda$

$\approx \frac{v}{\sqrt{2}} \frac{g^2}{M} f \approx \frac{250 \text{ GeV}}{\sqrt{2}} \frac{(1)}{(100 \text{ TeV})} (\text{TeV})$

$\approx 2.25 \text{ GeV} \leftarrow \text{CHARM bottom?}$

$\delta = 2$

~~$M_q \approx \frac{v}{\sqrt{2}} \frac{g^2}{M^2} \left(\frac{M}{\Lambda}\right)^2 f \Lambda$~~

NFL limit  $\Rightarrow$  Excluded Scales

M invariant

YUKAWA  $\sim \frac{g^2}{M^2} \left(\frac{M}{\Lambda}\right)^2 f \Lambda \sim g^2 \frac{f}{\Lambda}$

$\sim \frac{1}{10} - 1 \leftarrow \text{bottom top} \Rightarrow$

Despite the enhancement by  $\left(\frac{f}{v}\right)^2$ , still

need  $\delta \sim 1-2$  to explain quark masses

in a Composite Higgs Physics

ETC-like